Infusing domain knowledge in Al-based "black box" models for better explainability with application in bankruptcy prediction

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ABSTRACT

Although "black box" models such as Artificial Neural Networks, Support Vector Machines, and Ensemble Approaches show superior performance in many disciplines, sensitive disciplines (e.g. finance and healthcare) question adoption of these models due to their lack of interpretability and explainability-the extent to which the internal working mechanisms of an AI system can be explained in human terms. New and proposed legislation threaten future adoption of "black box" models. The European Union's recent rule of "right of explanation" requires banks to give consumers explanations behind an algorithmic decision. In the U.S., the proposed "Algorithmic Accountability Act", would require companies to assess their machine learning systems for bias and discrimination and take corrective measures. Top Bankruptcy Prediction Models are A.I.-based, and although explainable artificial intelligence is an emerging field of research, infusing domain knowledge may provide insight and better explainability. In this work, we demonstrate a way to collect and infuse domain knowledge into a "black box" model for mortgage default prediction. Our understanding from the experiments reveals that infused domain knowledge makes the output from the black box model more interpretable and explainable.

CCS CONCEPTS

• Computing methodologies → Inductive logic learning.

KEYWORDS

Artificial Intelligence, explainability, interpretability, bankruptcy prediction model, domain knowledge

ACM Reference Format:

Sheikh Rabiul Islam, William Eberle, Sid C. Bundy, and Sheikh K. Ghafoor. . Infusing domain knowledge in AI-based "black box" models for better explainability with application in bankruptcy prediction. In KDD '19: 2nd KDD Workshop on Anomaly Detection in Finance, August 04–08, 2019, Anchorage, Alaska - USA. , 9 pages.

1 INTRODUCTION

Over the past few years, the field of Artificial Intelligence (AI) has gained interest in many practical application areas. Some of the more notable models are Artificial Neural Networks (ANN), Genetic

Algorithms (GA), Support Vector Machines (SVM), and Ensemble Approaches. Sometimes these models are called "black box" models. Although the high complexity of the models' non-linear functions come with good predictive power for black box models, they are limited by their *explanation and interpretation* capabilities. Recent advances in machine learning and artificial intelligence gave rise to these complex and powerful models being adopted in sophisticated fields (e.g. medical, finance, and cyber-security).

In March 2019, the Department of Housing and Urban Development accused Facebook Inc. violated the Fair Housing Act with their algorithm that restricted views of housing-related advertisements, the complaint saying that Facebook Inc.'s "mechanisms function just like an advertiser who intentionally targets or excludes users based on their protected class." The agency is also investigating the algorithms used in advertising systems for Alphabet Inc. unit Google and Twitter Inc.

To fight the unethical use of AI and biases in decision making, governments are trying to introduce and enforce new laws and regulations. The European Union implemented the rule of "right of explanation", where a user can ask for an explanation of an algorithmic decision [34]. In addition, in April 2019, U.S. Senators Cory Booker and Ron Wyden, along with Representative Yvette D. Clarke, introduced the "Algorithmic Accountability Act" [78] which would require companies to assess their machine learning systems for bias and discrimination and take corrective measures. Should the bill pass, the US Federal Trade Commission, which is in charge of consumer protection and antitrust regulation, would create regulations to conduct impact assessments of highly sensitive automated decision systems.

Black box models are frequently used in the financial area, particularly towards loan default and bankruptcy prediction. The focus of bankruptcy prediction is to estimate the probability that the customer will be in default or bankrupt in the near future. Unanticipated bankruptcies impact shareholders, partners, society, and the overall economic condition of the country [7]. According to literature reviews by Alaka et al. [7] and Bellovary et al. [14], six out of the top eight Bankruptcy Prediction Models (BPM) are Artificial Intelligence (AI) based. The reviews suggest that BPMs based on "black box" models such as ANN, GA, and SVM outperform all other models due to their capability of learning any non-linear function. Recently another black box model, ensemble approaches,

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where multiple models are combined for better results by correcting each other's error, shows promising performances. However, these "black box" models lack explainability (i.e., explaining the internal working mechanism to humans) and interpretability (i.e., a sense of what's happening within the model), which raises ethical issues for domains like finance. A decision in the financial domain (e.g., credit approval, default prediction) needs to be more than a number— it needs to explain the reason behind the decision that makes sense to a human. It also needs to be free from biases against protected classes. Furthermore, when there are many explanatory variables, and some explanatory variables are complex, this further complicates the explainability.

