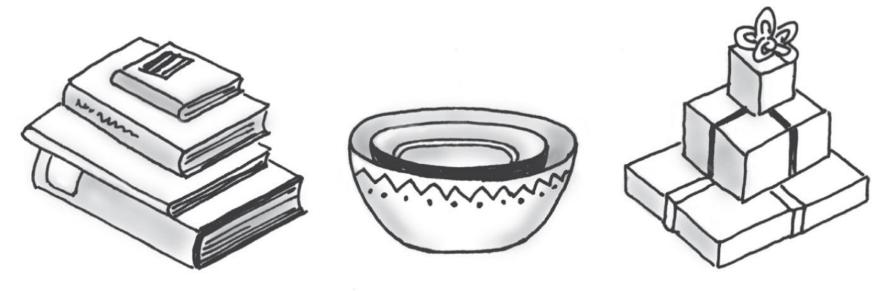
Class 03 – Stacks

CSIS 3475 Data Structures and Algorithms

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Stacks

- Add item on top of stack
- Remove item that is topmost
 - Last In, First Out ... LIFO



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• FIGURE 5-1 Some familiar stacks

Specifications of the ADT Stack • A collection of objects in reverse chronological order and having the same data type

Pseudocode	UML	Description
push(newEntry	+push(newEntry: T): void	Task: Adds a new entry to the top of the stack.
		Input: newEntry is the new entry.
		Output: None.
pop()	+pop(): T	Task: Removes and returns the stack's top entry.
		Input: None.
		Output: Returns the stack's top entry.
		Throws an exception if the stack is empty before the operation.
peek()	+peek(): T	Task: Retrieves the stack's top entry without changing the stack
		in any way.
		Input: None.
		Output: Returns the stack's top entry.
		Throws an exception if the stack is empty.
isEmpty()	+isEmpty(): boolean	Task: Detects whether the stack is empty.
		Input: None.
		Output: Returns true if the stack is empty.
clear()	+clear(): void	Task: Removes all entries from the stack.
		Input: None.
		Output: None.
size()	+size(): int	Task: Returns the size of the stack
		Input: None
		Output: size of the stack
toArray()	+toArray(): Object[]	Task: Returns a copy of the stack as an array
		Input:None
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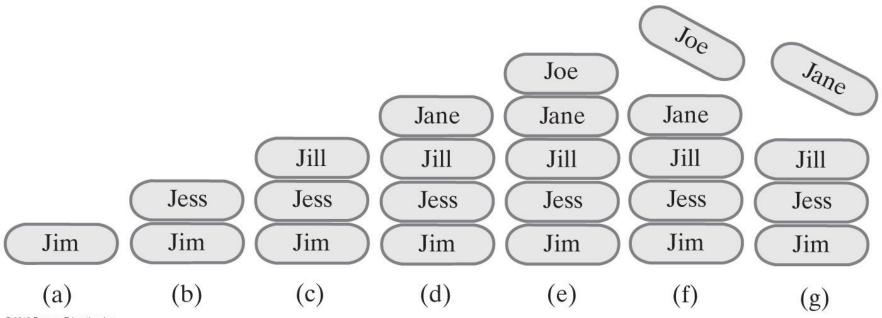
Design Decision

- When stack is empty
 - O What to do with pop and peek?
- Possible actions
 - Assume that the ADT is not empty;
 - Return null this is what we will do.
 - Throw an exception (which type?).

Stack Interface (modified from textbook)

```
public interface StackInterface<T> {
                                                        public boolean isEmpty();
   * Adds a new entry to the top of this stack.
                                                         /**
   * # @param newEntry An object added to the stack.
                                                         * Removes all entries from this stack.
                                                         */
  public void push(T newEntry);
                                                        public void clear();
  /**
   * Removes and returns this stack's top entry.
                                                         * Gets the number of elements in the stack
                                                         * @return stack size
   * @return the top of the stack or null if empty
                                                         */
                                                        public int size();
  public T pop();
  /**
                                                         * Gets a copy of the stack as an array.
   * Retrieves this stack's top entry.
                                                         * Top of stack is the last element in the array.
   * @return The top of the stack or null if empty
                                                         * @return copy of the stack
   */
                                                         */
  public T peek();
                                                        public T[] toArray();
  /**
   * Detects whether this stack is empty.
   * @return True if the stack is empty.
```

