```
• // ring var: RATO, all bit-level inputs (PS and PI) followed by P, S and T

    ring rr = (2,X), (n23,n43,n42,n18,n40,n39,...<omitted bit-level</li>

  intermediate vars>...,x0,x1,s0,s1,s2,s3,P,S,T), lp;

    minpoly = X^4+X+1;

ideal A in = s0,s1,s2,s3;
• poly def_S = s0+s1*X+s2*X^2+s3*X^3+S;
• ideal X in = x0,x1;
• poly def_X = x0 + x1*X^5+P;
poly red_S = S^16+S; // GF(2^4)

    poly red T = T^16+T;

• poly red_X = P^4+P; // GF(2^2) as a subset field of GF(2^4)

    // red all: vanishing polys

• ideal red_all = x0^2+x0, x1^2+x1, s0^2+s0, s1^2+s1, s2^2+s2,
  s3^2+s3,red S,red X;
• poly tran =
  T+(X^2+X+1)*x0*x1*s1*s3+(X^3+X)*x0*x1*s1+...<omitted>...;

    poly init_S = S+X^2;

 polý reached = T+X<sup>2</sup>;

// Bit-word substitution
ideal I1 = preprocess(def_S, red_all, A_in);
poly unitran = conv_word(tran,I1);
I1 = preprocess(def_X, red_all, X_in);
unitran = conv_word(unitran,I1);

    // Iterative BFS traversal

• int i = 1;

ideal from_l,to_l,new_l;
from_l[1] = init_S;

 while(1)
          i++;
to_l[i] = transition(from_l[i-1],unitran,red_all);
          "Iteration #",i-2;
"Next State(s): ",to_I[i];
          new_I[i] = redWord(to_I[i]+compl(reached,red_T), red_T);
"Newly reached states: ",new_I[i];
          if ((redWord(new_I[i], red_T) = 1) or (i>MAX_iter))
                    break;
          reached = redWord(reached * new_I[i],red T);
          "Currently reached states: ",reached;
          from I[i] = subst(new I[i],T,$);
   <u>"B</u>FS depth: ",i-2;
   'Final reachable states: ",reached;
```