

wk6_hw5_p1

November 7, 2024

```
[1]: from models import *
      from utilities import Utilities as helper
      from utilities import AverageMeter
      from data_loader import trainloader
      from data_loader import testloader
```

=> Building model...

Files already downloaded and verified

Files already downloaded and verified

```
[2]: model_name = "resnet20_quan"
      resnet20_model_quan = resnet20_quant().cuda()
```

```
[ ]: lr = 7e-3
      weight_decay = 1e-4
      epochs = 100
      # pre_best_prec = 85.470

      criterion = nn.CrossEntropyLoss().cuda()

      res20_optimizer = torch.optim.SGD(resnet20_model_quan.parameters(), lr=lr,
      ↪momentum=0.9, weight_decay=weight_decay)
      pre_best_prec = helper.train_model(resnet20_model_quan, model_name=model_name,
      ↪optimizer=res20_optimizer, trainloader=trainloader, testloader=testloader,
      ↪criterion=criterion, epochs=epochs, pre_best_prec=pre_best_prec)
```

```
[8]: helper.test_model(model=resnet20_model_quan, model_name=model_name,
      ↪testloader=testloader)
```

Test: [0/79] Time 0.190 (0.190) Loss 0.2105 (0.2105) Prec 93.750%
(93.750%)

* Prec 90.380%

```
[4]: w_bit = 4
      quan_con_layer = next(resnet20_model_quan.layer1[0].modules()).conv1
      weight_q = quan_con_layer.weight_q # quantized value is stored during the
      ↪training
```

```

w_alpha = quan_con_layer.weight_quant.wgt_alpha.data.item() # alpha is defined
↳ in your model already. bring it out here
w_delta = w_alpha/(2**(w_bit-1)-1) # delta can be calculated by using alpha
↳ and w_bit
weight_int = weight_q/w_delta # w_int can be calculated by weight_q and w_delta
print(weight_int) # you should see clean integer numbers

# conv.weight = torch.nn.Parameter(torch.randn(n_ch_out,n_ch_in,k_size,k_size))
# #####

# weight_quant = weight_quantize_fn(w_bit= w_bits) ## define quant function
# weight_quant.wgt_alpha = torch.tensor(w_alpha)
# w_quant = weight_quant(conv.weight)
# w_delta = w_alpha/(2**(w_bits-1)-1)
# w_int = w_quant/w_delta

```

```

tensor([[[[-0.0000,  0.0000,  0.0000],
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          [-1.0000, -0.0000,  1.0000]],

        [[ 2.0000, -0.0000, -1.0000],
          [-1.0000, -4.0000, -5.0000],
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        [[ 2.0000,  2.0000,  2.0000],
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          [ 2.0000,  3.0000,  2.0000]],

        ...,

        [[-0.0000, -4.0000, -1.0000],
          [-2.0000, -5.0000, -0.0000],
          [-1.0000, -3.0000,  1.0000]],

        [[ 1.0000, -3.0000, -3.0000],
          [ 2.0000, -3.0000, -4.0000],
          [ 3.0000, -1.0000, -2.0000]],

        [[ 3.0000,  2.0000,  1.0000],
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        [[[-5.0000, -7.0000, -5.0000],
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```

```

[ 2.0000,  6.0000,  4.0000]],

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...,

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 [-0.0000, -1.0000, -3.0000],
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[[-1.0000, -3.0000,  0.0000],

```

```

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...,

[[[-2.0000, -1.0000, -2.0000],
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  [-1.0000,  1.0000,  3.0000]],

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[[[-1.0000,  1.0000,  0.0000],
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...,

```

```

[[[-2.0000, -1.0000, 1.0000],
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  [-0.0000, 0.0000, -3.0000]],

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[[ 0.0000, 1.0000, 0.0000],
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  [ 1.0000, 1.0000, 1.0000]],

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  [ 0.0000, -1.0000, -0.0000]],

...,

[[-2.0000, -1.0000, -0.0000],
  [-1.0000, 1.0000, 1.0000],
  [ 0.0000, 1.0000, 1.0000]],

[[-0.0000, 0.0000, 1.0000],
  [-0.0000, -2.0000, -0.0000],
  [ 0.0000, -3.0000, -1.0000]],

[[-3.0000, -1.0000, -0.0000],
  [ 0.0000, 1.0000, 0.0000],
  [-0.0000, 2.0000, 2.0000]]], device='cuda:0',
grad_fn=<DivBackward0>)

```

```
[5]: from saveOutput import SaveOutput
```

```

resnet_save_out = SaveOutput()
blocks_res = SaveOutput.hook(resnet20_model_quant.layer1.modules(), QuantConv2d,
↪resnet_save_out)

```

```

prehooked
prehooked

```

prehooked
prehooked
prehooked
prehooked

```
[6]: def act_quantization(b):

    def uniform_quant(x, b=3):
        xdiv = x.mul(2 ** b - 1)
        xhard = xdiv.round().div(2 ** b - 1)
        return xhard

    class uq(torch.autograd.Function): # here single underscore means this_
    ↪ class is for internal use

        def forward(ctx, input, alpha):
            input_d = input/alpha
            input_c = input_d.clamp(max=1) # Mingu edited for Alexnet
            input_q = uniform_quant(input_c, b)
            ctx.save_for_backward(input, input_q)
            input_q_out = input_q.mul(alpha)
            return input_q_out

    return uq().apply
```

```
[9]: x = resnet_save_out.outputs[0][0] # input of the 2nd conv layer
x_bit = 4

x_alpha = 3.284
x_delta = x_alpha/(2**x_bit-1)

act_quant_fn = act_quantization(x_bit) # define the quantization function
x_q = act_quant_fn(x, x_alpha) # create the quantized value for x

x_int = x_q/x_delta
print(x_int) # you should see clean integer numbers
```

```
tensor([[[[ 2.0000,  4.0000,  4.0000, ...,  5.0000,  5.0000,  3.0000],
           [ 2.0000,  4.0000,  4.0000, ...,  4.0000,  4.0000,  3.0000],
           [ 3.0000,  4.0000,  4.0000, ...,  3.0000,  4.0000,  3.0000],
           ...,
           [ 0.0000,  0.0000,  0.0000, ...,  0.0000,  0.0000,  0.0000],
           [ 0.0000,  0.0000,  0.0000, ...,  0.0000,  0.0000,  0.0000],
           [ 0.0000,  0.0000,  0.0000, ...,  0.0000,  0.0000,  0.0000]],
        [[ 4.0000,  1.0000,  1.0000, ...,  0.0000,  0.0000,  1.0000],
         [10.0000,  7.0000,  8.0000, ...,  7.0000,  6.0000,  4.0000],
         [ 9.0000,  7.0000,  7.0000, ...,  8.0000,  6.0000,  4.0000],
```

```

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...,
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```

