

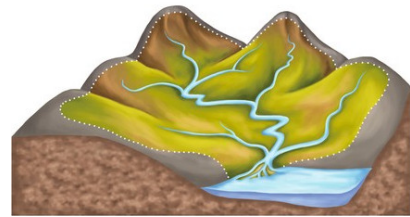
## PROBLEM I

## WATERSHEDS

30 POINTS

Geologists sometimes divide an area of land into different regions based on where rainfall flows down to. These regions are called *drainage basins*.

Given an elevation map (a 2-dimensional array of altitudes), label the map such that locations in the same drainage basin have the same label, subject to the following rules.



- From each cell, water flows down to at most one of its 4 neighbouring cells.
- For each cell, if none of its 4 neighbouring cells has a lower altitude than the current cell's, then the water does not flow, and the current cell is called a *sink*.
- Otherwise, water flows from the current cell to the neighbour with the lowest altitude.
- In case of a tie, water will choose the first direction with the lowest altitude from this list: North, West, East, South.

Every cell that drains directly or indirectly to the same sink is part of the same drainage basin. Each basin is labelled by a unique lower-case letter, in such a way that, when the rows of the map are concatenated from top to bottom, the resulting string is lexicographically smallest (in particular, the basin of the most North-Western cell is always labelled 'a'). Note that neighbouring sinks are not considered to be in the same drainage basin.

**Input**

The first line of the input contains two integers –  $H$  and  $W$  – the height and width of the map, in cells ( $1 \leq H, W \leq 100$ ). The next  $H$  lines will each contain a row of the map, from north to south, each containing  $W$  integers, from west to east, specifying the altitudes of the cells ( $0 \leq \text{altitudes} < 10,000$ ). It is guaranteed that there will be at most 26 basins.

**Output**

Output  $H$  lines that list the basin labels for each of the cells, in the same order as they appear in the input.

**Turn over for sample input and output.**

**Sample Input 1**

```
3 3
9 6 3
5 9 6
3 5 9
```

**Output for Sample Input 1**

```
a b b
a a b
a a a
```

**Explanation of Sample 1**

The upper-right and lower-left corners are sinks. Water from the diagonal flows towards the lower-left because of the lower altitude (5 versus 6).

**Sample Input 2**

```
1 10
0 1 2 3 4 5 6 7 8 7
```

**Output for Sample Input 3**

```
a a a a a a a a a b
```

**Sample Input 3**

```
2 3
7 6 7
7 6 7
```

**Output for Sample Input 3**

```
a a a
b b b
```

**Sample Input 4**

```
5 5
1 2 3 4 5
2 9 3 9 6
3 3 0 8 7
4 9 8 9 8
5 6 7 8 9
```

**Output for Sample Input 4**

```
a a a a a
a a b b a
a b b b a
a b b b a
a a a a a
```