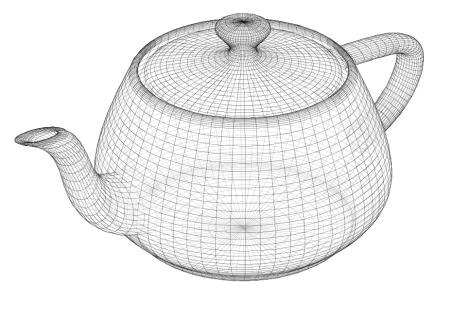
Orthographic Projection

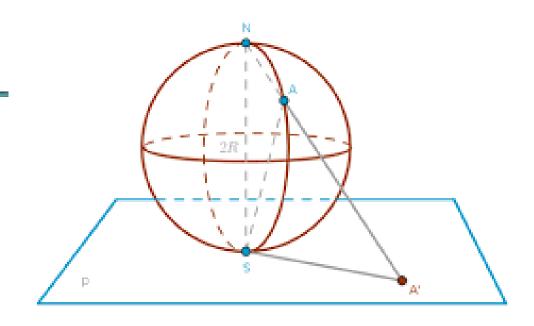


CS 418: Interactive Computer Graphics
Professor Eric Shaffer



Projections

In computer graphics, eventually we need to move from 3D space to 2D space



More accurately:

from 4D homogeneous coordinates to 3D homogeneous coordinates

A projection

is a transformation that maps from a high-dimensional space into a lower-dimensional space.

We will look at some common projections...and then we will discuss projection within WebGL



Planar Geometric Projections

Standard projections project onto a plane

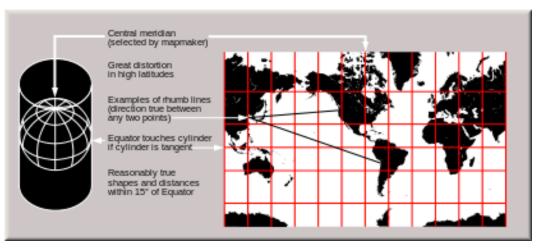
Projectors are lines that either

- converge at a center of projection
- are parallel

Such projections preserve lines

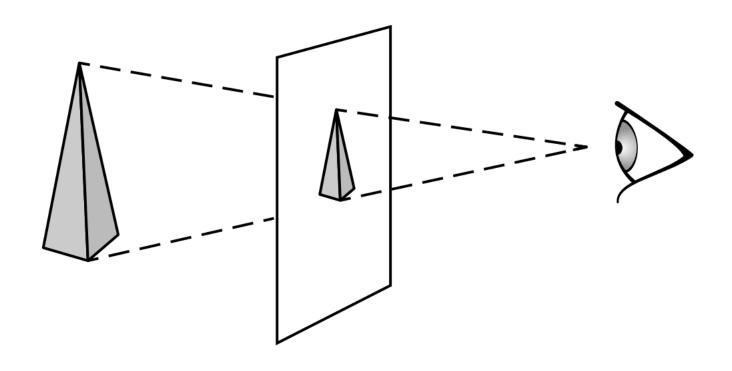
but not necessarily angles

Non-planar projections are often used in map construction



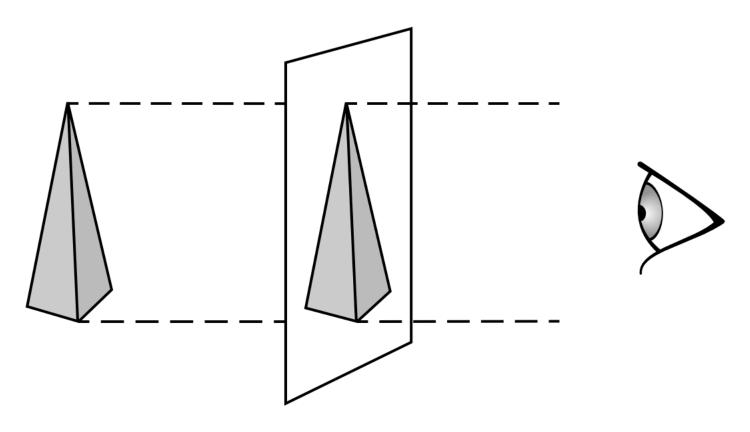


Perspective Projection





Orthographic Projection





Definition to Know: Foreshortening



Foreshortening is the visual effect or optical illusion that causes an object or distance to appear shorter than it actually is because it is angled toward the viewer.

i.e. projections squash receding surfaces

Can foreshortening happen in orthographic projection?

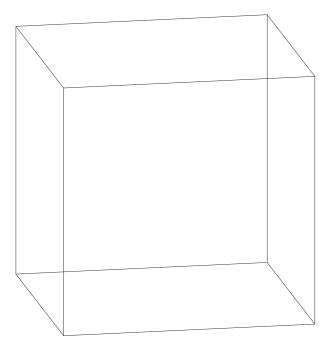
Andrea Mantegna
The Lamentation over
the Dead Christ

Clip Space View Volume

Before looking at projections in more detail...