Example of a Stack of Strings

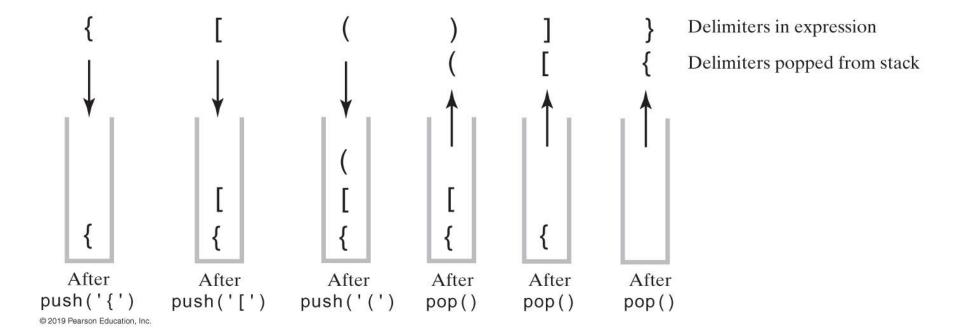


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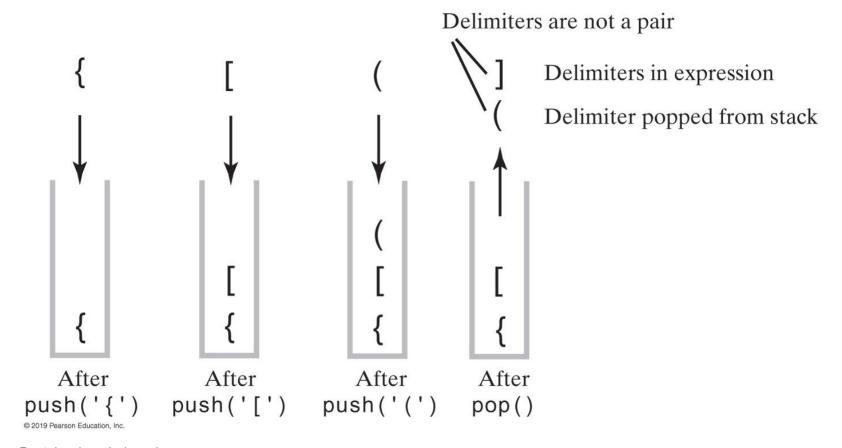
```
StackInterface<String> stringStack = new OurStack<>();
(a) stringStack.push("Jim");
(b) stringStack.push("Jess");
(c) stringStack.push("Jill");
(d) stringStack.push("Jane");
(e) stringStack.push("Joe");
(f) stringStack.pop();
(g) stringStack.pop();
```

- Infix:
 - o each binary operator appears between its operands
 - a + b
- Prefix:
 - o each binary operator appears before its operands
 - + a b
- Postfix:
 - o each binary operator appears after its operands
 - a b +
- Balanced expressions: delimiters paired correctly

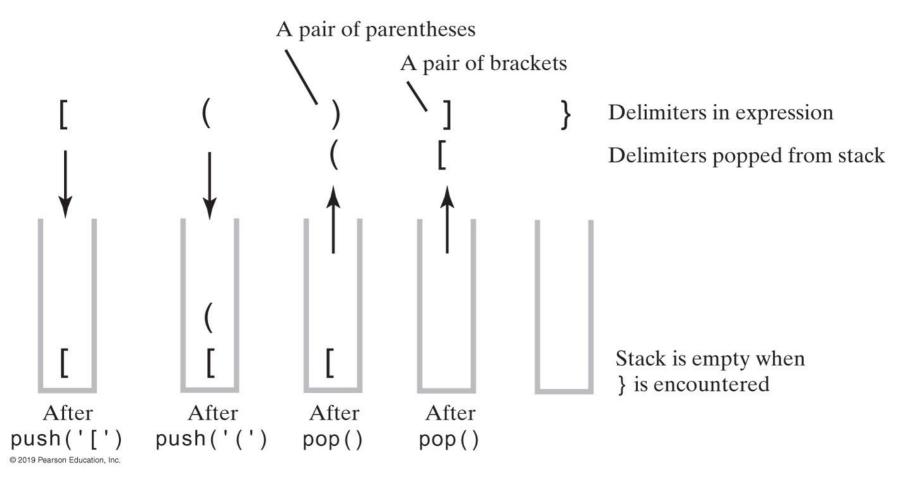
 FIGURE 5-3 The contents of a stack during the scan of an expression that contains the balanced delimiters{ [()] }