Research in Explainable Artificial Intelligence is an emerging field, seeing a resurgence after three decades of slowed progress since the work of Chandrasekaran et al. [21], Swartout et al. [73], and Buchanan et al. [72]. The classical learning paradigm Explanation-Based Learning (EBL), introduced in the early '80s, can also be regarded as a precursor of explainability. EBL involves learning a problem-solving technique by observing and analyzing solutions to a specific problem [23, 58, 59]. In their work on Explainable Artificial Intelligence (XAI), Miller et al. [57] argue that most of the work on XAI focuses on the researcher's intuition of what constitutes a good explanation. However, there exists a vast area of research in philosophy, psychology, and cognitive science on how people generate, select, evaluate, and represent explanations and associated cognitive biases and social expectations towards the explanation process. Therefore, the author emphasizes that, the research on explainable AI should incorporate studies from these different domains.

According to Lipton et al. [52] and [31], interpretability has three different notions:

- interpretability in pre-modeling: finding and using simple, summarized, and relevant set of features from the domain;
- (2) interpretability in modeling: generating explanation along with the prediction to improve transparency; and
- (3) interpretability in post modeling (a.k.a. post-hoc): understanding the dynamics between input and predicted output for an already trained/tested model.

Unfortunately, the post-hoc notion of interpretability is not purely transparent and can be misleading, as it provides an explanation after the decision has been made. The algorithm can be optimized to placate subjective demand, and the explanation from it also can be misleading though it seems plausible [31, 52]. Furthermore, from the literature review, we find that interpretability in pre-modeling is under-focused. Therefore, we particularly focus on the explainability of black box models *using domain knowledge* which falls into interpretability in the pre-modeling stage. In this work, we take mortgage default prediction as the context for our experiments.

In our proposed approach, we replace hard to interpret features of a model with easily interpretable features (induced from domain knowledge) which allows the decision to be expressed in terms of an interpretable and concise set of features. We use a frequent pattern mining algorithm to find frequent feature sets used in different bankruptcy and consumer default literature. Later, we relate the frequent feature set with the popular financial concept of credit to come up with a generalized feature set for the experiments, which

ultimately allows us to infuse domain knowledge to increase the explainability and interpretability of "black box" models. To asses credit risk by human experts, the 5C's of credit is commonly used to analyze key factors: character (reputation of the borrower/firm), capital (leverage), capacity (volatility of the borrower's earnings), collateral (pledged asset) and cycle (macroeconomic) conditions [11, 63]. The domain knowledge infused feature set gives us a generalized frequent feature set which is used for our experiments for better explainability.

In summary, our contributions in this work are as follows: (1) we demonstrate a method for the collection and use of domain knowledge from the literature; (2) we introduce a way to bring popular concepts (e.g., the 5 C's of credit) from literature to aid in interpretability and explainability; and (3) our experimental results show that infusing domain knowledge into "black box" models can make them better explainable with little or no compromise in performance.

We start with a background of related work (Section 2) followed by a description of our proposed approach and an overview of the dataset (Section 3) used in this work. In Section 4, we describe our experiments, followed by Section 5 which contains results and a discussion of the experiments. We conclude with limitations and future work in section 6.

2 BACKGROUND

Early research in explainable AI started with the preliminary work of Chandrasekaran et al. [21], Swartout et al. [73], and Buchanan et al. [72]. Recent advancements in AI, successful adoption in different applications, and awareness of ethical and bias issues necessitates recent research in Explainable Artificial Intelligence (XAI). For instance, in September 2018 the DARPA division of the Department of Defense (DoD) announced spending \$2 billion on its XAI program. They are developing a toolkit library consisting of machine learning and human-computer interface software for developing explainable AI systems that will be available for military and commercial use [75]. The agency funds over 20 AI programs including: (1) Common Ground Learning and Explanation (COGLE) to establish common ground between the ways human minds and machines work and (2) Causal Models to Explain Learning (CAMEL) to simplify the explanations of how those machines work. The ultimate goal is to produce machines that can tell its human operators why it arrives at the conclusions it does.

Yang et al. [79], propose a method based on "Bayesian Teaching", where a subset of an example in used to train the model instead of the whole dataset. The subset of the example is chosen by domain experts that are most relevant to the problem. However, for this purpose, choosing the right subset of examples in the real world is challenging.