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```



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...,

```

```

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```

```

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...,

[[[ 0.0000, 4.0000, 4.0000, ..., 4.0000, 4.0000, 7.0000],
[ 0.0000, 3.0000, 2.0000, ..., 3.0000, 3.0000, 8.0000],
[ 0.0000, 2.0000, 2.0000, ..., 3.0000, 3.0000, 8.0000],
...,
[ 0.0000, 3.0000, 2.0000, ..., 3.0000, 3.0000, 1.0000],
[ 1.0000, 3.0000, 2.0000, ..., 3.0000, 2.0000, 0.0000],
[ 0.0000, 1.0000, 1.0000, ..., 1.0000, 1.0000, 0.0000]]],

[[[ 7.0000, 3.0000, 3.0000, ..., 3.0000, 3.0000, 0.0000],
[ 7.0000, 2.0000, 2.0000, ..., 2.0000, 2.0000, 0.0000],
[ 7.0000, 2.0000, 2.0000, ..., 2.0000, 2.0000, 0.0000],
...,
[ 4.0000, 2.0000, 3.0000, ..., 3.0000, 3.0000, 6.0000],
[ 4.0000, 3.0000, 3.0000, ..., 3.0000, 3.0000, 6.0000],
[ 3.0000, 2.0000, 2.0000, ..., 2.0000, 2.0000, 4.0000]]],

[[[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],

```

```

[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
...,
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000]]],

[[[ 2.0000, 3.0000, 3.0000, ..., 6.0000, 7.0000, 6.0000],
[ 2.0000, 2.0000, 2.0000, ..., 5.0000, 6.0000, 5.0000],
[ 2.0000, 3.0000, 2.0000, ..., 5.0000, 6.0000, 5.0000],
...,
[ 0.0000, 0.0000, 0.0000, ..., 6.0000, 6.0000, 5.0000],
[ 0.0000, 0.0000, 0.0000, ..., 6.0000, 6.0000, 5.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000]]],

[[ 0.0000, 1.0000, 1.0000, ..., 0.0000, 0.0000, 5.0000],
[ 5.0000, 6.0000, 6.0000, ..., 3.0000, 3.0000, 3.0000],
[ 4.0000, 4.0000, 5.0000, ..., 3.0000, 3.0000, 3.0000],
...,
[ 6.0000, 5.0000, 5.0000, ..., 3.0000, 3.0000, 3.0000],
[ 6.0000, 7.0000, 8.0000, ..., 3.0000, 3.0000, 3.0000],
[ 8.0000, 5.0000, 5.0000, ..., 4.0000, 5.0000, 6.0000]]],

[[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
[ 0.0000, 0.0000, 0.0000, ..., 0.0000, 0.0000, 0.0000],
...,
[ 3.0000, 3.0000, 3.0000, ..., 0.0000, 0.0000, 0.0000],
[ 3.0000, 2.0000, 2.0000, ..., 0.0000, 0.0000, 0.0000],
[ 2.0000, 1.0000, 1.0000, ..., 0.0000, 0.0000, 0.0000]]],

...,

[[ 9.0000, 3.0000, 3.0000, ..., 5.0000, 4.0000, 0.0000],
[11.0000, 4.0000, 3.0000, ..., 5.0000, 4.0000, 0.0000],
[11.0000, 5.0000, 2.0000, ..., 6.0000, 4.0000, 0.0000],
...,
[ 0.0000, 3.0000, 3.0000, ..., 6.0000, 4.0000, 0.0000],
[ 0.0000, 2.0000, 2.0000, ..., 5.0000, 3.0000, 0.0000],
[ 1.0000, 4.0000, 4.0000, ..., 4.0000, 3.0000, 0.0000]]],

[[ 0.0000, 2.0000, 2.0000, ..., 1.0000, 2.0000, 12.0000],
[ 0.0000, 2.0000, 4.0000, ..., 1.0000, 2.0000, 15.0000],
[ 0.0000, 2.0000, 4.0000, ..., 0.0000, 2.0000, 15.0000],
...,
[ 6.0000, 3.0000, 2.0000, ..., 1.0000, 3.0000, 15.0000],
[ 5.0000, 3.0000, 3.0000, ..., 1.0000, 3.0000, 15.0000],
[ 4.0000, 3.0000, 2.0000, ..., 0.0000, 1.0000, 11.0000]]],

```

```

[[ 6.0000,  3.0000,  4.0000, ...,  9.0000,  9.0000,  3.0000],
 [ 4.0000,  2.0000,  1.0000, ...,  7.0000,  7.0000,  4.0000],
 [ 4.0000,  3.0000,  2.0000, ...,  7.0000,  7.0000,  4.0000],
 ...,
 [ 0.0000,  0.0000,  0.0000, ...,  7.0000,  7.0000,  4.0000],
 [ 0.0000,  0.0000,  0.0000, ...,  7.0000,  7.0000,  4.0000],
 [ 0.0000,  0.0000,  0.0000, ..., 10.0000, 10.0000,  6.0000]]],
device='cuda:0')

```

```

[10]: conv_quan = nn.Conv2d(16, 16, kernel_size=(3, 3), padding=(1, 1), bias=False)
conv_quan.weight = torch.nn.Parameter(weight_int)

psum_int = conv_quan(x_int)
print("psum int:", psum_int)
psum_recovered = psum_int*w_delta*x_delta

```

```

psum int: tensor([[[[ 3.6000e+01,  1.5300e+02,  1.7800e+02, ...,  1.7400e+02,
                    1.1400e+02,  5.1000e+01],
 [-8.8000e+01,  1.6000e+01,  3.4000e+01, ...,  1.5000e+01,
 -9.0000e+00, -1.6000e+01],
 [-1.1100e+02,  7.0000e+00, -5.0000e+00, ...,  2.0000e+00,
  1.3000e+01,  2.0000e+01],
 ...,
 [ 2.4800e+02,  2.1200e+02,  2.1300e+02, ...,  1.6900e+02,
  1.3900e+02, -3.3000e+01],
 [ 1.7400e+02,  1.8600e+02,  1.8900e+02, ...,  1.5000e+02,
  1.2800e+02, -3.8000e+01],
 [ 1.0600e+02,  1.2200e+02,  1.2800e+02, ...,  1.4100e+02,
  9.7000e+01,  2.6000e+01]]],

[[ 1.3500e+02,  2.2400e+02,  2.6300e+02, ...,  2.4900e+02,
  2.8600e+02,  2.7000e+01],
 [-3.5000e+01,  2.5000e+01,  4.4000e+01, ...,  9.0000e+00,
  1.3000e+01, -1.0600e+02],
 [ 2.7000e+01,  6.5000e+01,  6.5000e+01, ...,  1.0000e+01,
  3.5000e+01, -7.3000e+01],
 ...,
 [ 1.1400e+02, -9.3000e+01, -5.2000e+01, ...,  5.8000e+01,
 -2.1500e+02, -8.2000e+01],
 [ 1.6200e+02,  3.5000e+01,  5.0000e+00, ...,  3.0000e+00,
  1.5900e+02, -1.8200e+02],
 [ 1.6400e+02,  2.4600e+02,  1.9900e+02, ...,  1.5300e+02,
  4.2700e+02, -1.5100e+02]]],

[[ 1.6600e+02,  1.4400e+02,  4.1000e+01, ...,  9.2000e+01,
  1.4600e+02,  3.0000e+01],
 [ 9.2000e+01,  5.1000e+01, -4.7000e+01, ..., -7.3000e+01,

