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Homework #3  
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### Problem #1

== Conversion into FOL

- A.  $\forall s: \neg G(s, \text{Blues}) \vee \neg G(s, \text{Opera})$
- B.  $\forall s: W(\text{Amy}, s) \Rightarrow S(\text{Amy}, s)$
- C.  $\exists s: W(\text{Amy}, s) \wedge G(s, \text{Blues})$
- D.  $\forall s [ \exists p [ F(p, \text{Joe}) \wedge S(p, s) ] \Rightarrow L(\text{Joe}, s) ]$
- E.  $F(\text{Amy}, \text{Joe})$
- F.  $\exists s: L(\text{Joe}, s) \wedge \neg G(s, \text{Opera})$
- G.  $\forall s [ L(\text{Joe}, s) \Rightarrow \exists p [ F(p, \text{Joe}) \wedge S(s, p) ] ]$
- H.  $\forall s [ \exists p [ F(p, \text{Joe}) \wedge S(p, s) ] \Rightarrow W(\text{Ted}, s) ]$
- I.  $\forall s [ W(\text{Ted}, s) \Rightarrow \neg L(\text{Joe}, s) ]$

== Problem #2 (prove F is a consequence of A-E) ==

=== CNF

- A.  $\forall s: \neg G(s, \text{Blues}) \vee \neg G(s, \text{Opera})$
- B.  $\forall s: \neg W(\text{Amy}, s) \vee S(\text{Amy}, s)$
- C.  $\exists s: W(\text{Amy}, s) \wedge G(s, \text{Blues})$
- D.  $\forall p, s: \neg F(p, \text{Joe}) \vee \neg S(p, s) \vee L(\text{Joe}, s)$
- E.  $F(\text{Amy}, \text{Joe})$
- F.  $\exists s: L(\text{Joe}, s) \wedge G(s, \text{Opera})$

=== remove Quantifiers & break up top-level conjunctions

- A.  $\neg G(s, \text{Blues}) \vee \neg G(s, \text{Opera})$
- B.  $\neg W(\text{Amy}, s) \vee S(\text{Amy}, s)$
- C1.  $W(\text{Amy}, \text{SK1})$
- C2.  $G(\text{SK1}, \text{Blues})$
- D.  $\neg F(p, \text{Joe}) \vee \neg S(p, s) \vee L(\text{Joe}, s)$
- E.  $F(\text{Amy}, \text{Joe})$

=== negate

$$F' = \neg L(\text{Joe}, s) \vee G(s, \text{Opera})$$

=== Resolution

- G.  $\neg S(\text{Amy}, s) \vee L(\text{Joe}, s)$  (from E + D)
- H.  $\neg G(\text{SK1}, \text{Opera})$  (from A + C2)
- I.  $S(\text{Amy}, \text{SK1})$  (from B + C1)
- J.  $L(\text{Joe}, \text{SK1})$  (from G + I)
- K.  $G(\text{SK1}, \text{Opera})$  (from H + J)

==Problem #3 (prove I is a consequence of G+H )==

G.  $\forall s [ L(\text{Joe}, s) \Rightarrow \exists p [ F(p, \text{Joe}) \wedge S(s, p) ] ]$   
 $\forall s [ \sim L(\text{Joe}, s) \vee \exists p [ F(p, \text{Joe}) \wedge S(s, p) ] ]$   
 $\forall s [ \sim L(\text{Joe}, s) \vee [ F(\text{SK0}(s), \text{Joe}) \wedge S(s, \text{SK0}(s)) ] ]$   
 $[ \sim L(\text{Joe}, s) \vee [ F(\text{SK0}(s), \text{Joe}) \wedge S(s, \text{SK0}(s)) ] ]$   
 $( \sim L(\text{Joe}, s) \vee F(\text{SK0}(s), \text{Joe}) ) \wedge ( \sim L(\text{Joe}, s) \vee S(s, \text{SK0}(s)) )$

H.  $\forall s [ \exists p [ F(p, \text{Joe}) \wedge S(p, s) ] \Rightarrow \sim W(\text{Ted}, s) ]$   
 $\forall s [ \sim \exists p [ F(p, \text{Joe}) \wedge S(p, s) ] \vee \sim W(\text{Ted}, s) ]$   
 $\forall s, p [ \sim F(p, \text{Joe}) \vee \sim S(p, s) \vee \sim W(\text{Ted}, s) ]$

I.  $\sim \forall s [ W(\text{Ted}, s) \Rightarrow \sim L(\text{Joe}, s) ]$   
 $\exists s \sim (W(\text{Ted}, s) \Rightarrow \sim L(\text{Joe}, s))$   
 $\exists s W(\text{Ted}, \text{SK2}) \wedge L(\text{Joe}, \text{SK2})$   
 $W(\text{Ted}, \text{SK2}) \wedge L(\text{Joe}, \text{SK2})$

===== CNF

G1.  $\sim L(\text{Joe}, s) \vee F(\text{SK0}(s), \text{Joe})$   
G2.  $\sim L(\text{Joe}, s) \vee S(\text{SK0}(s), s)$   
H.  $\sim F(p, \text{Joe}) \vee \sim S(p, s) \vee \sim W(\text{Ted}, s)$   
I1.  $W(\text{Ted}, \text{SK2})$   
I2.  $L(\text{Joe}, \text{SK2})$

=== Resolution

J.  $F(\text{SK0}(\text{SK2}), \text{Joe})$  (from G1 + I2)  
K.  $S(\text{SK0}(\text{SK2}), \text{SK2})$  (from G2 + I2)  
L.  $\sim F(p, \text{Joe}) \vee \sim S(p, \text{SK2})$  (from H + I1)  
M.  $\sim S(\text{SK0}(\text{SK2}), \text{SK2})$  (from J + L)  
N.  $\emptyset$  (from K + M)