In sentiment analysis, the rationale for a prediction is important for understanding decisions. Lei et al. [50] propose an approach that generates the rationale for a prediction. They demonstrate the approach with sentiment analysis from the text where a subset of text is selected as the rationale for the prediction. In addition, the selected text is concise and sufficient enough to act as a substitute for the original text, still capable of the correct prediction. Although

their approach outperforms available attention-based models, it is limited to only text analysis.

Making a prediction that can be trusted is another challenge. Ribeiro et al. [62] propose a novel explanation technique capable of explaining the prediction of any classifier in an interpretable and faithful manner by learning an interpretable model locally around the prediction. Their concern is on two issues: (1) whether the user should trust the prediction of the model and act on that, and (2) whether the user should trust a model to behave reasonably well when deployed. In addition, they involve human judgment in their experiment to decide whether to trust the model or not.

Kim et al. [47] propose a an approach that provides an interpretation of the neural network's internal state in a human-friendly manner. Their approach Testing with CAV (TCAV) quantifies the prediction's sensitivity to a high dimensional concept. For example, a user-defined set of examples that defines the concept 'striped', TCAV can quantify the influence of 'striped' in the prediction of 'zebra' as a single number. Although this work is focused on the image classification system, the authors suggest that their work could be utilized to work with other types of data such as audio, video, sequences, etc. Other than for the use in interpretation, their approach can also be used in identifying adversarial examples for neural nets. Furthermore, for better explainability and validation of results from neural network based black box models, Horel et al. [39] develop a statistical test to assess the statistical significance of the features/variables in a single layer feed-forward neural network. In addition, the test statistics also enable one to rank the variables based on their influence on the prediction. However, their approach is limited to only a single layer feed-forward neural network and requires a very large amount of samples to fit the data in the asymptotic distribution.

Lundberg et al. [56] propose a unified approach called "SHAP" which unifies seven previous approaches: LIME [62], DeepLIFT [64], Tree Interpreter [10], QII [22], Shapley sampling values [71], Shapley regression values [51], and Layer-wise relevance propagation [13] to make the explanation of prediction for any machine learning model. Both LIME [62] and SHAP [56] use a simplified input mapping, mapping the original input to a simplified set of input. However, none of the models incorporate domain knowledge. The following approach infuses domain knowledge into the experiment and works as a substitute for original complex features in order to generate a prediction which is explainable by itself.

3 METHODOLOGY

The proposed approach consists of two components: a feature *generalizer*, which gives a generalized frequent feature set with the help of domain knowledge, and an *evaluator*, that produces and compares the results using the generalized feature set from the original feature set.

3.1 Feature Generalizer

First, the frequent feature miner takes multiple different sets of features used in different mortgage default prediction literature (see section 3.4) to discover the most frequent set of features (i.e., a frequent combination of features used in different literature) using a popular and classic frequent pattern mining algorithm called

Apriori (Agrawal et al. [6]). In Figure 1, the input to the algorithm is: $X_1, X_2, ..., X_n \in X$ where X is the universal set of features used in mortgage default prediction literature. The output is some frequent set of features with a specified support and maximum count of features in the set: X_{f1} , X_{f2} ,.... $X_m \in X$ where X is the universal set of features as before, but here *m* is much smaller than *n*. Finally, the frequent set of features is fed into the domain knowledge mapper. In the domain knowledge mapper, a popular, easy to understand and interpret domain concept is introduced and mapped with the frequent feature set. For our case, we introduce the 5 Cs of credit which refers to capital, character, cash flow, conditions, and collateral. Based on the mapping, the domain knowledge mapper outputs a generalized frequent feature set infused with domain knowledge. This generalized frequent feature set is free of complex and hard to interpret features such as actualLossCalculation, which actually consists of multiple other features: Actual Loss = (Default UPB -Net Sale Proceeds) + Delinquent Accrued Interest - Expenses - MI Recoveries - Non MI Recoveries).

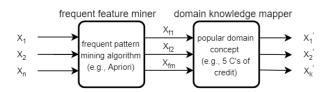


Figure 1: Feature generalizer

3.2 Evaluator

The task of the evaluator (Figure 2) is to execute and compare the performance of two experiments: one using original features (X) of the dataset and the other one using the generalized frequent feature sets (X'). If the difference is within an allowable threshold, then the output from the latter experiment is deemed as final output, and the output is explained using the contribution from each of generalized, and more explainable and interpretable, frequent features.