```

```

    1.6000e+01, -1.1800e+02],
  [ 7.9000e+01,  4.0000e+00, -3.8000e+01, ..., -8.2000e+01,
    -4.0000e+00, -7.8000e+01],
  ...,
  [-2.1800e+02,  3.3000e+01,  1.4200e+02, ...,  8.8000e+01,
    -4.0000e+00,  1.8300e+02],
  [ 4.0000e+00,  1.6000e+01,  1.5500e+02, ...,  2.3900e+02,
    -7.8000e+01,  2.3600e+02],
  [ 1.2400e+02,  1.3000e+02,  1.4300e+02, ...,  1.3400e+02,
    1.9000e+01,  1.0200e+02]],
  ...,
  [[ 2.6800e+02,  2.7600e+02,  2.5900e+02, ...,  2.2900e+02,
     2.3600e+02,  1.3200e+02],
   [ 4.8000e+01,  1.0400e+02,  9.8000e+01, ...,  1.4100e+02,
     2.0100e+02,  9.5000e+01],
   [ 1.7400e+02,  2.5100e+02,  2.5500e+02, ...,  2.8700e+02,
     2.4400e+02,  2.0900e+02],
   ...,
   [ 5.6000e+01,  4.0200e+02,  1.9600e+02, ...,  1.4900e+02,
     2.9900e+02, -2.0000e+00],
   [ 2.1000e+02,  3.7900e+02,  2.9400e+02, ...,  3.8500e+02,
     2.1100e+02,  1.4100e+02],
   [ 2.0200e+02,  2.5400e+02,  1.5300e+02, ...,  2.4600e+02,
     2.7500e+02,  2.8000e+01]],
  [[-1.7600e+02, -3.2300e+02, -3.9600e+02, ..., -3.3900e+02,
     -3.7400e+02, -3.6800e+02],
   [-1.1200e+02, -3.0300e+02, -4.3700e+02, ..., -3.3200e+02,
     -4.1500e+02, -4.4800e+02],
   [-9.5000e+01, -2.4800e+02, -3.8400e+02, ..., -2.2800e+02,
     -3.2500e+02, -4.1600e+02],
   ...,
   [-3.6700e+02, -2.0100e+02, -2.1500e+02, ..., -6.6000e+01,
     -1.3900e+02, -5.0000e+00],
   [-3.6300e+02, -2.2400e+02, -2.7700e+02, ..., -1.4800e+02,
     -1.5300e+02, -6.5000e+01],
   [-3.8200e+02, -3.2500e+02, -3.6200e+02, ..., -2.8200e+02,
     -2.6400e+02, -1.4100e+02]],
  [[-7.4000e+01, -1.8900e+02, -2.1100e+02, ..., -1.6900e+02,
     -1.7500e+02, -3.5000e+01],
   [-1.7300e+02, -3.7800e+02, -3.9100e+02, ..., -3.1900e+02,
     -3.0700e+02, -2.3200e+02],
   [-1.2400e+02, -3.5900e+02, -3.5100e+02, ..., -2.8400e+02,
     -2.8900e+02, -1.9500e+02],
   ...,

```

```

[-1.2800e+02, -1.0100e+02, -7.6000e+01, ..., -1.1200e+02,
 -1.2800e+02, -7.1000e+01],
[-7.1000e+01, -1.3000e+02, -9.5000e+01, ..., -3.8000e+01,
 -2.9500e+02, -1.6000e+01],
[ 7.0000e+00, -6.1000e+01, -5.3000e+01, ..., -2.7000e+01,
 -1.0800e+02,  6.0000e+00]]],

[[[ 4.6000e+01,  1.1000e+01, -6.1000e+01, ..., -5.5000e+01,
    -1.4000e+01, -6.2000e+01],
 [ 2.6000e+01,  7.1000e+01, -2.4000e+01, ..., -2.2000e+01,
    -2.4000e+01, -9.7000e+01],
 [ 6.9000e+01,  1.3300e+02,  5.2000e+01, ...,  4.8000e+01,
    2.9000e+01, -6.4000e+01],
 ...,
 [ 9.0000e+00, -5.2000e+01,  3.4000e+01, ...,  1.1700e+02,
    1.3600e+02,  5.0000e+00],
 [-1.2000e+01, -5.8000e+01,  1.6000e+01, ...,  1.8700e+02,
    2.1800e+02,  7.9000e+01],
 [-2.3000e+01, -3.5000e+01,  8.5831e-06, ..., -3.1000e+01,
    -8.0000e+00, -8.7000e+01]]],

[[-1.2900e+02, -2.4400e+02, -1.7100e+02, ..., -1.8000e+02,
    -1.8100e+02, -1.6200e+02],
 [-6.3000e+01, -3.0500e+02, -1.1000e+02, ..., -1.1600e+02,
    -9.6000e+01, -8.5000e+01],
 [-3.5000e+01, -2.8400e+02, -7.6000e+01, ..., -7.7000e+01,
    -5.4000e+01, -8.3000e+01],
 ...,
 [ 2.1500e+02, -3.0000e+00,  5.5000e+01, ..., -9.2000e+01,
    -3.7000e+01, -8.4000e+01],
 [ 1.9900e+02, -6.2000e+01,  1.2700e+02, ..., -1.0100e+02,
    -3.1000e+01, -1.1100e+02],
 [ 1.5200e+02,  1.9000e+01,  1.3800e+02, ..., -1.3000e+01,
    -9.0000e+00,  5.2000e+01]]],

[[-3.7600e+02, -1.8200e+02, -1.5800e+02, ..., -1.6400e+02,
    -2.4900e+02, -2.1400e+02],
 [-3.2700e+02, -9.4000e+01, -5.5000e+01, ..., -5.5000e+01,
    -1.2400e+02, -1.0400e+02],
 [-2.8800e+02, -6.6000e+01, -1.9000e+01, ..., -8.0000e+00,
    -1.0400e+02, -8.9000e+01],
 ...,
 [-8.1000e+01,  1.4700e+02, -2.4000e+01, ..., -1.4000e+02,
    -1.9200e+02, -5.7000e+01],
 [-3.8000e+01,  7.2000e+01, -5.7000e+01, ..., -1.9600e+02,
    -2.7100e+02, -1.4100e+02],
 [-9.4000e+01, -1.3600e+02, -1.8300e+02, ...,  2.3500e+02,