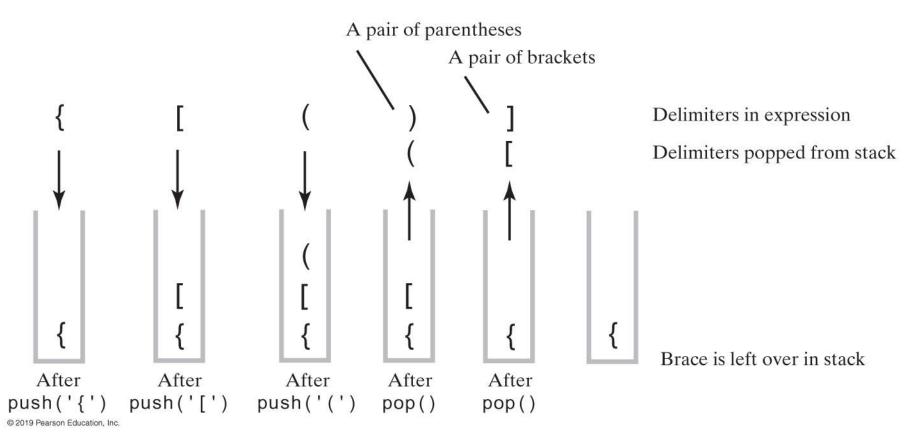
 The contents of a stack during the scan of an expression that contains the unbalanced delimiters { [(]) }



 The contents of a stack during the scan of an expression that contains the unbalanced delimiters [()] }



 The contents of a stack during the scan of an expression that contains the unbalanced delimiters { [()]



```
Algorithm checkBalance(expression)
//Returns true if the parentheses, brackets, and braces in an expression are paired correctly.
isBalanced = true // The absence of delimiters is balanced
while ((isBalanced == true) and not at end of expression)
    nextCharacter = next character in expression
    switch (nextCharacter)
        case '(': case '[': case '{':
                                             Push nextCharacter onto stack
                                             break
        case ')': case ']': case '}':
             if (stack is empty)
                 isBalanced = false
             else
                 openDelimiter = top entry of stack
                 Pop stack
                 isBalanced = true or false according to whether openDelimiter and
                                                      nextCharacter are a pair of delimiters
             break
if (stack is not empty)
    isBalanced = false
return isBalanced
```

BalanceChecker Class (see Demo)

```
public class BalanceChecker {
         * Decides whether the parentheses, brackets, and braces in a string occur in
           @param expression A string to be checked.
         * @return True if the delimiters are paired correctly.
        public static boolean checkBalance(String expression) {
                 Stack<Character> openDelimiterStack = new Stack<Character>();
                 boolean isBalanced = true; // assume it is balanced to start
        // continue as long as it is balanced and we have characters in the expression
                 for(int i = 0; isBalanced && (i < expression.length()); i++) {</pre>
                          char c = expression.charAt(i); // get the character
                          switch (c) {
                          case
                          case
                                   // it is an opening symbol
                                   openDelimiterStack.push(c);
                          case ')':
                          case ']':
                          case '}':
                                   // it is a closing symbol
                                  // did we already see the opening one?
                                   if (openDelimiterStack.isEmpty())
                                           isBalanced = false;
                                           char openDelimiter = openDelimiterStack.pop();
                                           isBalanced = isPaired(openDelimiter, c);
                                   break:
                          default:
                                   break; // Ignore unexpected characters
                         } // end switch
                 // if the stack still has elements left, it is unbalanced!
                 if (!openDelimiterStack.isEmpty())
                          isBalanced = false;
                 return isBalanced;
        } // end checkBalance
        // Returns true if the given characters, open and close, form a pair
        // of parentheses, brackets, or braces.
        private static boolean isPaired(char open, char close) {
    return (open == '(' && close == ')') ||
                                  (open == '[' && close == ']') ||
(open == '{' && close == '}');
        } // end isPaired
```

Evaluating algebraic expressions

- How to evaluate a + b + c?
- Convert to postfix
- Evaluate postfix
- Steps
 - \circ a + b + c
 - o ab+c+ 🗐
 - Evaluate
 - abc are placed on the stack until an operator is found
 - When operator is found, evaluate, the push result back on stack
 - Repeat

Converting Infix to Postfix

a + b * c

Next Character in Infix Expression	Postfix Form	Operator Stack (bottom to top)
а	a	
+	a	+
b	a b	+
*	a b	+ *
c	abc	+ *
	a b c * a b c * +	+
	a b c * +	

a ^ b ^ c

Next Character in Infix Expression	Postfix Form	Operator Stack (bottom to top)
а	a	
^	a	٨
b	a b	٨
^	a b	^^
c	a b c	^^
	a b c ^	٨
	a b c ^ ^	

a - b + c

Next Character in Infix Expression	Postfix Form	Operator Stack (bottom to top)
а	а	
_	a	_
b	a b	_
+	a b -	
	a b -	+
С	ab-c	+
	ab-c+	

Converting Infix to Postfix

a / b * (c + (d - e))



Next Character from Infix Expression	Postfix Form	Operator Stack (bottom to top)
a	a	
/	a	/
b	a b	/
*	a b /	
	a b /	*
(a b /	* (
c	a b / c	* (
+	a b / c	* (+
(ab/c	* (+ (
d	a b / c d	* (+ (
_	a b / c d	* (+ (-
e	ab/cde	* (+ (-
)	a b / c d e -	* (+ (
,	a b / c d e -	* (+
)	a b / c d e - +	* (
,	a b / c d e - +	*
	a b/c d e - + *	

