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Yoon

CSC345-02

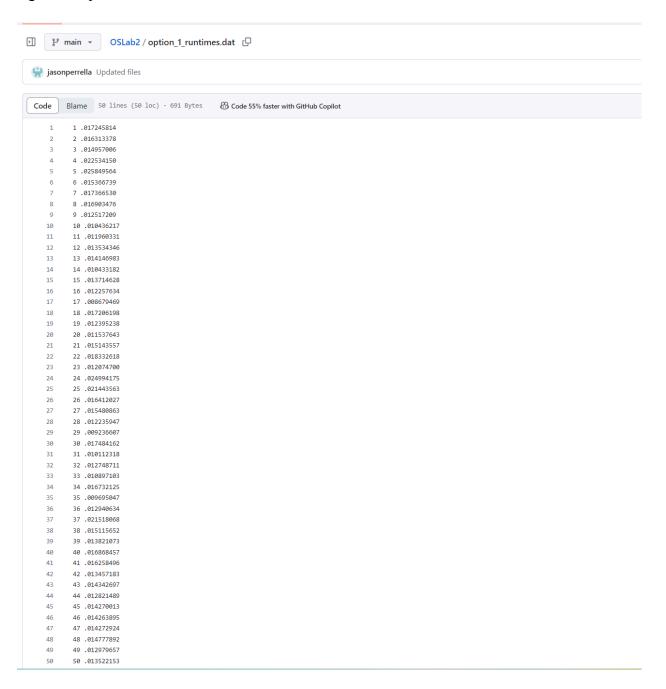
10 March 2024

## Project 2

For project two, we were tasked with developing a sudoku-board validity checker, with three methods of checking. For option one, one thread was to be used for checking rows, one thread for columns, and nine for each subgrid in the 9x9 grid, totaling 11 threads. Option two was similar, but instead of one thread for the rows and columns, it was nine for each, resulting in 27 total threads. Option three was a multiprocess implementation in which three child processes were created, one for checking rows, one for checking columns, and one for checking subgrids. After whichever option was chosen completes, the variable used to track the validity is used to determine what is outputted (valid or not), along with a variable used to hold the amount of time the execution took. Implementing the first two options was not that difficult, however, option three gave some trouble. At one point just before we finished, the program was able to successfully identify an invalid board with every option, but if the board was valid, only options one and two worked. We were using a pipe to allow the processes to communicate and update the variable valid, but every time the program got to the parent process and attempted to read from the pipe, nothing would occur because the problem, which was very simple, was that we were not closing the write end of the pipe in the parent process. After implementing that, the program was finished. To run each option 50 times, we wrote a bash script that would write the execution times to a .dat file and used the MATPLOTLIB python library to generate graphs to

analyze options 1 and 2, options 2 and 3, and options 1 and 3. We used Pandas and SciPy to load the data into a dataframe and run the hypothesis tests(This was not required by the project requirements but we wanted to make it easier to plot graphs, and run hypothesis tests as the math could easily be done by these libraries and is less error prone).