```

```

2.1700e+02, 1.1900e+02]],
...,
[[ 1.1400e+02, 5.0900e+02, 4.0900e+02, ..., 3.9700e+02,
   3.4900e+02, 9.2000e+01],
 [ 6.7000e+01, 4.0800e+02, 3.5000e+02, ..., 3.4300e+02,
   2.5000e+02, 2.2600e+02],
 [ 1.0000e+02, 3.5000e+02, 3.2800e+02, ..., 3.2200e+02,
   2.0900e+02, 1.8800e+02],
 ...,
 [ 1.5000e+01, 3.0300e+02, 1.4900e+02, ..., 2.4900e+02,
   1.4300e+02, 8.2000e+01],
 [ 1.4000e+02, 2.8000e+02, 1.7400e+02, ..., 2.3200e+02,
   1.4900e+02, 1.1300e+02],
 [ 1.3300e+02, 2.1100e+02, 1.2500e+02, ..., 8.3000e+01,
   1.8000e+01, 2.6000e+01]],

[[-2.9800e+02, -2.6000e+02, -2.2400e+02, ..., -2.3200e+02,
  -1.7000e+02, -2.0000e+01],
 [-4.8600e+02, -4.4800e+02, -4.2200e+02, ..., -4.2700e+02,
  -3.5800e+02, -1.2000e+02],
 [-3.8100e+02, -3.4000e+02, -3.0300e+02, ..., -3.0100e+02,
  -2.6600e+02, -4.7000e+01],
 ...,
 [-9.1000e+01, -1.4200e+02, -2.5600e+02, ..., -2.3400e+02,
  -2.3900e+02, -7.4000e+01],
 [-5.2000e+01, -1.2500e+02, -2.2200e+02, ..., -2.2600e+02,
  -1.9700e+02, -7.9000e+01],
 [-2.7000e+01, -8.9000e+01, -1.2300e+02, ..., -3.4200e+02,
  -2.8600e+02, -1.0600e+02]],

[[-2.4900e+02, -1.4800e+02, -1.5100e+02, ..., -1.5900e+02,
  -1.0900e+02, -1.0000e+02],
 [-2.6800e+02, -2.6100e+02, -2.6700e+02, ..., -2.7100e+02,
  -1.7400e+02, -1.2400e+02],
 [-1.9000e+02, -1.5600e+02, -1.7500e+02, ..., -1.7600e+02,
  -8.7000e+01, -7.9000e+01],
 ...,
 [-8.0000e+01, -9.0000e+01, -1.7300e+02, ..., -2.1400e+02,
  -1.5400e+02, -7.1000e+01],
 [-9.1000e+01, -1.9200e+02, -2.6400e+02, ..., -2.3600e+02,
  -1.5500e+02, -8.8000e+01],
 [-7.4000e+01, -1.8200e+02, -2.3000e+02, ..., -1.4200e+02,
  -8.5000e+01, -1.0100e+02]]],

[[[ 1.2100e+02, 6.5000e+01, -6.5000e+01, ..., -1.0900e+02,

```



```

    6.0000e+00, -5.8000e+01],
    [ 1.6900e+02,  1.7000e+02,  2.3000e+01, ..., -7.2000e+01,
      3.7000e+01, -7.7000e+01],
    [ 1.8500e+02,  1.8300e+02,  2.4000e+01, ..., -1.9000e+01,
      7.5000e+01, -4.9000e+01],
    ...,
    [-6.7000e+01,  4.6000e+01,  5.5000e+01, ...,  6.1000e+01,
      -9.9000e+01, -1.3000e+02],
    [-6.3000e+01,  2.3000e+01,  3.9000e+01, ..., -1.1000e+01,
      -9.7000e+01, -1.5400e+02],
    [ 7.0000e+00,  6.7000e+01,  8.5000e+01, ...,  6.7000e+01,
      -1.6000e+01, -4.3000e+01]],

    [[-1.8000e+02, -2.2800e+02, -2.9100e+02, ..., -2.3900e+02,
      -1.3900e+02, -1.5700e+02],
     [-1.2000e+01, -1.0100e+02, -1.3600e+02, ..., -2.2100e+02,
      -1.9000e+01, -9.2000e+01],
     [ 2.0000e+00, -1.3300e+02, -1.1100e+02, ..., -2.0700e+02,
       6.6000e+01, -1.1600e+02],
     ...,
     [-5.7000e+01,  1.1900e+02, -6.0000e+00, ...,  1.9400e+02,
       9.8000e+01, -3.3300e+02],
     [-4.8000e+01,  1.8300e+02,  8.3000e+01, ...,  1.8200e+02,
       1.0700e+02, -2.6900e+02],
     [-6.0000e+00,  2.5200e+02,  1.5900e+02, ...,  5.4000e+01,
       1.5000e+02, -2.6600e+02]],

    [[-4.0100e+02, -2.9600e+02, -4.8000e+01, ..., -8.9000e+01,
      -3.3800e+02, -2.3100e+02],
     [-3.0400e+02, -1.2200e+02,  7.3000e+01, ...,  4.2000e+01,
      -2.3600e+02, -9.0000e+01],
     [-2.3500e+02, -6.6000e+01,  1.2100e+02, ...,  1.2700e+02,
      -2.0300e+02, -7.1000e+01],
     ...,
     [ 1.6000e+02, -6.2000e+01, -4.2000e+01, ...,  5.7000e+01,
       1.5600e+02,  8.0000e+01],
     [ 2.2400e+02,  2.9000e+01,  6.0000e+00, ...,  2.7200e+02,
       1.3700e+02,  6.5000e+01],
     [-6.8000e+01, -1.3300e+02, -1.3300e+02, ..., -1.0100e+02,
      -2.2500e+02, -1.1300e+02]],

    ...,

    [[ 5.5000e+01,  2.6600e+02,  3.0700e+02, ...,  4.1200e+02,
      3.1100e+02,  1.1200e+02],
     [ 8.7000e+01,  3.3200e+02,  3.4500e+02, ...,  3.6600e+02,
      1.7800e+02,  2.5600e+02],
     [ 1.0000e+02,  2.5200e+02,  3.1400e+02, ...,  3.8900e+02,

```

```

    9.4000e+01, 2.2800e+02],
...,
[ 1.2100e+02, 1.0300e+02, 1.4300e+02, ..., 2.4000e+01,
  4.0300e+02, 1.2200e+02],
[ 2.0900e+02, 1.4300e+02, 1.6000e+02, ..., 1.8800e+02,
  3.8000e+02, 1.0200e+02],
[ 1.8300e+02, 1.8100e+02, 1.1500e+02, ..., 1.6700e+02,
  3.0000e+02, 9.8000e+01]],

[[-1.7600e+02, -5.1000e+01, -5.8000e+01, ..., -2.3500e+02,
  -1.7100e+02, -6.0000e+00],
 [-4.1400e+02, -2.9400e+02, -2.9200e+02, ..., -4.4300e+02,
  -3.6800e+02, -1.0300e+02],
 [-3.8700e+02, -3.1500e+02, -2.8200e+02, ..., -3.2800e+02,
  -2.7500e+02, -2.6000e+01],
...,
 [-2.1500e+02, -2.7300e+02, -2.2200e+02, ..., -1.7300e+02,
  -2.5200e+02, -2.6300e+02],
 [-1.7800e+02, -2.7500e+02, -2.1000e+02, ..., -2.3400e+02,
  -2.8900e+02, -2.7300e+02],
 [-1.3500e+02, -2.3700e+02, -1.7900e+02, ..., -1.4400e+02,
  -1.9200e+02, -1.7900e+02]],

[[-1.7900e+02, -1.4300e+02, -1.1300e+02, ..., -1.2800e+02,
  -1.1800e+02, -9.9000e+01],
 [-2.0600e+02, -1.4800e+02, -1.9300e+02, ..., -2.5300e+02,
  -1.9200e+02, -1.2500e+02],
 [-1.5100e+02, -7.9000e+01, -1.4000e+02, ..., -1.5100e+02,
  -1.0700e+02, -5.7000e+01],
...,
 [ 4.7000e+01, -1.3900e+02, -5.9000e+01, ..., -2.9000e+01,
  -1.4000e+01, 7.0000e+00],
 [-1.7000e+01, -2.4000e+02, -1.7400e+02, ..., -1.9000e+01,
  -1.6000e+02, -9.3000e+01],
 [-4.1000e+01, -2.0100e+02, -1.5600e+02, ..., -1.0800e+02,
  -2.2700e+02, -8.9000e+01]]],

...,

[[[ 8.0000e+01, 1.0400e+02, 2.3000e+01, ..., 6.4000e+01,
    4.3000e+01, -3.3000e+01],
  [-2.7000e+01, -3.0000e+00, -9.7000e+01, ..., -1.2800e+02,
    -1.1600e+02, -7.9000e+01],
  [-3.3000e+01, 2.0000e+00, -1.0700e+02, ..., -2.0100e+02,
    -1.1500e+02, -8.2000e+01],
...,