...let's experimentally determine what the default view and view volume are.

So, if we don't do any transformations...where are we and what direction are we looking?



Take a look at

https://developer.mozilla.org/en-US/docs/Web/API/WebGL API/WebGL model view projection

http://jsfiddle.net/2x03hdc8/

It is a simple WebGL program that lets you draw rectangles

No transformations

By altering the rectangle coordinates, you can figure out the view....

Clip Space View Volume

Something new – the code enables hidden surface removal

```
// Tell WebGL to test the depth when drawing, so if a square is behind
// another square it won't be drawn
gl.enable(gl.DEPTH_TEST);
```

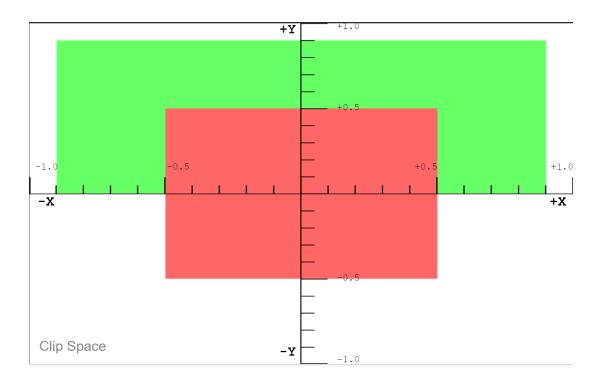
Side note - the overall code uses different conventions than used in our course (e.g. no glmatrix library)

So, probably don't base your assignments on this code

Clip Space View

- Red rectangle has z=0
- Green has z=0.5

What direction are we looking?

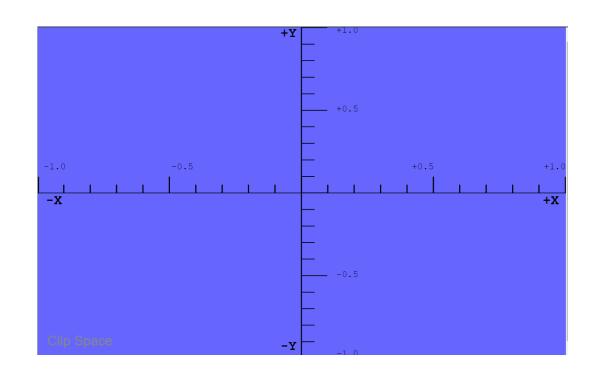


Clip Space View

We add a blue rectangle

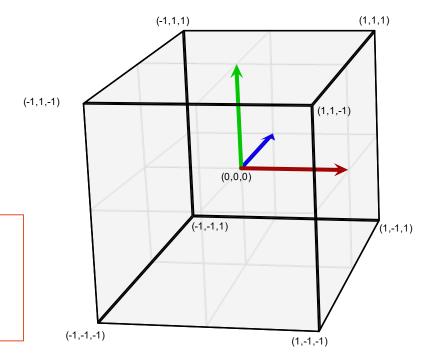
It's at z=-1

Where is the near clipping plane?



Clip Space View and View Volume

View is looking down Z+ Eyepoint is effectively at (0,0,-1) This is a left-handed coordinate system

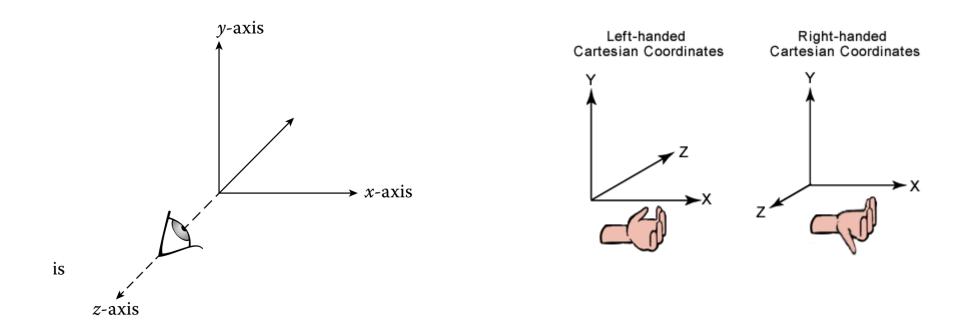


This is a little-known fact....

People often learn to use WebGL without ever learning this.