Infix-to-postfix Conversion

 To convert an infix expression to postfix form, you take the following actions, according to the symbols you encounter, as you process the infix expression from left to right:

Operand	Append each operand to the end of the output expression.	
Operator ^	Push ^ onto the stack.	
Operator +, -, *, or /	Pop operators from the stack, appending them to the output expression, until either the stack is empty or its top entry has a lower precedence than the newly encountered operator. Then push the new operator onto the stack.	
Open parenthesis	Push (onto the stack.	
(lose narenthesis	Pop operators from the stack and append them to the output expression until an open parenthesis is popped. Discard both parentheses.	

Infix-to-postfix Algorithm (Part 1)

```
Algorithm convertToPostfix(infix)
// Converts an infix expression to an equivalent postfix expression.
operatorStack = a new empty stack
postfix = a new empty string
while (infix has characters left to parse)
   nextCharacter = next nonblank character of infix
   switch (nextCharacter)
   ſ
      case variable:
         Append nextCharacter to postfix
         break
      case '^' :
         operatorStack.push(nextCharacter)
         break
      case '+' : case '-' : case '*' : case '/' :
         while (!operatorStack.isEmpty() and
       precedence of nextCharacter <= precedence of operatorStack.peek())</pre>
             Append operatorStack.peek() to postfix
             operatorStack.pop()
        operatorStack.push(nextCharacter)
        break
```

Infix-to-postfix Algorithm (Part 2)

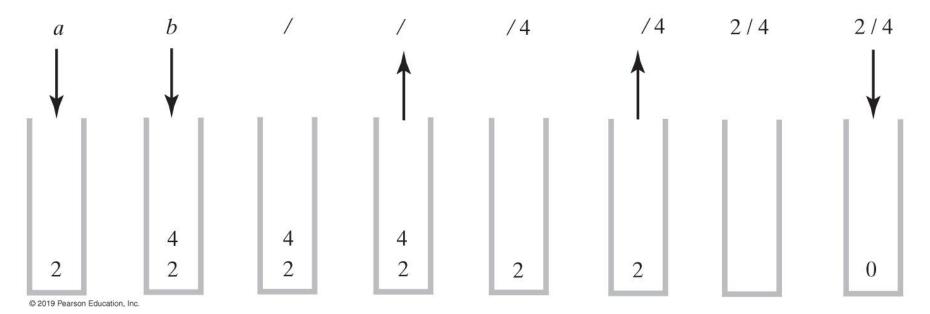
```
case '(':
         operatorStack.push(nextCharacter)
         break
      case ') ' : // Stack is not empty if infix expression is valid
          topOperator = operatorStack.pop()
         while (topOperator != '(')
            Append topOperator to postfix
             topOperator = operatorStack.pop()
         break
      default:
         break // Ignore unexpected characters
   }
while (!operatorStack.isEmpty())
   topOperator = operatorStack.pop()
   Append topOperator to postfix
return postfix
```

Evaluating Postfix Expressions

```
Algorithm evaluatePostfix(postfix)
// Evaluates a postfix expression.
valueStack = a new empty stack
while (postfix has characters left to parse)
   nextCharacter = next nonblank character of postfix
   switch (nextCharacter)
      case variable:
         valueStack.push(value of the variable nextCharacter)
         break
      case '+' : case '-' : case '*' : case '/' : case '^' :
         operandTwo = valueStack.pop()
         operandOne = valueStack.pop()
         result = the result of the operation in nextCharacter and
                  its operands operandOne and operandTwo
         valueStack.push(result)
         break
      default: break // Ignore unexpected characters
return valueStack.peek()
```

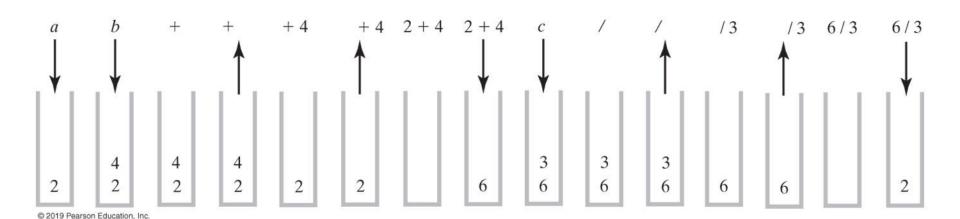
Evaluating Postfix Expressions

The stack during the evaluation of the postfix expression
 a b / when a is 2 and b is 4



Evaluating Postfix Expressions

• The stack during the evaluation of the postfix expression a b + c / when a is 2, b is 4, and c is 3