```

```

[-1.8100e+02, 3.2000e+01, 3.8000e+01, ..., -1.3000e+01,
 2.0000e+01, -4.8000e+01],
[-2.3700e+02, -1.0100e+02, -3.8000e+01, ..., -1.7600e+02,
-4.2000e+01, -5.7000e+01],
[-2.4800e+02, -2.4200e+02, -2.3200e+02, ..., -8.7000e+01,
-6.0000e+01, -3.9000e+01]],

[[ 1.1800e+02, 1.6000e+01, 3.0000e+01, ..., 1.1400e+02,
 1.8600e+02, -2.0900e+02],
 [ 7.0000e+00, -1.0600e+02, -3.8000e+01, ..., -8.1000e+01,
 4.6000e+01, -2.9100e+02],
 [ 8.3000e+01, -6.6000e+01, -1.9000e+01, ..., -9.0000e+00,
-6.8000e+01, -2.4400e+02],
...,
 [-9.4000e+01, -9.8000e+01, 7.1000e+01, ..., 1.8000e+01,
-6.3000e+01, -1.0400e+02],
 [-1.4600e+02, -2.0100e+02, 1.9000e+01, ..., -1.3000e+01,
-5.2000e+01, -1.4100e+02],
 [-1.0900e+02, -1.8800e+02, 2.7000e+01, ..., -4.3000e+01,
 1.6600e+02, -1.3300e+02]],

[[-1.5800e+02, -5.3000e+01, -6.8000e+01, ..., 3.9000e+01,
-9.6000e+01, 7.8000e+01],
 [-1.3500e+02, -3.4000e+01, -8.3000e+01, ..., -1.2700e+02,
-1.1600e+02, -1.0000e+02],
 [-1.7600e+02, -4.9000e+01, -1.3000e+02, ..., -9.6000e+01,
-7.0000e+01, -2.2000e+01],
...,
 [-5.9000e+01, -1.6100e+02, -3.0400e+02, ..., -2.7900e+02,
-1.8700e+02, -7.0000e+00],
 [-9.2000e+01, -1.2500e+02, -3.1300e+02, ..., 4.1000e+01,
-3.2200e+02, -5.7000e+01],
 [-7.0000e+00, 2.9000e+01, -1.8000e+01, ..., -1.3300e+02,
-1.5600e+02, -2.2000e+01]],

...,

[[ 1.8800e+02, 4.6300e+02, 3.4200e+02, ..., 3.0800e+02,
 3.1600e+02, 3.6300e+02],
 [-9.4000e+01, 1.4600e+02, 1.7900e+02, ..., -9.0000e+00,
 5.8600e+02, 4.4600e+02],
 [-1.2000e+01, 3.0500e+02, 3.2700e+02, ..., 6.8000e+01,
 6.2400e+02, 4.9900e+02],
...,
 [ 8.6000e+01, 6.0000e+01, 1.7300e+02, ..., -4.6000e+01,
 4.2400e+02, 1.5800e+02],
 [ 9.0000e+01, 5.8000e+01, 8.1000e+01, ..., 9.9000e+01,
 1.0900e+02, 2.0400e+02],

```

```

[-2.5000e+01, -6.6000e+01, -6.2000e+01, ..., 9.8000e+01,
 7.5000e+01, 7.3000e+01]],

[[-3.3900e+02, -3.7900e+02, -3.3300e+02, ..., -6.0300e+02,
 -2.7000e+02, -5.5000e+01],
 [-4.1800e+02, -4.5000e+02, -4.5100e+02, ..., -8.3000e+02,
 -3.9900e+02, -6.2000e+01],
 [-3.2000e+02, -3.1200e+02, -3.1700e+02, ..., -6.3300e+02,
 -3.1600e+02, -5.8000e+01],
 ...,
 [-1.5400e+02, -2.1900e+02, -3.4900e+02, ..., -3.9200e+02,
 -4.0800e+02, -1.5600e+02],
 [-1.8800e+02, -2.1700e+02, -3.3500e+02, ..., -3.6300e+02,
 -3.0400e+02, -1.5800e+02],
 [-1.5000e+02, -1.3400e+02, -1.5300e+02, ..., -2.7000e+02,
 -1.9800e+02, -1.0100e+02]],

[[-1.5800e+02, -1.2400e+02, -1.3600e+02, ..., 4.0000e+01,
 -7.8000e+01, 4.7000e+01],
 [-1.8600e+02, -3.0400e+02, -2.5300e+02, ..., -1.4000e+02,
 -1.8700e+02, -9.5000e+01],
 [-1.4600e+02, -2.5100e+02, -2.5200e+02, ..., -1.9400e+02,
 -1.6100e+02, -9.2000e+01],
 ...,
 [-1.4100e+02, -2.9200e+02, -2.7200e+02, ..., -2.8300e+02,
 -1.2100e+02, -6.4000e+01],
 [-4.4000e+01, -1.2600e+02, -1.4300e+02, ..., -1.2900e+02,
 -2.6500e+02, -8.1000e+01],
 [-4.8000e+01, -1.5700e+02, -2.1700e+02, ..., -8.4000e+01,
 -1.8200e+02, -6.4000e+01]]],

[[[ 1.1300e+02, 7.4000e+01, 5.5000e+01, ..., 5.5000e+01,
 5.8000e+01, -1.3000e+01],
 [ 1.6200e+02, 1.6200e+02, 1.5500e+02, ..., 1.4400e+02,
 1.3000e+02, 4.0000e+00],
 [ 1.8700e+02, 1.9000e+02, 1.8400e+02, ..., 1.4700e+02,
 1.1300e+02, -2.4000e+01],
 ...,
 [ 9.9000e+01, 7.2000e+01, 7.9000e+01, ..., -7.3000e+01,
 -1.0600e+02, -5.5000e+01],
 [ 1.1200e+02, 8.5000e+01, 9.5000e+01, ..., -8.3000e+01,
 -8.2000e+01, -1.0300e+02],
 [ 8.0000e+00, -3.0000e+00, 7.0000e+00, ..., -3.2000e+01,
 -4.4000e+01, -3.8000e+01]]],

[[-1.2300e+02, -2.4900e+02, -2.2600e+02, ..., -2.3600e+02,
 -2.6200e+02, -1.8100e+02],