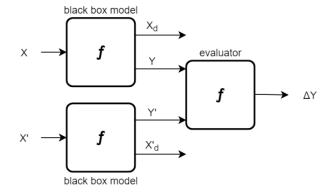


Figure 2: Evaluator

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3.3 Algorithms

We use six different algorithms: one is for frequent pattern mining, and the remaining five are supervised "black box" models for predicting bankruptcy/default.

3.3.1 Apriori. The Apriori algorithm which was proposed by Agrawal et al. [6], a classical algorithm in data mining for finding frequent patterns. For our case, when a set of features or explanatory variables found in a paper meets a user-specified support threshold, then that set of features can be treated as frequent feature sets. The support for a set of features X in a paper p_i is defined as follows: Support (X) = (number of paper in which all features of X appear) / (total number of paper). For example, if the support threshold is set to .5 (i.e., 50%), then the feature set {LTV, creditScore, interestRate, delinquencyStatus} is called a frequent feature set if and only if this set of features is found together at least 50% of times among all the papers. Here is an intuition of the working mechanism of the Apriori algorithm. The Apriori algorithm iteratively finds frequent feature sets of a length starting from 1 to k, where k is the maximum number of features in any frequent feature set. The frequent feature sets must meet the minimum support threshold of the algorithm. In addition, a subset of features from the frequent feature set must also be a frequent feature. For example, if {LTV, creditScore, interestRate, delinquencyStatus} is a frequent feature set, then any of the features or any combination of features (e.g., {LTV}, , {LTV, creditScore}) within this feature set is also a frequent feature set. In Section 4, we will clarify this more.

3.3.2 Artificial Neural Network (ANN). An Artificial Neural Network is a non-linear model, capable of mimicking human brain functions. It consists of an input layer, multiple hidden layers, and the output layer. Each layer consists of multiple neurons that help to learn the complex pattern, each subsequent layer learns more abstract concepts before it finally merges into the output layer. ANN was first used in 1994 by Wilson and Sharda [76] for bankruptcy prediction. In terms of different performance metrics, given enough data, ANN performs best for many problems due to its capability of learning any non-linear function.

3.3.3 Support Vector Machine (SVM). The Support Vector Machine (SVM) was first introduced by Boser, Guyon, and Vapnik [17] and has been used for many supervised classification tasks. The model learns an optimal hyperplane that separates instances of different classes using a highly non-linear mapping of input vectors in high dimensional feature space [38]. SVM is listed as one of the top non-linear algorithms for bankruptcy prediction in different literature surveys [7, 14]. When the number of samples is too high (i.e., millions) then it is very costly in terms of computation time. In that case, a non-linear algorithm like ANN can be a better choice as an ANN usually works well with large datasets.

3.3.4 Random Forest (RF). A Random Forest is a tree-based ensemble technique developed by Breiman et al. [19] for the supervised classification task. In RF, many trees are generated from the bootstrapped subsamples (i.e., random sample drawn with replacement) of the training data. In each tree, the splitting attribute is chosen from a smaller random subset of attributes of that tree (i.e., the chosen split attribute that is the best among that random subset).

This randomness helps to make trees less correlated as correlated trees makes the same kinds of prediction errors and can overfit the model. This results in a forest of trees being generated, and the output from all the trees are averaged for the final prediction. This averaging helps to reduce the variance from the model. Furthermore, RF can work in a parallel computing environment as trees can be grown independently. According to [27], RF has been used in different credit scoring and customer attrition applications.

3.3.5 Extra Trees (ET). Extremely Randomized Trees or Extra Trees (ET) is also a tree-based ensemble technique like RF and share a similar concept with RF. The only difference is in the process of splitting attribute selection and determining the threshold (cutoff) value, both are chosen in extremely random fashion [44]. As in RF, a random subset of features are taken into consideration for the split selection but instead of choosing the most discriminative cut off threshold, ET cut off thresholds are set to random values. Thus, the best of these randomly chosen values is set as the threshold for the splitting rule [2]. As a result of multiple trees, the variance is reduced, compared to Decision Trees, however bias is introduced, as a subset of the whole feature set is chosen for each tree. The ET which was proposed by Geurts et al.[32], has continued its success by achieving the state of the art performance in some anomaly/intrusion detection research [42–44].