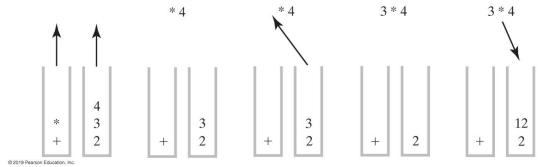
Evaluating Infix Expressions

- Two stacks during the evaluation of
- a + b * cwhen a is 2, b is 3,and c is 4

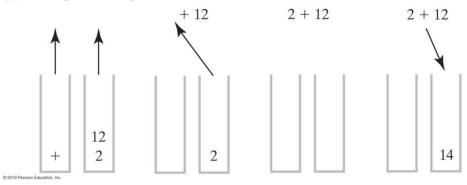
(a) After reaching the end of the expression



(b) While performing the multiplication



(c) While performing the addition



Evaluating Infix Expressions (Part 1)

```
Algorithm evaluateInfix(infix) // Evaluates an infix expression.
operatorStack = a new empty stack
valueStack = a new empty stack
while (infix has characters left to process)
   nextCharacter = next nonblank character of infix
   switch (nextCharacter)
      case variable:
         valueStack.push(value of the variable nextCharacter)
         break
      case '^' :
         operatorStack.push(nextCharacter)
         break
      case '+' : case '-' : case '*' : case '/' :
         while (!operatorStack.isEmpty() and
         precedence of nextCharacter <= precedence of operatorStack.peek())</pre>
            // Execute operator at top of operatorStack
            topOperator = operatorStack.pop()
            operandTwo = valueStack.pop()
            operandOne = valueStack.pop()
            result = the result of the operation in
             topOperator and its operands operandOne and operandTwo
            valueStack.push(result)
  ©Michael Hrybyk and crstack.push (nextCharacter)
```

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Evaluating Infix Expressions (Part 2)

```
case '(' :
         operatorStack.push(nextCharacter)
         break
      case ') ' : // Stack is not empty if infix expression is valid
         topOperator = operatorStack.pop()
         while (topOperator != '(')
            operandTwo = valueStack.pop()
            operandOne = valueStack.pop()
            result = the result of the operation in
              topOperator and its operands operandOne and operandTwo
            valueStack.push(result)
             topOperator = operatorStack.pop()
         break
      default: break // Ignore unexpected characters
   }
while (!operatorStack.isEmpty())
   topOperator = operatorStack.pop()
   operandTwo = valueStack.pop()
   operandOne = valueStack.pop()
   result = the result of the operation in
         topOperator and its operands operandOne and operandTwo
   valueStack.push(result)
return valueStack.peek()
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```

Calculator

• See Calculator.java for a complete infix to postfix example

The Application Program Stack

```
public static
     void main(string[] arg)
        int x = 5:
        int y = methodA(x);
50
     } // end main
     public static
100
     int methodA(int a)
        int z = 2;
        methodB(z);
120
        return z;
     } // end methodA
     public static
150
     void methodB(int b)
     } // end methodB
```

```
(a) When main
                      (b) When methodA
                                             (c) When methodB
  begins execution
                         begins execution
                                                begins execution
                                                 methodB
                                                   PC = 150
                                                   b = 2
                          methodA
                                                 methodA
                            PC = 100
                                                   PC = 120
                            a = 5
                                                   a = 5
                                                   z = 2
                          main
                                                main
   main
     PC = 1
                            PC = 50
                                                   PC = 50
     arg = \dots
                            arg = \dots
                                                   arg = \dots
                            x = 5
                                                   x = 5
                                                   v = 0
                            V = 0
```

Program

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Program stack at three points in time (PC is the program counter)

Java Class Library: The Class Stack

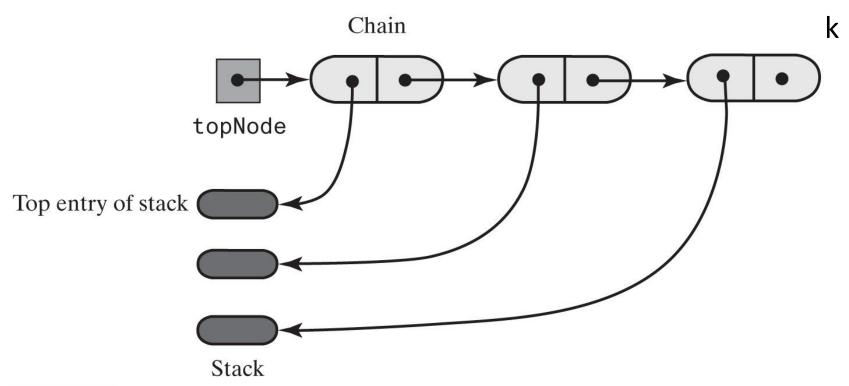
- Found in java.util
- Methods