```

```

[-9.0000e+00, -1.8100e+02, -9.8000e+01, ..., -1.0000e+02,
 -9.9000e+01, -1.3100e+02],
[-7.0000e+00, -2.0500e+02, -6.6000e+01, ..., -1.0600e+02,
 -6.9000e+01, -1.4300e+02],
...,
[ 5.0000e+00, -1.4800e+02, -8.3000e+01, ..., -9.2000e+01,
 -1.1700e+02, -1.9000e+02],
[ 5.0000e+00, -1.0900e+02, -3.5000e+01, ..., 1.3000e+01,
 -9.7000e+01, -1.0600e+02],
[ 6.7000e+01, 4.4000e+01, 8.7000e+01, ..., 1.2300e+02,
 1.3900e+02, -5.3000e+01]],

[[-2.8800e+02, -1.7400e+02, -1.4700e+02, ..., -1.3700e+02,
 -1.9100e+02, -8.9000e+01],
 [-2.2700e+02, -5.8000e+01, -4.8000e+01, ..., -1.9000e+01,
 -9.3000e+01, 5.2000e+01],
 [-1.8900e+02, -2.1000e+01, -6.0000e+00, ..., -1.8120e-05,
 -8.3000e+01, 4.2000e+01],
...,
 [-9.4000e+01, -3.2000e+01, -5.6000e+01, ..., -1.1100e+02,
 -6.0000e+01, -5.9000e+01],
 [-1.1700e+02, -7.5000e+01, -6.2000e+01, ..., -3.7000e+01,
 -6.0000e+01, 1.8000e+01],
 [ 9.8000e+01, 1.5200e+02, 1.6400e+02, ..., 4.0000e+00,
 -2.3000e+01, 7.8000e+01]],

...,

[[ 5.8000e+01, 2.5100e+02, 1.9800e+02, ..., 1.9900e+02,
 1.7600e+02, 6.0000e+00],
 [ 1.1600e+02, 3.0000e+02, 2.4000e+02, ..., 2.3900e+02,
 2.2300e+02, 1.3400e+02],
 [ 1.3500e+02, 2.8100e+02, 1.9500e+02, ..., 2.2300e+02,
 2.0400e+02, 9.2000e+01],
...,
 [ 1.0000e+02, 2.3000e+02, 1.9500e+02, ..., 1.1400e+02,
 2.7200e+02, 1.1000e+02],
 [ 1.5500e+02, 2.5900e+02, 2.0700e+02, ..., 1.8100e+02,
 3.2100e+02, 9.1000e+01],
 [ 8.5000e+01, 1.4800e+02, 1.1600e+02, ..., 9.0000e+01,
 1.5000e+02, 9.8000e+01]],

[[-1.2500e+02, -6.3000e+01, -4.4000e+01, ..., -3.7000e+01,
 -1.3000e+01, 7.3000e+01],
 [-2.9800e+02, -2.3800e+02, -2.1700e+02, ..., -2.1000e+02,
 -1.8600e+02, 9.9997e-01],
 [-2.6600e+02, -2.4300e+02, -2.1800e+02, ..., -2.0200e+02,
 -1.8300e+02, -6.0000e+00],

```

```

...,
[-2.8200e+02, -2.4900e+02, -2.1900e+02, ..., -2.0900e+02,
-1.8900e+02, -3.3000e+01],
[-2.6200e+02, -2.2100e+02, -2.1300e+02, ..., -2.1100e+02,
-1.7700e+02, -5.0000e+00],
[-2.9300e+02, -3.0400e+02, -2.9600e+02, ..., -2.4500e+02,
-2.3100e+02, -8.4000e+01]],

[[-2.0400e+02, -1.7100e+02, -1.8100e+02, ..., -1.8300e+02,
-1.5700e+02, -9.9000e+01],
[-2.0200e+02, -2.0500e+02, -2.2900e+02, ..., -2.1500e+02,
-1.9700e+02, -8.1000e+01],
[-1.7400e+02, -1.3700e+02, -1.6800e+02, ..., -1.2300e+02,
-1.2800e+02, -3.4000e+01],

...,
[-1.0400e+02, -9.6000e+01, -1.2700e+02, ..., -9.6000e+01,
-6.6000e+01, -3.3000e+01],
[-1.0800e+02, -1.4600e+02, -1.5900e+02, ..., -1.0900e+02,
-1.3900e+02, -7.4000e+01],
[-5.6000e+01, -8.2000e+01, -9.8000e+01, ..., -7.6000e+01,
-1.1700e+02, -3.0000e+00]]],

[[[-4.5000e+01, -1.1000e+01, 1.5000e+01, ..., 7.6000e+01,
-3.6000e+01, -1.0900e+02],
[-1.1900e+02, -1.4100e+02, -8.8000e+01, ..., -2.0000e+00,
-1.2200e+02, -1.5100e+02],
[-1.5200e+02, -1.0300e+02, -1.0100e+02, ..., 2.7000e+01,
-7.1000e+01, -1.1800e+02],

...,
[-1.3200e+02, -6.9000e+01, -4.5000e+01, ..., 4.2000e+01,
-5.9000e+01, -1.2300e+02],
[-8.6000e+01, -4.5000e+01, -1.0200e+02, ..., 3.1000e+01,
-7.2000e+01, -1.4600e+02],
[-1.3100e+02, -1.5700e+02, -1.5900e+02, ..., 9.6000e+01,
9.0000e+00, -3.3000e+01]],

[[-1.0000e+01, 1.1300e+02, 3.0000e+01, ..., 1.3900e+02,
2.3100e+02, -1.4800e+02],
[-7.3000e+01, 5.7000e+01, -1.0200e+02, ..., 3.8000e+01,
1.3000e+02, -3.6400e+02],
[4.5000e+01, 2.6000e+01, -2.5000e+01, ..., 8.5000e+01,
1.4400e+02, -3.0900e+02],

...,
[5.0000e+00, -1.8700e+02, 4.5000e+01, ..., 6.4000e+01,
1.6800e+02, -3.1100e+02],
[-2.5000e+01, -2.1100e+02, -8.7000e+01, ..., 1.0800e+02,
2.0000e+02, -3.0000e+02],