3.3.6 Gradient Boosting (GB). Friedman et al. [30], generalized Adaboost to a Gradient Boosting algorithm that allows a variety of loss function. Here the shortcoming of weak learners is identified using the gradient, while in AdaBoost it is done through highly weighted data points. Gradient Boosting (GB) is a classifier/regression model in the form of an ensemble of weak prediction models, such as Decision Trees which are fitted with data initially. It also works sequentially like the AdaBoost algorithm, in that each subsequent model tries to minimize the loss function (i.e., Mean Squared Error) by paying special focus on instances that were hard to get right in previous steps.

3.4 Data

We use two sources of data in this work:

- (1) Explanatory variables dataset: We analyzed the following 33 research papers related to mortgage default prediction: [8, 9, 12, 15, 16, 18, 20, 24–29, 33, 35–38, 45, 46, 48, 49, 53, 54, 60, 65–70, 74, 77]. We collected the explanatory variables used in each of these papers. We made the dataset available to the research community at here [40]. Table 1 lists the features that appear four or more times in the literature.
- (2) Freddie Mac single-family loan-level dataset: The Freddie Mac dataset [4] is the most frequently used dataset in the 33 previously mentioned research papers. It is also a publicly available dataset. For ensuring transparency, supporting the risk-sharing initiative, and building more accurate credit performance models, Freddie Mac, a government-sponsored enterprise, is making available loan-level credit performance data on fixed-rate mortgages that the company purchased or guaranteed. This is the source of data for the supervised algorithms used in this work. The dataset is not directly labeled with whether accounts are default or non-default.

We follow the same data labeling technique used by [16] on this dataset, where an account is treated as default when the feature zeroBalanceCode = 03, 06, or 09. The feature zeroBalanceCode tells the reason for which the balance is zero. We took a stratified sample of the data to make sure the ratio of default vs non-default sample is same in both the original and the sample dataset. As the original dataset is an imbalanced dataset, the sampled data contains 113,130 records, out of which only 198 of the records are defaults, giving us a highly imbalanced dataset with only .18% (<1%) of target samples. In the anomaly detection problem, the class imbalance is not uncommon. In total there are 54 features in the dataset. We removed 24 unimportant features using feature ranking of the Random Forest algorithm, which gives us 30 features that we use for the experiments. Furthermore, we use 70% of the data for training the models and kept 30% of the data as a holdout set to test the model. We make sure the target class has the same ratio in both the training and test sets.

4 EXPERIMENTS

First, in the feature generalizer (see Section 3.1), for frequent feature mining, we use the Python-based library Mlxtend [61], which is actually an implementation of the Apriori algorithm. Second, in the evaluator (see Section 3.2), all supervised algorithms are implemented using the Python-based *Scikit-learn* [3] library. In addition, we use Tensorflow [5] for the Artificial Neural Network. We run all experiments on a laptop with 12GB of RAM and a core i7 processor.

In our research, we investigated a wide-variety of approaches [8, 9, 12, 15, 16, 18, 20, 24-29, 33, 35-38, 45, 46, 48, 49, 53, 54, 60, 65-70, 74, 77] related to mortgage default/bankruptcy prediction and collected all explanatory variables (i.e., features) [40]. These collected features are the input data for the frequent feature mining algorithm. The output is the frequent feature sets. The hyperparameters for the frequent pattern mining algorithm (i.e., Apriori) are a minimum support threshold .05 and a maximum length 8. Here, support for a set of feature(s) is the ratio of the number of research paper containing that feature(s) and the total number of the research paper. Furthermore, maximum length refers to the maximum number of features that we want to see in any frequent feature set. We brought 5 C's of credit as a concept from the domain and mapped the frequent features with the individual C's. We only keep the frequent feature sets that have at least one matching feature from each of the C's in the 5 C's of credit. Table 3 shows how we conducted mapping and 4 shows the mapped generalized frequent feature set. We wrote a python script [41] to do this mapping.

In the evaluator part, we use the Freddie Mac dataset for experimenting with the supervised algorithms ANN, SVM, RF, GB, and ET used in this work. We took a stratified sample of the data which contains 113,130 records, out of which 198 of the records are default giving us a highly imbalanced dataset with only .18% (<1%) of target samples. Furthermore, we use 70% of the data for training the models and kept 30% of the data as a holdout set to test the model. We confirmed the target class had the same ratio in both sets. We run the supervised algorithms in two different ways:

- (1) using original features: we use all 30 selected features given by the feature selection algorithm;
- (2) using generalize frequent features set: we use each of the 25 generalized features sets separately for each algorithm. Each of the generalized feature sets consists of eight generalized feature based on the mapping from the domain knowledge (see Table 3 and 4). Out of the 25 runs for each algorithm with a different generalized feature set, we observe the performance and report the best performance with a corresponding generalized feature set in Section 5.