Figure 1: Option 1 Runtimes



# Figure 2: Option 2 Runtimes

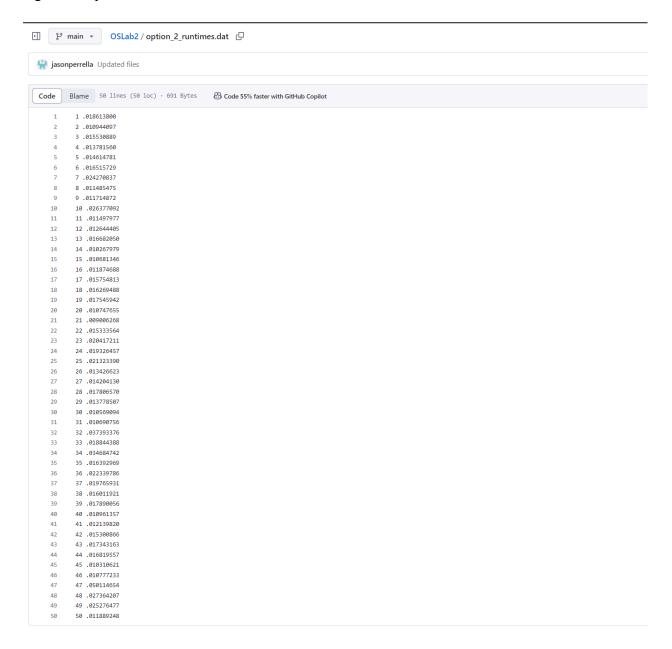


Figure 3: Option 3 Runtimes

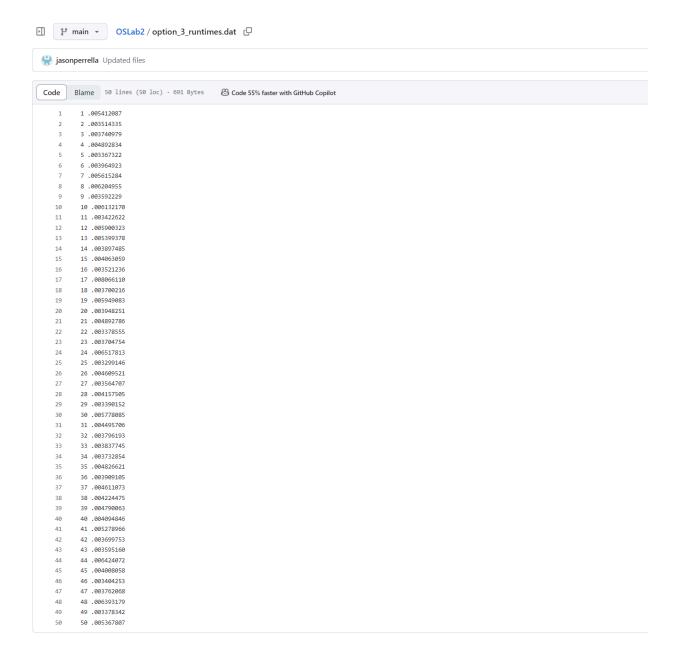


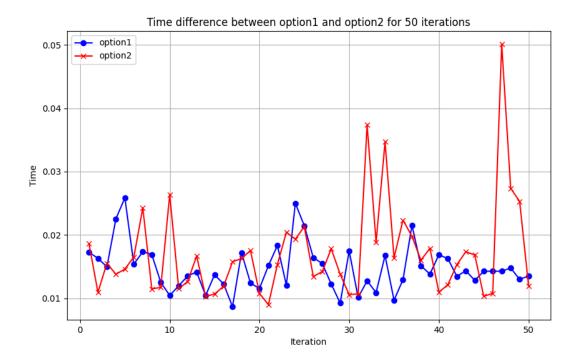
Figure 4: Bash shell script. The graphing did not work. We needed to use our own local machines to graph everything.