```

```

[-5.6000e+01, 7.0000e+00, -3.2000e+01, ..., 1.0400e+02,
 1.6000e+02, -3.0600e+02]],

[[ 1.5400e+02, 1.1000e+01, 8.0000e+00, ..., 1.4700e+02,
 1.8900e+02, 2.1500e+02],
 [-2.3000e+01, -3.9000e+01, -1.5400e+02, ..., -2.9000e+01,
 -5.9000e+01, -2.0000e+00],
 [ 6.7000e+01, -9.0000e+00, -2.6000e+01, ..., 4.6000e+01,
 1.1000e+01, 4.0000e+01],
 ...,
 [-3.9000e+01, -2.4000e+01, -1.6600e+02, ..., 4.8000e+01,
 -3.7000e+01, 3.9000e+01],
 [-1.1300e+02, -9.4000e+01, -3.9000e+01, ..., 1.5700e+02,
 5.0000e+01, 7.5000e+01],
 [ 5.2000e+01, 5.3000e+01, 1.5000e+02, ..., -1.7100e+02,
 -2.4800e+02, -1.1600e+02]],

...,

[[ 1.9800e+02, 7.0000e+00, 1.4800e+02, ..., -1.0000e+01,
 7.9000e+01, 5.2000e+01],
 [ 1.0500e+02, 2.4900e+02, 2.0500e+02, ..., 1.9900e+02,
 3.5700e+02, 1.0200e+02],
 [ 8.1000e+01, 2.5900e+02, 1.9300e+02, ..., 1.9000e+02,
 3.6100e+02, 1.4300e+02],
 ...,
 [ 3.4000e+01, 2.0100e+02, 2.5100e+02, ..., 2.0900e+02,
 3.5200e+02, 1.3900e+02],
 [ 9.1000e+01, 2.3800e+02, 2.0200e+02, ..., 2.1800e+02,
 3.6000e+02, 1.1900e+02],
 [-1.0600e+02, -6.1000e+01, 5.6000e+01, ..., 1.6900e+02,
 3.0700e+02, 8.7000e+01]],

[[-1.1700e+02, -1.5300e+02, -1.4100e+02, ..., -6.4000e+01,
 -1.6800e+02, -2.1500e+02],
 [-2.0500e+02, -2.5800e+02, -2.4700e+02, ..., -1.8100e+02,
 -2.8600e+02, -2.5900e+02],
 [-2.2000e+02, -2.8000e+02, -2.9800e+02, ..., -1.6300e+02,
 -2.2600e+02, -2.1600e+02],
 ...,
 [-3.9300e+02, -3.1700e+02, -3.2700e+02, ..., -1.9200e+02,
 -2.8100e+02, -2.2900e+02],
 [-3.5900e+02, -2.9800e+02, -2.5200e+02, ..., -2.4200e+02,
 -3.0600e+02, -2.5100e+02],
 [-2.7400e+02, -2.4800e+02, -2.5800e+02, ..., -1.3700e+02,
 -1.9300e+02, -1.5500e+02]],

[[ 1.4600e+02, -2.2000e+01, 1.8000e+01, ..., 9.4000e+01,

```

```

        1.2000e+01, 1.1700e+02],
[ 9.9999e-01, -1.2100e+02, -1.0600e+02, ..., -2.1935e-05,
 -9.1000e+01, -9.0000e+00],
[-2.9000e+01, -1.3400e+02, -1.3900e+02, ..., -2.5000e+01,
 -1.0700e+02, -2.0000e+01],
...,
[-7.1000e+01, -8.2000e+01, -9.9000e+01, ..., -1.8000e+01,
 -1.0500e+02, -1.1000e+01],
[ 2.0000e+00, -9.8000e+01, -1.3700e+02, ..., -1.1900e+02,
 -2.1000e+02, -6.7000e+01],
[-5.3000e+01, -1.7800e+02, -8.4000e+01, ..., -1.7900e+02,
 -2.2100e+02, -8.6000e+01]]], device='cuda:0',
grad_fn=<ConvolutionBackward0>)

```

```

[11]: conv_unquan = nn.Conv2d(16, 16, kernel_size=(3, 3), padding=(1, 1), bias=False)
conv_unquan.weight = torch.nn.Parameter(weight_q)
out = conv_unquan(x)

```

```

[12]: diff = abs(out - psum_recovered)
print("gap", diff)

```

```

gap tensor([[[[5.1659e-01, 6.7050e-01, 9.4139e-01, ..., 1.8837e-01,
 5.8331e-01, 2.4019e-01],
[1.1429e-01, 2.0802e-01, 3.8295e-01, ..., 6.7232e-01,
 2.7058e-01, 7.9369e-01],
[1.9863e-01, 3.1256e-02, 2.1388e-01, ..., 1.1955e+00,
 4.6978e-01, 5.2290e-01],
...,
[3.4516e-01, 6.7371e-01, 8.7989e-01, ..., 6.0625e-01,
 2.7849e-01, 5.2161e-01],
[4.2660e-01, 4.7936e-01, 1.2529e-01, ..., 2.2255e-01,
 4.5503e-01, 2.8423e+00],
[1.8825e-02, 4.2435e-01, 2.9205e-01, ..., 7.0882e-02,
 8.7108e-01, 9.2278e-01]],
[[[4.3692e-01, 2.9545e-01, 1.6597e-01, ..., 6.1315e-01,
 2.3375e-01, 4.9136e-01],
[9.9156e-01, 8.3958e-02, 4.3507e-01, ..., 3.2550e-01,
 3.4743e-01, 7.3152e-01],
[1.1248e+00, 2.6149e-02, 6.1545e-01, ..., 1.2539e+00,
 1.1430e+00, 4.0929e-01],
...,
[4.0891e-01, 1.4092e-01, 3.0194e-01, ..., 1.7048e-01,
 1.3846e+00, 4.6885e-01],
[6.2307e-01, 4.1691e-01, 5.9603e-01, ..., 7.8116e-03,
 1.4114e-01, 7.5591e-01],
[6.8830e-01, 3.2772e-01, 1.8181e-01, ..., 3.1025e-01,
 2.3153e+00, 4.3510e+00]],

```



```

[[6.5044e-01, 3.8426e-01, 7.0635e-01, ..., 5.4763e-01,
  1.5085e-01, 8.8686e-01],
 [6.1921e-02, 2.7636e-01, 7.0539e-01, ..., 1.4966e+00,
  7.3114e-01, 1.1154e+00],
 [5.9208e-01, 6.1310e-02, 3.9279e-01, ..., 1.9616e-01,
  1.4218e+00, 5.4240e-02],
 ...,
 [1.3114e+00, 5.4916e-02, 1.3638e+00, ..., 9.5369e-01,
  1.2015e+00, 3.4888e-01],
 [1.6831e-01, 5.8005e-01, 3.5946e-01, ..., 1.6365e+00,
  1.2923e+00, 4.4609e+00],
 [9.2791e-02, 3.5758e-01, 2.9470e-01, ..., 5.8231e-01,
  1.4531e+00, 2.5712e+00]],

...,

[[5.1051e-01, 7.3021e-01, 7.1130e-01, ..., 8.5436e-01,
  2.3287e-01, 2.9173e-01],
 [8.1345e-01, 1.5405e-01, 1.3020e+00, ..., 3.7302e-01,
  1.3013e+00, 5.2149e-01],
 [6.1609e-01, 3.8033e-01, 4.3506e-01, ..., 8.5455e-01,
  8.0384e-01, 2.0256e+00],
 ...,
 [2.2570e-01, 1.0249e-01, 4.5536e-01, ..., 7.8557e-01,
  1.8171e+00, 1.2723e-01],
 [9.2548e-01, 1.3273e-01, 6.9197e-01, ..., 7.0657e-01,
  2.7231e+00, 2.0390e+00],
 [1.4506e-01, 4.6022e-01, 8.6923e-01, ..., 5.1645e-02,
  1.6757e+00, 2.6752e+00]],

[[2.6193e-01, 4.4637e-01, 6.2078e-01, ..., 7.8300e-01,
  5.9817e-01, 1.7756e-01],
 [6.7313e-01, 3.2362e-01, 5.0590e-01, ..., 6.9812e-01,
  6.5816e-01, 9.0003e-01],
 [1.3038e+00, 5.3690e-01, 4.0259e-01, ..., 1.0052e+00,
  1.0588e+00, 1.1014e+00],
 ...,
 [6.8077e-01, 6.3858e-01, 4.2283e-01, ..., 1.3990e-01,
  5.8650e-01, 7.0901e-02],
 [2.6490e-01, 7.3754e-01, 7.1752e-01, ..., 4.8044e-01,
  1.3717e+00, 3.2455e-01],
 [5.0750e-01, 7.3895e-01, 1.0732e-01, ..., 3.9750e-01,
  1.3505e+00, 1.1915e+00]],

[[6.5624e-02, 9.2188e-01, 1.3843e+00, ..., 4.1897e-01,
  2.0055e-01, 1.1315e-01],
 [8.8878e-01, 4.7188e-01, 2.4605e-01, ..., 3.1597e-02,