We'll see why in a few slides

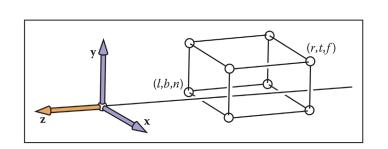
WebGL Style View

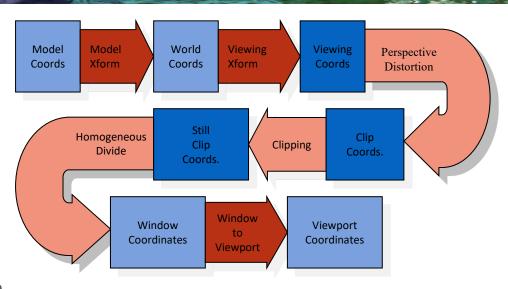


WebGL/OpenGL convention is to assume a right-handed world coordinate system

The *ortho* matrix is used to flip this coordinate system by scaling Z by -1 It then matches WebGL clip space

More WebGL Secrets





WebGL only performs an orthographic projection

- Everything is projected to the z=0 plane in the normalized view volume
- But you can distort your geometry to achieve a perspective projection

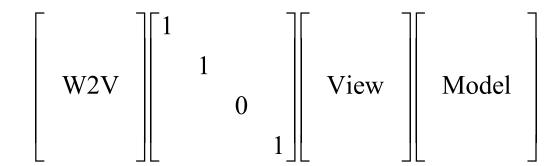
The projection occurs when the geometry is in clip space (NDC)

- Even then, depth information is kept around to do hidden surface removal
- Depth information means transformed z coordinates



Orthographic Projection

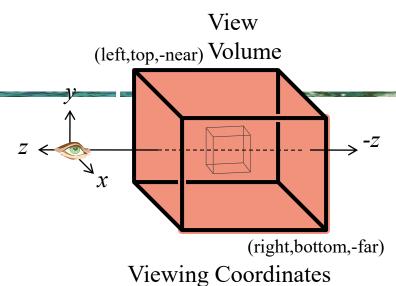
- Foreshortens
- No change in size by depth
- Classic Orthographic Projection matrix simply zeros the z-coordinate



mat4.ortho(out,left,right,bottom,top,near,far)

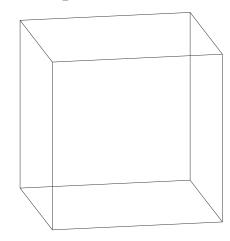
$$\begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{-2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 Does the ort matrix performance projection?

Does the ortho matrix perform a





Clip Coordinates

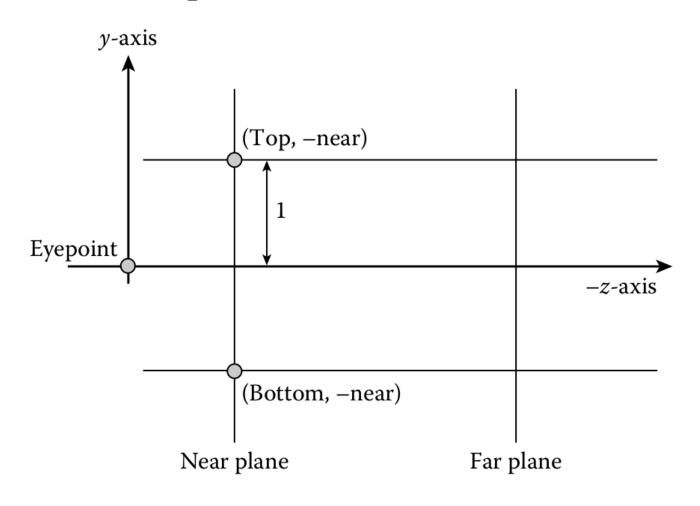




GLMatrix ortho matrix

ortho(left,right,bottom,top,near,far)

- near and far are distances
 down the -z axis from
 origin
- I,r,b,t are coordinates of the bounding planes
- what does the matrix do?



GLMatrix ortho matrix

ortho(left,right,bottom,top,near,far)

Imagine the eye is at (0,0,0) We look down the -z axis

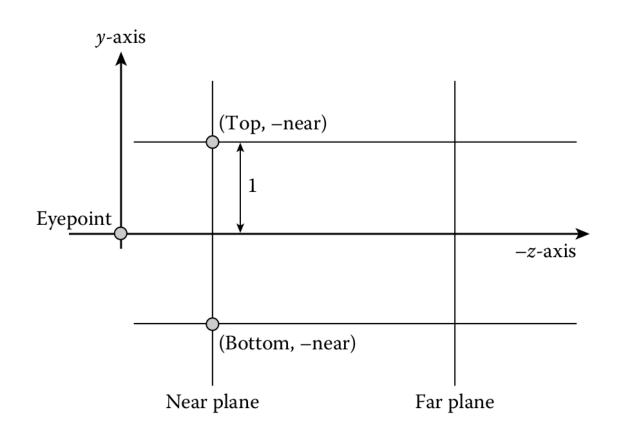
The view volume is:

[left, right] =[-1, 1] [bottom, top]=[-1, 1]

near =0

far = 2

What does the matrix look like?



GLMatrix ortho matrix

```
ortho(left,right,bottom,top,near,far)
```

Imagine the eye is at (0,0,0) We look down the -z axis

```
The view volume is:

[left, right] =[-1, 1]

[bottom, top]=[-1, 1]

near =0

far =2
```

Where does (0,0,0) get moved to? What else happens?

```
egin{bmatrix} 1 & 0 & 0 & 0 \ 0 & 1 & 0 & 0 \ 0 & 0 & -1 & -1 \ 0 & 0 & 0 & 1 \end{bmatrix}
```

In WebGL Code

In the vertex shader....