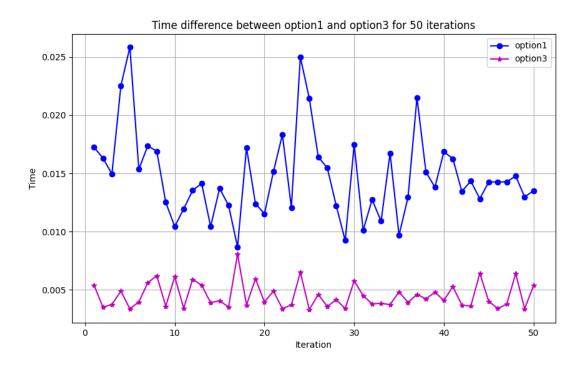
```
P main → OSLab2 / sudoku.sh
 igasonperrella adding files to repo
 for option in 1 2 3; do
               data_file="option_${option}_runtimes.dat"
               graph_file="option_${option}_graph.png"
               total time=0
               iterations=50
               echo "Option $option Runtimes:"
     11
               for i in $(seq 1 $iterations); do
                  start_time=$(date +%s.%N)
     12
     13
                   ./main $option
                  end_time=$(date +%s.%N)
                   duration=$(echo "$end_time - $start_time" | bc)
                  total_time=$(echo "$total_time + $duration" | bc)
     17
     18
                  # Print '*' for each second of runtime
                  seconds=\$(echo "\$duration/1" | bc) \\ printf "%3s | %s\n" "\$i" "\$(yes '*' | head -n \$seconds | tr -d '\n')" \\ echo "\$i $duration" >> "\$data_file" \\ \end{aligned}
     19
     20
     21
     22
     23
     24
               avg time=$(echo "$total time/$iterations" | bc -1)
     25
               echo -e "\nAverage execution time for option $option: $avg_time seconds\n"
     26
     27
            # Plot graphs after the 3rd option using Python and matplotlib
            if command -v python3 &> /dev/null; then
               python3 - <<EOF
     31
           import matplotlib.pyplot as plt
     33
            for option in [1, 2, 3]:
     34
               data_file = f"option_{option}_runtimes.dat"
               graph_file = f"option_{option}_graph.png"
     35
     36
               with open(data file, 'r') as f:
     37
                  data = [line.split() for line in f.readlines()]
     38
               iterations, runtimes = zip(*data)
               plt.plot(iterations, runtimes, label=f'Option {option} Runtimes')
            plt.title('Runtimes for Options 1, 2, and 3')
     44
            plt.xlabel('Iteration')
     45
            plt.ylabel('Runtime (seconds)')
     46
            plt.legend()
     47
            plt.savefig('combined_graph.png')
     48
            plt.show()
     49
            EOF
```

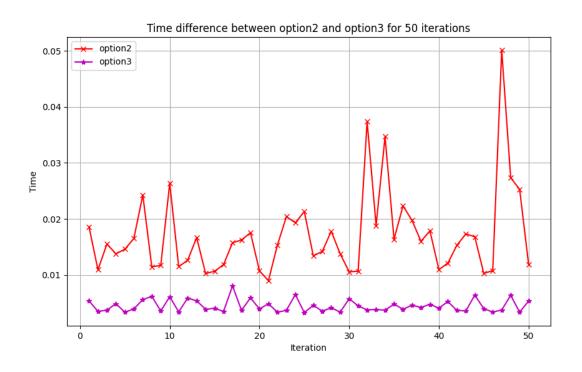
Figure 5: Hypothesis Testing Script

```
import pandas as pd
df = pd.read_csv(filename, names=['Iteration', 'Time'], sep=' ')
df2 = pd.read_csv(filename2, names=['Iteration', 'Time'], sep=' ')
df3 = pd.read_csv(filename3, names=['Iteration', 'Time'], sep=' ')
print(df)
times_option1 = df['Time']
times_option2 = df2['Time']
times_option3 = df3['Time']
_, p_value_normality_option1 = stats.shapiro(times_option1)
_, p_value_normality_option2 = stats.shapiro(times_option2)
_, p_value_normality_option3 = stats.shapiro(times_option3)
print(f"Normality test p-value for option 1: {p_value_normality_option1}")
print(f"Normality test p-value for option 3: {p_value_normality_option3}")
if p_value_normality_option1 > 0.05 <mark>and</mark> p_value_normality_option2 > 0.05 <mark>and</mark> p_value_normality_option3 > 0.05:
    t_stat, p_value = stats.ttest_ind(times_option1, times_option3, equal_var=False)
    u_stat, p_value = stats.mannwhitneyu(times_option1, times_option3)
    print(p_value)
print(f"Method 1 average runtime: {times_option1.mean()}")
print(f"Method 2 average runtime: {times_option3.mean()}")
if p_value < 0.05:
```

Figures 6 - 8: Graphs







## **Hypothesis Testing:**

The hypothesis tests we will be running are based on the assumptions from the Mann-Whitney U test:

- 1. All of the observations from both groups are independent of each other.
- 2. The responses are at least ordinal.
- 3. Under the null hypothesis, the distributions of both populations are identical.
- 4. Under the alternative hypothesis, the distributions of both populations are not identical.