5 RESULTS AND DISCUSSION

The frequent pattern mining algorithm gives us a total of 4,691 different combinations of feature sets. We discard feature sets that consist of less than eight features because frequent feature sets need to be big enough to cover at least one feature from each of the 5 C's. In addition, a few of the 5 C's are related to two or more features. By keeping combinations that consist of only eight features, we get 231 combinations of frequent feature sets. Table 2 exhibits few randomly chosen frequent feature sets of length 8.

Table 3 shows a mapping of the 5 C's to relevant features based on the information from [11, 63]. So far, we have 231 frequent feature sets irrespective of those containing at least one representative feature (based on mapping in 3) from each C of the 5 C's of credit . We filter these frequent feature sets of length 8 by matching with the features mapping in Table 3 —all feature sets that don't contain at least one of the features from each category (each of the 5 C's) is discarded. This gives us 25 feature sets where each of the feature sets contains at least one of the features under each C of the 5 C's of credit. We call these 25 feature sets the *generalized frequent feature sets*. Table 4 shows some random generalized features sets.

Table 5 exhibits the performance comparison of different algorithms with or without using the generalized frequent feature set in terms of different performance metrics. An appended -G after the algorithm name refers to when the algorithm is run using the generalized frequent feature set. In addition, Figure 3 complements Table 5 by providing the dispersion in performance metrics when using the generalized frequent feature set. Surprisingly, for all algorithms, there is no difference in accuracy in either of the cases when we use the generalized frequent features set or the original feature set. However, accuracy is not a good fit for our dataset to measure the performance due to a high imbalance in the data. The model can achieve a very high accuracy by classifying most of the samples as the majority class, which is misleading. Instead, recall, precision, fscore, and ROC-AUC are better measurements as it takes into account the misclassification errors (Type I error or false positives, Type II error or false negatives) that the model makes. In terms of precision, for all algorithms, performance drops slightly (in between 2 to 5%) when using the generalized frequent feature set. In terms of recall and fscore, GB-G is the best and SVM-G is the worst. In terms of ROC-AUC, ANN-G is the worst and ET-G is the best. Overall, in terms of recall, precision, and fscore, the algorithm using the generalized frequent feature set performs better than when the same algorithms uses the original features of the dataset. Islam et al.

Table 1: Frequent features found in different mortgage bankruptcy prediction literature with their appearance count and brief description

Feature	Count	Description			
creditScore	26	A number in between 300 and 850 that indicates the borrower's creditworthiness.			
LTV	20	Loan amount divided by the appraised value of the property.			
LTVoriginal	13	Original mortgage loan amount divided by the appraised value of the property on th note/purchase date.			
creditScoreOriginal	12	Credit score at loan origination time.			
interestRateOriginal	10	Original interest rate as indicated by the mortgage note.			
interestRateCurrent	9	Active interest on the note.			
CLTVoriginal	8	Sum of all mortgage loans disclosed by the borrower divided by the apprised price of			
		the mortgaged property on the note date.			
propertyState	8	The territory of the property securing the mortgage.			
UPBoriginal	8	Unpaid principle balance on the note date.			
postalCode	7	Denotes first three digits of five-digit postal code where the property is located.			
DebtToIncomeRatioOriginal	6	Sum of monthly total debt payment divided by borrower's monthly income.			
loanAge	6	Number of month passed since its origination.			
CLTV	6	Sum of all mortgage loans disclosed by the borrower divided by the apprised price of			
		the mortgaged property.			
numberOfBorrowers	5	Number of borrowers obligated to repay the loan.			
UPBactual	5	Unpaid principle balance as of latest month of payment.			
currentLoanDelinquencyStatus	4	Indicates the number of days the borrower is delinquent.			
numberOfUnits	4 Indicates the number of unit in the property.				

