ST1131

AY21/22 Sem 2

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01. Exploratory Data Analysis

- **Quantitative Variable**: Discrete vs. Continuous
- **Categorical Variable**: Ordinal vs. Nominal
- Difference: Is distance between 2 points meaningful?

Single Variable

Frequency Table - Categorical

- **Proportion** - aka relative frequency. $\frac{\#\text{ of obs. in 1 cat.}}{Total\#ofobs.}$
- **Modal Frequency** - Category with highest frequency
- Summarizing: Modal category and its proportion

Bar Plots - Categorical

- Summarizing: Modal category and its proportion, Categories with high/low proportions, Mention trends if ordinal

Histogram - Quantitative

- Skewed left/right: Left/right tail is longer
- Summarizing: Outlier, Unimodal/Bimodal/Multimodal, Skewness

Describing Center

- **Mean** - $\bar{X} = \frac{1}{n}\sum_{i=1}^{n} x_i$
  - Linear Transformation: $\hat{Y} = b\hat{X} + a$
  - Sensitive to outliers, unlike median
- **Median** - $X_{(0.5)}$
- If $\bar{X} > X_{(0.5)}$, skew right. If $\bar{X} < X_{(0.5)}$, skew left.

Describing Variability

- **Range** - Sensitive to outliers
- **Variance** - $S^2 = \frac{1}{n-1}\sum_{i=1}^{n}(x_i - \bar{x})^2$
- **Standard deviation** - $sd = \sqrt{S^2}$
  - Linear Transformation: $S_y^2 = b^2 s_x^2$ $S_y = |b|s_x$
- **Inter-quartile Range (IQR)** - $Q_3 - Q_1$
  - **Quantile** - (q_p) Value such that p of observations are below
  - Lower quartile (Q_1), Median (Q_2), Upper quartile (Q_3)
- If symmetric, mean and variance. If skewed, median and IQR.

Boxplot - Variability

- Includes: Min, Q1, Q2, Q3, Max
- **Outliers** - $< Q_1 - 1.5IQR$ or $> Q_3 + 1.5IQR$
- **Max/min Whisker Reach** - Boundary of outliers
- **Upper/lower Whisker** - Min/max obs. excluding outliers
- Does not show features of distribution. If unimodal, can show skewness.
- Summarizing: Median, Outliers, Compare medians and IQR if > 1 boxplots

Two Variables

- Response Variable vs. Explanatory Variable

Bar Plots - 2 categorical

Contingency Table - 2 categorical

- **Conditional Percentage** - % out of total
- **Join Percentage** - % out of some group. Use explanatory as group.
- Be careful of phrasing (Eg. Ppl w/o cancer of PMH users vs. PMH users of those w/o cancer)
- **Relative Risk** - Ratio of 2 percentages. (Eg. % of cancer in PMH users is 1.24 times the % of cancer in non-PMH users)

2 Boxplots - 1 Categorical and 1 Quantitative

Scatter Plot - 2 Quantitative Variables

- Summarizing: Pos./neg. association, Linear, Constant variability, Outliers

Correlation - $r \in [-1, 1]$

- 2 variables have same correalation, no matter $x \sim y$ or $y \sim x$
- Correlation is linear, when $r = \pm 1$

02. Data Collection

- **Confounding Variable** - Related to exp. and resp. variable. Confounds their association. Observed.
- **Lurking Variable** - Unobserved
- **Experimental Study** - Assign subjects (or **experimental units**) to **treatments** and observe response variable
  - Pros: Control over lurking variables
  - Cons: Costly, Unethical
- **Observational Study** - Explanatory and response variable observed for subjects. No treatments.

Sample Survey

1. Identify population
2. Compile **sampling frame** - Where sample is from
3. **Sampling design** - How to choose subjects from sampling frame
   - **Simple Random Sample** - Each sample has same chance of being chosen

Sources of Bias in Sample Survey:

- **Sampling Bias** - Sample not random or undercoverage
- **Non-response Bias** - No response from subject
- **Response Bias** - Subject does not answer truthfully

Elements of Good Experimental Study:

- Control comparison group
- Randomization: Eliminate lurking variables
- Blinding the study: Placebo

03. Probabililty

- **Sample space** - (S) Set of all possible outcomes
- **Event** - (E) Subset of sample space
- $P(A) = \frac{\#\text{ of outcomes in A}}{\text{Total \# of possible outcomes}}$

Axioms of Probability

1. $0 \leq P(A) \leq 1$
2. $P(S) = 1$
3. If A and B are mutually exclusive (or **disjoint**), then $P(A \cup B) = P(A) + P(B)$ and $P(A \cap B) = 0$
4. $P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(A \cap C) - P(B \cap C) + P(A \cap B \cap C)$

For any events A and B:

- $P(A^c) = 1 - P(A)$
- $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
- $P(A) = P(A \cap B) + P(A \cap B^c)$
- A and B are **independent** if $P(A \cap B) = P(A)P(B)$

Conditional Probability

$P(A|B) = \frac{P(A \cap B)}{P(B)}$

Law of Total Probabililty

$P(A) = P(A \cap B_1) + ... + P(A \cap B_n)$

Bayes' Theorem

$P(B_i|A) = \frac{P(A|B_i)P(B_i)}{P(A|B_1)P(B_1)+...+P(A|B_n)P(B_n)}$

Epidemiological Terms:

- **Sensitivity** - Given has disease, prob. of positive test
- **Specificty** - Given has no disease, prob. of neg. test
- **Prevalence** - $\frac{\#\text{ of people with disease}}{\text{Total population}}$

04. Random Variables

05. Sampling Distribution

06. Confidence Intervals

07. Hypothesis Testing

08. Linear Regression

09. R Code

```r
# Create matrix, Bind matrices
matrix(c(1:6), nrow=2, ncol=3, byrow=T)
rbind(m, c(1,2,3))

# Read CSV, Add header, Get col. in df
data = read.csv("./crab.txt")
names(data) = c("Subject", "Gender")
data$Subject # Or attach()

# Select, Filter by condition
data[1:8,]
data[Gender == "M" & HW == "A",]

# Summary of vector
summary(marks)

# Replace elements based on condition
ifelse(Gender == "0", "F", "M")

# Return indices that match condition
which(flat == "3 ROOM")

# Frequency Table
table(data)
prop.table(table(data))

# Bar Plot
barplot(table(data))

# Contingency Table
tab = table(bbd, pmh) # (r, c)
prop.table(tab) # Joint probabililty
prop.table(tab, "pmh") # Conditional
    probability on pmh groups

# Bar Plot with 2 variables
barplot(proptab)

# Boxplot
bp = boxplot(age~cancer) # quan. ~ cat.
bp$out # Values of outliers
grp = bp$group # Outliers in each group
which(grp == 1) # Index of outliers in
    group 1
bp$out[which(grp == 1)]

# Histogram
hist(flatPrice)

# Scatter Plot, Correlation
plot(size, price) # (x-axis, y-axis)
cor(size, price)
```