## **Hypothesis Testing:**

We generated a python script to test whether the population for method A and method B were normal. By utilizing the Shapiro-Wilk Test(SWT) for normality, we determined that neither of the population distributions were normal for an alpha of 0.05:

- p-value for option 1(SWT) = 0.0037256674841046333 < 0.05 we reject that the population distribution for option 1 is normal because the p-value is less than alpha.
- p-value for option 2(SWT) = 3.005404494160757e-07 < 0.05 we reject that the population distribution for option 2 is normal for the same reason above.
- p-value for option 3(SWT) = 7.0082867750898e-05 < 0.05 we reject that the population distribution for option 3 is normal for the same reason above.

Therefore, we will use the Mann-Whitney U-test(MWU) for all of our tests. This test does not assume that the population distributions for methods A and B are normal. From the

Mann-Whitney U-test assumptions, we can determine that the observations from methods A and B are independent of each other since we ran 50 experiments in succession(technically a simple random sample) for each option and the times we received from those runs had no effect on the other runs. So, the independence condition is satisfied. The responses(execution times) are at least ordinal since we can determine a clear ordering of the time values. These values were measured on a continuous scale and therefore, allows for a clear measurement of the magnitude of difference for each run and allows for the ordering of each run from fastest to slowest run time. Therefore, the ordinal condition is satisfied. We are assuming that there is no statistically significant difference between methods A and B in our null hypothesis(H<sub>0</sub>) meaning that the distributions for both populations are identical. We are assuming that there is a statistically significant difference between methods A and B in our alternative hypothesis(H<sub>1</sub>) meaning that the distributions for both populations are not identical. The notation A and B are used as a way to generalize these assumptions to all three methods since the conclusion of the SWT was the same for all three methods and these assumptions were already met for comparison of each method.

#### **RESULTS:**

#### **Option 1 and Option 2 comparison:**

H<sub>0</sub>: There is no statistically significant difference between methods 1 and 2 for an alpha of 0.05.

H<sub>1</sub>: There is a statistically significant difference between methods 1 and 2.

The assumptions to be able to run the MWU-test have already been satisfied. Therefore, we can perform this test. After executing the python script(Figure 5), the resulting U-statistic calculated was U = 1084.0. The sample mean for methods 1 and 2 were 0.014792190820000002 and

0.01710636834 average run time respectively. The resulting p-value was p = 0.25390022371319265. Since we chose the alpha to be 0.05, and p >= alpha, we fail to reject the null hypothesis which means that based on our calculations we found that methods 1 and 2 are statistically indistinguishable.

## Option 2 and Option 3 comparison:

H<sub>0</sub>: There is no statistically significant difference between methods 2 and 3 for an alpha of 0.05. H<sub>1</sub>: There is a statistically significant difference between methods 2 and 3.

The assumptions to be able to run the MWU-test have already been satisfied. Therefore, we can perform this test. After executing the python script(Figure 5), the resulting U-statistic calculated was U = 2500.0. The sample mean for methods 2 and 3 were 0.01710636834 and 0.00450456488 average run time respectively. The resulting p-value was p = 7.066071930388932e-18. Since we chose the alpha to be 0.05, and p < alpha, we reject the null hypothesis which means that based on our calculations, we found that methods 2 and 3 are statistically distinguishable. Therefore, we determine that method 3 is better than method 2 in terms of run-time.

### **Option 1 and Option 3 comparison:**

 $H_0$ : There is no statistically significant difference between methods 1 and 3 for an alpha of 0.05.  $H_1$ : There is a statistically significant difference between methods 1 and 3.

7.066071930388932e-18. Since we chose the alpha to be 0.05, and p < alpha, we reject the null hypothesis which means that based on our calculations, we found that methods 1 and 3 are statistically distinguishable. Therefore, we determine that method 3 is better than method 1 in terms of run-time.