Table 2: Some randomly chosen frequent feature set of length 8 and minimum support .05

Frequent Feature Set

{UPBoriginal, LTV, LTVoriginal, creditScoreOriginal, interestRateCurrent, UPBactual, propertyState, creditScore}

 $\{postal Code, interest Rate Current, property Type, loan Term Original, Debt To Income Ratio Original, product Type, property State, credit Score\}$

{postalCode, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBactual, propertyState, creditScore}

 $\{UPBoriginal, postalCode, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBactual, propertyState, creditScore\} \\ \{postalCode, interestRateOriginal, prepaymentPenaltyMortgageFlag, interestRateCurrent, productType, UPBoriginal, propertyState, creditScore\} \\ (PBoriginal, propertyState, creditScore)$

{interestRateOriginal, interestRateCurrent, propertyType, loanTermOriginal, DebtToIncomeRatioOriginal, productType, UPBoriginal, prepaymentPenaltyMortgageFlag}

Table 3: Feature mapping with 5 C's of credit

5 C's	Mapped Feature from Frequent Feature Set
Character	creditScore, creditScoreOriginal, creditScore-
	Coborrower
Capacity	debtToIncomeRatioOriginal, currentDelinquen-
	cyStatus
Capital	UPBactual, UPBoriginal
Conditions	property State, interest Rate Current, interest Ra-
	teOriginal, postalCode
Collateral	LTV, LTVoriginal, CLTV, CLTVoriginal

Furthermore, from Figure 4, we can also see that, for the most important performance metric recall, we are getting better performance (ranging from 2-10%) for ANN-G, RF-G, and GB-G. In terms

of any performance metrics, there is at least one algorithm that performs better or equal using the generalized frequent feature. We need to choose the right algorithm based on the class distribution in the data as performance metric response differs based upon the distribution of the class in the data. Furthermore, when we use the generalized feature sets, we run the algorithm on all 25 generalized feature sets to discover the best feature sets. We found that using frequent feature set # 5 (see Table 4), out of the 25 generalized feature sets, for algorithms RF-G, ET-G, and GB-G we are able to achieve the best result based on performance metric *recall*. For ANN-G and SVM-G, pattern 3 and 6 worked better accordingly. Therefore, this helps to choose the best generalized frequent feature set for a particular algorithm among many generalized frequent feature sets.

Table 4: Frequent feature set that matches 5 C's of credit

SL#	Frequent Feature Set
1	$\{number Of Borrowers, postal Code, interest Rate Original, interest Rate Current, current Loan Delinquency Status, CLT Voriginal, and Code and Co$
	UPBactual, creditScore}

- 2 {numberOfBorrowers, postalCode, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBoriginal, creditScore}
- 3 {numberOfBorrowers, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBactual, propertyState, creditScore}
- 4 {numberOfBorrowers, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBoriginal, propertyState, creditScore}
- 5 {numberOfBorrowers, UPBoriginal, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBactual, creditScore}
- 6 {postalCode, interestRateOriginal, interestRateCurrent, currentLoanDelinquencyStatus, CLTVoriginal, UPBactual, propertyState, creditScore}

Table 5: Comparison of accuracy, precision, recall, F-score, ROC-AUC, and computation time between algorithms using original features and generalized frequent features

Alg.	Acc. Prec.		Rec.	F.	AUC	Time
ANN	0.999	0.845	0.831	0.838	0.980	458.852
ANN-G	0.999	0.794	0.847	0.820	0.924	23.259
	0.000	0.051	(0.017)	0.018	0.057	435.593
SVM	VM 0.997		0.881	0.507	0.995	955.312
SVM-G	0.997	0.310	0.763	0.441	0.997	491.200
	0.000	0.046	0.119	0.066	(0.002)	464.112
RF	1.000	1.000	0.831	0.907	0.958	12.371
RF-G	1.000	0.982	0.932	0.957	0.983	1.948
	0.000	0.018	(0.102)	(0.049)	(0.025)	10.423
ET	1.000	1.000	0.831	0.907	0.966	219.501
ET-G	1.000	0.979	0.797	0.879	1.000	5.576
	0.000	0.021	0.034	0.029	(0.034)	213.925
GB	1.000	0.932	0.932	0.932	0.999	625.230
GB-G	1.000	0.966	0.949	0.957	0.999	373.387
	0.000	(0.033)	(0.017)	(0.025)	0.000	251.843

We only tested with the *Freddie Mac* dataset and there is a chance that the original features (even after excluding unnecessary features using the feature selection technique) still overfit the model, which leads to a better or equal result for all performance metrics in our case. Validating the result with multiple datasets is part of the future direction of this work. Furthermore, overall, all algorithms using a generalized frequent feature set takes less execution time compared to their counterparts due to the much fewer number of features. For a few algorithms (e.g., ANN), a fewer number of features decreases the computation time.