```

```

1.0266e+00, 2.1669e-01],
[1.2950e-01, 8.9456e-01, 1.6690e+00, ..., 3.7082e-01,
8.5307e-01, 8.2910e-02],
...,
[1.0402e+00, 1.4301e-01, 3.3263e-01, ..., 6.3674e-01,
5.8925e-01, 5.2960e-02],
[2.6188e-01, 5.1748e-01, 7.9167e-01, ..., 7.6774e-01,
2.3503e+00, 1.0842e+00],
[3.1382e-01, 2.3601e-01, 2.2143e-01, ..., 6.8289e-01,
2.4043e+00, 2.5512e+00]]],

[[[7.1422e-01, 1.0893e+00, 9.1012e-01, ..., 9.5333e-01,
2.9235e-01, 7.7260e-01],
[1.4352e+00, 1.4003e+00, 8.3932e-01, ..., 3.2938e-01,
1.5351e+00, 1.2381e+00],
[1.0823e+00, 1.3482e+00, 1.7006e+00, ..., 9.7087e-01,
7.1628e-01, 4.3097e-01],
...,
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[3.8966e-01, 5.1220e-01, 3.5895e-01, ..., 4.2475e-01,
 2.0123e+00, 4.0704e+00],
[5.3417e-01, 3.1895e-01, 5.2775e-01, ..., 1.2519e+00,
 4.1218e-01, 1.4692e+00],
...,

```

```

[6.3243e-01, 5.3181e-01, 8.6811e-01, ..., 1.0824e+00,
 1.9368e-01, 1.3300e+00],
[9.1411e-01, 8.4782e-01, 3.0086e-01, ..., 3.7915e-01,
 5.3559e-01, 9.4519e-02],
[8.4466e-02, 5.6615e-01, 3.8145e-01, ..., 6.8351e-01,
 3.4610e+00, 2.3065e+00]],

[[3.5540e-01, 1.8324e-01, 8.0090e-01, ..., 7.2805e-01,
 7.9644e-01, 1.5628e+00],
[2.9950e-02, 4.1141e-01, 1.2257e+00, ..., 1.0380e+00,
 8.9306e-01, 2.1895e+00],
[9.1862e-01, 5.2428e-01, 8.6294e-02, ..., 5.2746e-01,
 6.7423e-01, 1.7111e-01],
...,
[3.6799e-01, 1.0288e+00, 1.3892e-01, ..., 3.1431e-01,
 1.1667e+00, 6.9645e-01],
[4.7767e-01, 8.3368e-02, 2.4920e-01, ..., 1.7948e-01,
 5.5734e-01, 3.3789e+00],
[1.7721e-01, 3.0067e-01, 4.6431e-01, ..., 3.0685e-01,
 6.8080e-01, 3.3923e+00]],

...,

[[1.9621e-01, 3.2009e-01, 1.1132e+00, ..., 5.7941e-01,
 4.2009e-01, 2.3432e+00],
[3.9641e-01, 3.4582e-01, 4.6390e-01, ..., 1.9269e+00,
 1.0147e+00, 4.4679e+00],
[2.2361e-01, 8.7543e-01, 9.0261e-01, ..., 2.1440e+00,
 2.8856e-02, 6.6558e-01],
...,
[3.2711e-01, 1.1300e+00, 2.5863e-01, ..., 9.7422e-01,
 5.9200e-01, 2.1076e-02],
[7.9700e-01, 1.0287e+00, 8.3844e-01, ..., 4.4240e-01,
 4.8548e+00, 1.6951e+00],
[9.7963e-01, 6.0355e-01, 1.0041e+00, ..., 4.2072e-02,
 1.8367e+00, 3.5230e+00]],

[[2.4897e-01, 1.4671e+00, 4.1045e-01, ..., 4.7430e-01,
 1.5965e+00, 2.0864e+00],
[2.5631e-02, 1.0900e+00, 7.8481e-01, ..., 9.2041e-01,
 4.9843e-01, 1.1175e-01],
[1.2807e+00, 4.2488e-02, 1.6632e+00, ..., 3.9236e-01,
 5.7086e-01, 1.9590e+00],
...,
[1.2601e+00, 5.3115e-01, 1.3203e+00, ..., 8.1354e-02,
 1.0595e+00, 1.4882e+00],
[1.4702e+00, 1.2530e+00, 4.3078e-01, ..., 1.5914e-01,
 5.0841e-01, 4.6161e-01],

```

```
[9.3919e-01, 7.8232e-01, 3.7109e-02, ..., 4.9173e-01,
 1.8802e+00, 2.4092e+00]],

[[2.5532e-01, 3.7306e-01, 2.8211e-01, ..., 7.1081e-02,
 2.7513e+00, 2.7442e+00],
 [2.3849e-01, 3.7920e-01, 1.5709e-01, ..., 8.5134e-01,
 7.5342e-01, 1.9515e+00],
 [8.3821e-01, 8.4165e-01, 6.9706e-02, ..., 8.6512e-01,
 6.0488e-02, 1.7450e-01],
 ...,
 [1.6983e-01, 1.5249e-01, 5.3876e-01, ..., 1.5062e-01,
 2.1238e-01, 7.1967e-01],
 [3.1201e-01, 5.1463e-01, 4.5135e-01, ..., 2.2796e-02,
 1.1476e+00, 5.2258e-01],
 [4.9031e-01, 3.9788e-01, 2.1007e-01, ..., 2.8001e-01,
 2.3411e+00, 2.8592e+00]]], device='cuda:0', grad_fn=<AbsBackward0>)
```

```
[13]: diff.mean()
```

```
[13]: tensor(0.7316, device='cuda:0', grad_fn=<MeanBackward0>)
```

```
[16]: resnet20_2bit_quan = resnet20_quant(w_quan_bits=2).cuda()
pre_best_prec = 0
quan_model_name = "2bit_quan_resnet"
```

```
[ ]: lr = 7e-2
weight_decay = 1e-4
epochs = 100
# pre_best_prec = 85.470

criterion = nn.CrossEntropyLoss().cuda()

res20_2bit_optimizer = torch.optim.SGD(resnet20_2bit_quan.parameters(), lr=lr,
    ↪momentum=0.9, weight_decay=weight_decay)
pre_best_prec = helper.train_model(resnet20_2bit_quan,
    ↪model_name=quan_model_name, optimizer=res20_2bit_optimizer,
    ↪trainloader=trainloader, testloader=testloader, criterion=criterion,
    ↪epochs=epochs, pre_best_prec=pre_best_prec)
```

```
[17]: helper.test_model(model=resnet20_2bit_quan, model_name=quan_model_name,
    ↪testloader=testloader)
```

```
Test: [0/79]    Time 0.233 (0.233)    Loss 0.3729 (0.3729)    Prec 87.500%
(87.500%)
* Prec 83.960%
```

```
[ ]:
```