```
o A constructor - creates an empty stack
opublic T push(T item);
opublic T pop();
opublic T peek();
opublic boolean empty();
```

Linked Stack Implementation

- Each operation involves top of stack
 - opush
 - o pop
 - o peek
- Head of linked list easiest, fastest to access
 - Let this be the top of the stack

Linked Implementation



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Use of the Node Class in LinkedStack

```
* Get the data from the node
* Node in a linked list. Each node
                                                               * @return
 * contains data and a link to the next node in the
 * list.
                                                              public T getData() {
                                                                  return data;
  @author mhrybyk
* @param <T> data type
                                                               * Set the data in the node
public class Node<T> {
                                                               * @param newData
    private T data; // Entry in bag
    private Node<T> next; // Link to next node
                                                              public void setData(T newData) {
                                                                  data = newData;
    /**
     * Create a new node containing data
     * @param dataPortion
                                                              /**
                                                               * Get the next node
    public Node(T dataPortion) {
                                                               * @return
        this(dataPortion, null);
                                                              public Node<T> getNextNode() {
                                                                  return next;
     * Create a new node containing data
     * and set the next node.
     * @param dataPortion
                                                               * Set the next node
     * @param nextNode
                                                               * @param nextNode
    public Node(T dataPortion, Node<T> nextNode) {
                                                              public void setNextNode(Node<T> nextNode) {
        data = dataPortion;
                                                                  next = nextNode;
        next = nextNode;
    /**
```

LinkedStack implementation

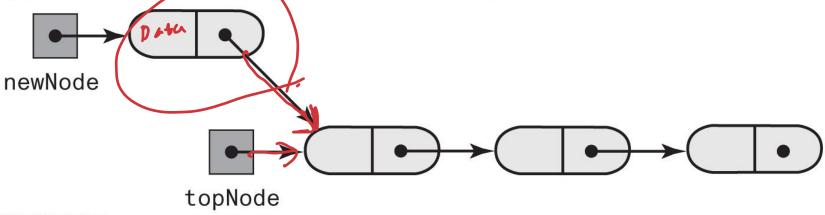
Keep the top node and a count of the number of entries

```
public final class LinkedStack<T> implements StackInterface<T> {
    private Node<T> topNode; // References the first node in the chain
    private int numberOfEntries;

public LinkedStack() {
        topNode = null;
        numberOfEntries = 0;
}
```

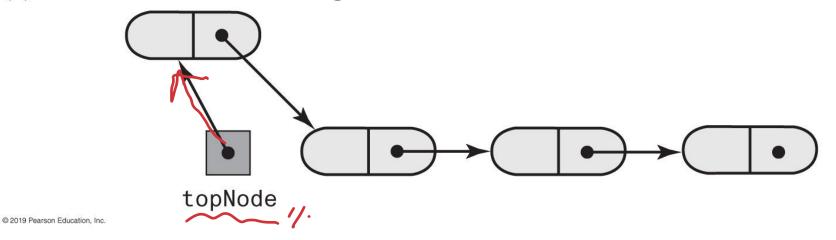
Pushing a new node onto the stack

(a) A new node that references the node at the top of the stack



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(b) The new node is now at the top of the stack



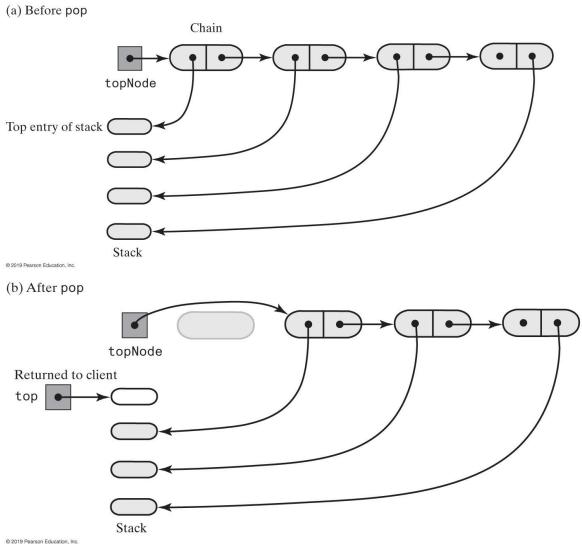
push()

- Create a new node, and make that the top
- The new node's next link is the old top node.
- New items are therefore always at the front
- Make sure we increase the number of entries (used for size())

```
public void push(T newEntry) {
    // create a new node, set its next node to the top
    Node<T> newNode = new Node<T>(newEntry, topNode);
    // set the top to the new node just created
    topNode = newNode;
    numberOfEntries++;
    // topNode = new Node<T>(newEntry, topNode); // Alternate code
}
```

Popping a node from the stack

• The stack before and after pop deletes the first node in the chain



pop()

- peek() and get the top node
- Set the top node to the next one in the chain