Overall, even though infusing domain knowledge might lead to some compromise in performance, clearly it ensures better explainability and interpretability as the output is made from a concise and familiar set of features from the domain. Our success so far is in the generation of the output using an intuitive set of features. Our further concern is to show the result in an interpretable way. One way is by expressing the output as a percentage of the total

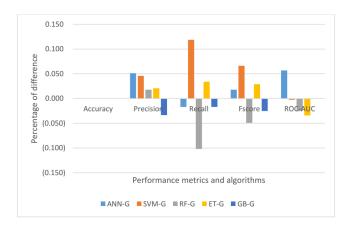


Figure 3: Dispersion in performance metrics for the case of using generalized frequent feature set

risk, and the segregation of the output value is the percentage that each of the generalized frequent features is liable. We can express the total risk probability with the following formula:

$$P(D) = \sum_{g=0}^{G} contribution(g)$$
 (1)

where g is the generalized frequent feature. Instead of using contributions from generalized frequent features, we can also express the output in terms of the contribution from each element of the domain concept. This might improve the interpretability a little bit at the expense of losing some details.

The correct way to come up with the breakdown of contribution from each feature for a particular prediction contribution is challenging. A naive approach to formulate this breakdown can be by using the importance or permutation importance of the features. However, the importance of the feature is usually calculated based on a set of data (e.g., training set) and can be achieved directly from feature importance methods in most supervised algorithms. However, in case of sample wise feature importance this is not straight forward. Moreover, the test sample might not be a good

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representative of the training set. Other work such as LIME [62], Tree Interpreter [10], SHAP [56], and ELI5 [1], can discover the contributions of features in the prediction. However, each of the available techniques/tools come with some limitations: some are applicable to only text or images individually, and some are applicable to only a class of algorithms (e.g., tree based approaches, neural networks). Most of these approaches measure the prediction deviations from the base/average scenario. Lime [62] tries to generate an explanation by locally (i.e., using local behavior) approximating the model with an interpretable model (e.g., decision trees, linear model). However, LIME is limited by the use of a linear model to approximate local behavior. Furthermore, SHAP unifies previous approaches including LIME by borrowing features from those. While SHAP comes with theoretical guarantees about consistency and local accuracy from game theory, in the case of black box kernel SHAP, it needs to run many evaluations of the original model to estimate a single vector of feature importance [55]. ELI5 also uses the LIME algorithm internally for explanations, however, the model is not truly agnostic, mostly limited to tree-based and other parametric or linear models. Tree Interpreter is limited to only tree-based approaches (e.g., Random Forest, Decision Trees). Our future work includes finding an optimal solution for sample-wise feature contribution in the prediction and express the sample-wise output according to the formula 1.

6 CONCLUSIONS AND FUTURE WORK

Due to the lack of explainability, the future adoption of "black box" models is in an inauspicious position. Governments of different countries have started to introduce laws to ensure accountability, right of explanation, and eliminating bias/discrimination in AI model decisions. Sophisticated areas such as finance, security, and healthcare need their "black box" models to offer better explanations. In this work, we demonstrated a way to collect and use domain knowledge from the literature. We also introduced a way to bring and infuse popular concepts (e.g., 5 C's of credit) from the literature that aide in better interpretability and explainability. Our experimental results show that "black box" models can be better explainable without much compromise in performance when domain knowledge is infused.

Going forward, experimenting with our proposed approach on multiple data sets will help us validate its versatility and will aide in formulating the theoretical properties of the approach. Moreover, finding an optimal solution to segregate the contribution of each participating feature (sample wise) will aide in better explainability of sample wise output and a better run-time of the model. In addition, incorporating other concepts as domain knowledge will verify its generality, making this approach transferable to other domains like cyber-security and healthcare. For instance, in cyber-security, better explanation would aide in the understanding of different attack scenarios and safeguarding the model from adversarial attacks.

ACKNOWLEDGMENTS

Thanks to Tennessee Tech Cyber-security Education, Research and Outreach Center (CEROC) for funding this research. Thanks to Dr. Doug Talbert and Dr. Ambareen Siraj for their influence/support (direct or indirect) in this work.

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