```
public T pop() {
    if(isEmpty())
        return null;

    // get the top node

    T top = peek();

    // set the top to the next node

    topNode = topNode.getNextNode();
    numberOfEntries--;
    return top;
}

public T peek() {
    if (isEmpty())
        return null;
    else
        return topNode.getData();
}
```

Other LinkedStack methods

- clear()
 - note that we only have to set top to null and the number of entries to 0. Garbage collection takes care
 of cleaning things up.
- toArray()
 - o to convert to array, we have to walk down the chain and copy each node's data to the array.

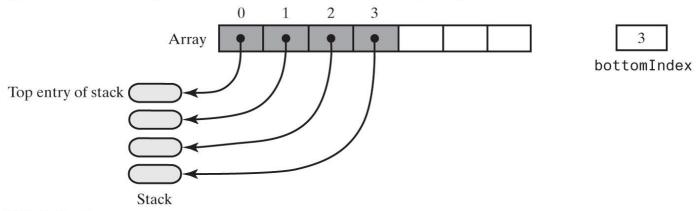
```
public void clear() {
  topNode = null; // Causes deallocation of nodes in the chain
  numberOfEntries = 0;
@Override
public int size() {
  return numberOfEntries;
@Override
public T[] toArray() {
  // create a new array
  @SuppressWarnings("unchecked")
  T[] tempStack = (T[]) new Object[size()];
  // walk along the chain, copying the data to the array each iteration
      index = 0;
      (Node<T> currentNode = topNode; currentNode != null; currentNode = currentNode.getNextNode()) {
    tempStack[index] = currentNode.getData();
    index++;
  return tempStack;
```

Array-Based Stack Implementation

- Each operation involves top of stack
 - o push
 - o pop
 - o peek
- End of the array easiest to access
 - Let this be top of stack
 - Let first entry be bottom of stack

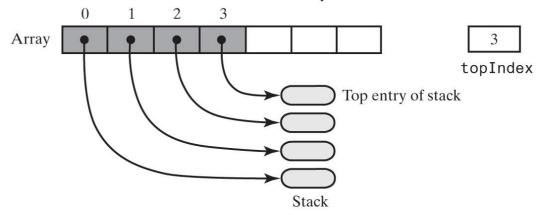
Two array representations of a stack: from the top or bottom

(a) Inefficient: The array's first element references the stack's top entry



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(b) Efficient: The array's first element references the stack's bottom entry



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ArrayStack implementation

- Uses a backing array and an index to the top of the stack.
- As we add items, the index will grow.
- Index starts at -1, so top of stack for first element added will be 0

```
public final class CompletedArrayStack<T> implements StackInterface<T> {
    private T[] stack; // Array of stack entries
    private int topIndex; // Index of top entry

    private static final int DEFAULT_CAPACITY = 50;
    private static final int MAX_CAPACITY = 10000;

    public CompletedArrayStack() {
        this(DEFAULT_CAPACITY);
    }

    public CompletedArrayStack(int initialCapacity) {
        checkCapacity(initialCapacity); // do we have enough room?

        // The cast is safe because the new array contains null entries
        @SuppressWarnings("unchecked")
        T[] tempStack = (T[]) new Object[initialCapacity];
        stack = tempStack;
        topIndex = -1; // note default value
}
```

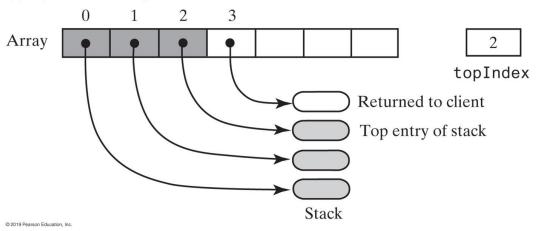
push()

- Make sure we have enough room.
 - If not, double the size of the array.
 - Copy the old elements to the new array. Expensive to do.
- Increment the top index, and store the data there

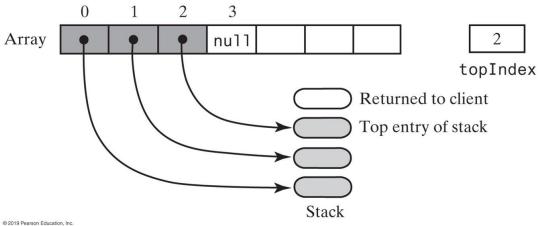
```
public void push(T newEntry) {
   ensureCapacity(); // make sure we have enough room
   // place the entry at the end, and increment the index
   stack[topIndex + 1] = newEntry;
   topIndex++;
* Throws an exception if the client requests a capacity that is too large.
* @param capacity requested capacity
private void checkCapacity(int capacity) {
   if (capacity > MAX CAPACITY)
      throw new IllegalStateException(
             "Attempt to create a stack " + "whose capacity exceeds " + "allowed maximum.");
* Doubles the size of the array stack if it is full
private void ensureCapacity() {
   if (topIndex >= stack.length - 1)
      // the array is full, so double the size
      int newLength = 2 * stack.length;
      checkCapacity(newLength);
      // copyOf will create a new array with
      // the larger size and copy all elements
      stack = Arrays.copyOf(stack, newLength);
```

pop(): An array-based stack after its top entry is removed in two different ways

(a) By decrementing topIndex



(b) By setting stack[topIndex] to null and then decrementing topIndex



pop() and peek()

- Get the element at the top. Operation is O(1)
- For pop(), then decrement the index

```
public T pop() {
     if (isEmpty())
          return null;
     else {
          // get the top index
          T top = stack[topIndex];
          // now set that location to null
          // and decrement the index
          stack[topIndex] = null;
          topIndex--;
          return top;
     } // end if
public T peek() {
     if (isEmpty())
           return null;
     else
           return stack[topIndex];
```

Other methods

- clear() could just set topIndex to -1 directly, but setting everything to null is safer
- Notice simple array copy for toArray()

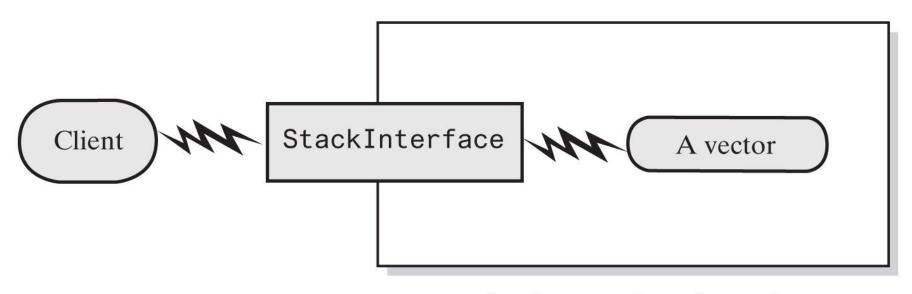
```
public boolean isEmpty() {
    return topIndex < 0;</pre>
public void clear() {
    // Remove references to the objects in the stack,
    // but do not deallocate the array
    // note that topIndex reverts to -1
    while (topIndex > -1) {
         stack[topIndex] = null;
         topIndex--;
public T[] toArray() {
    return Arrays.copyOf(stack, [
                                     5.size());
public int size() {
    return topIndex + 1;
```

Vector-Based Stack Implementation

- The class **Vector**
 - An object that behaves like a high-level array
 - Index begins with 0
 - Methods to access or set entries
 - Size will grow as needed
 - Has methods to add, remove, clear
 - Also methods to determine
 - o Last element
 - Is the vector empty
 - Number of entries
- Use vector's methods to manipulate stack

Vector-Based Stack Implementation

 FIGURE 6-6 A client using the methods given in StackInterface; these methods interact with a vector's methods to perform stack operations



Implementation of a stack

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VectorStack implementation

- Use Vector as backing object for the stack
- Use Vector methods to implement stack methods
- Vector will grow dynamically, no need to increase size

```
public final class CompletedVectorStack<T> implements StackInterface<T> {
    private Vector<T> stack; // Last element is the top entry in stack

    // Vector class can grow dynamically, so no need to increase

    private static final int DEFAULT_CAPACITY = 50;

    public CompletedVectorStack() {
        this(DEFAULT_CAPACITY);
    }

    public CompletedVectorStack(int initialCapacity) {
        stack = new Vector<>(initialCapacity); // Size doubles as needed
}
```

push(), peek(), pop()

- Simply use Vector methods
- remove() needs an index, so we calculate the last one as size 1

```
public void push(T newEntry) {
    stack.add(newEntry);
public T peek() {
    if (isEmpty())
         return null;
    else
         return stack.lastElement();
}
public T pop() {
    if (isEmpty())
         return null;
    else
         return stack.remove(stack.size() - 1);
}
```

Other methods

 Notice toArray() needs an array of the appropriate size to copy into.

```
public boolean isEmpty() {
     return stack.isEmpty();
public void clear() {
     stack.clear();
}
@Override
public int size() {
    return stack.size();
}
public T[] toArray() {
    @SuppressWarnings("unchecked")
    T[] tempStack = (T[]) new Object[size()];
    // Vector toArray() requires an array as an arg to fill in
    return stack.toArray(tempStack);
}
```

Java library Stack class

- Has all of the methods of StackInterface more or less.
- See StackDemo for examples.

In class exercises

- Complete
 - ArrayStack.java
 - VectorStack.java
 - LinkedStack.java
- Test using StackTestDriver.java and BalanceCheckerDemo.java
- These classes will be used again in the future, so save your work.