1 Representations

1.1 Source Language

```
statement ::= compound-statement
    if (expression) compound-statement else compound-statement
    while (expression) compound-statement
    for (statement; statement; statement) compound-statement
    qualifier type name;
    qualifier type name = expression;
    return expression;
    expression;
compound-statement ::= { statement* }
primary-expression ::= identifier
    constant
    string-literal
    (expression)
postfix-expression ::= primary-expression
    postfix-expression [expression]
    name (argument-list)
    postfix-expression ++
    postfix-expression --
unary-expression ::= postfix-expression
    ++ unary-expression
    -- unary-expression
    unary-operator postfix-expression
multiplicative-expression ::= unary-expression
    multiplicative-expression * unary-expression
    multiplicative-expression / unary-expression
    multiplicative-expression % unary-expression
additive-expression ::= multiplicative-expression
    additive-expression + multiplicative-expression
    additive-expression - multiplicative-expression
shift-expression ::= additive-expression
    shift-expression << additive-expression
    shift-expression >> additive-expression
relational-expression ::= shift-expression
    relational-expression < shift-expression
    relational-expression > shift-expression
```

```
relational-expression <= shift-expression
    relational-expression >= shift-expression
equality-expression ::= relational-expression
    equality-expression == relational-expression
    equality-expression != relational-expression
bitwise-and-expression ::= equality-expression
    and-expression & equality-expression
exclusive-or-expression ::= bitwise-and-expression
    exclusive-or-expression ^ bitwise-and-expression
bitwise-or-expression ::= exclusive-or-expression
   bitwise-or-expression | exclusive-or-expression
logical-and-expression ::= bitwise-or-expression
    logical-and-expression && bitwise-or-expression
logical-or-expression ::= logical-and-expression
 | logical-or-expression | logical-and-expression
conditional-expression ::= logical-or-expression
    conditional-expression? expression: conditional-expression
assignment-expression ::= conditional-expression
    unary-expression assignment-operator assignment-expression
expression ::= assignment-expression
parameter-list ::= qualifier type name, argument-list
 type-qualifier type name
argument-list ::= expression, argument-list
    expression
assignment-operator ::= = | *= | /= | %= | += | -=
unary-operator ::= * | - | ! | ~
type-qualifier ::= const | volatile
type-specifier ::= int | unsigned | char
type ::= type-qualifier type-specifier
function-definition ::= type name ( parameter-list ) compound-expression
```

2 Symbolic Execution

2.1 Metavariables

```
e - source language expressions c - source language statements s - symbolic expressions x, \alpha - names v - symbolic values
```

2.2 Symbolic Expressions

```
s ::= v \mid x
\mid s \text{ binop } s
\mid \text{ unop } s
\mid \text{ sel}(s, (s, ..., s))
\mid \text{ upd}(s, (s, ..., s), s)
\mid x(s, ..., s)
\mid s? : s : s
\mid \text{ NewArr } \tau
\tau ::= \text{Arr } \tau
\mid \text{ int8}
\mid \text{ int32}
\mid \text{ word32}
```

2.3 Symbolic State

```
\begin{split} S &= \langle g; \rho; \mu \rangle \\ g &\text{ - path condition} \\ \rho &\text{ - mapping of names to stack memory} \\ \mu &\text{ - mapping of names to heap memory} \end{split}
```

2.4 Expressions

$$\overline{\langle S;v\rangle \Downarrow \langle S;v\rangle} \text{ Literal }$$

$$\frac{\langle S;e\rangle \Downarrow S';s\rangle}{\langle S;-e\rangle \Downarrow \langle S';-s\rangle} \text{ Negate}$$

$$\frac{\langle S; e_1 \rangle \Downarrow S_1; s_1 \rangle \qquad \langle S_1; e_2 \rangle \Downarrow S_2; s_2 \rangle}{\langle S; e_1 + e_2 \rangle \Downarrow \langle S_2; s_1 + s_2 \rangle} \text{ Add}$$

$$\frac{\forall i \in 1..n, \langle S_i; e_i \rangle \Downarrow \langle S_{i+1}; s_i \rangle}{\langle S_1; x(e_1, ..., e_n) \rangle \Downarrow \langle S_{n+1}; x(s_1, ..., s_n) \rangle} \text{ FunCall}$$

2.5 Statements

$$\frac{\langle S;e\rangle \Downarrow \langle S';s\rangle}{\langle S;e;\rangle \Downarrow \langle S';0\rangle} \text{ Expression}$$

$$\frac{\forall i \in \{1..n\}. \langle S_k; c_i \rangle \Downarrow \langle S_{i+1}; s_{i+1} \rangle}{\langle S_1; \{c_1..c_n\} \rangle \Downarrow \langle S_{n+1}[\rho \mapsto \rho(S_1)]; s_{n+1} \rangle} \text{ CompoundStatement}$$

$$\frac{\langle S; e \rangle \Downarrow \langle S_1; g_1 \rangle \qquad \langle S_1[g \mapsto g(S_1) \land g_1]; c_1 \rangle \Downarrow \langle S_2; s_2 \rangle}{\langle S; \text{if } e \ c_1 \ \text{else} \ c_2 \rangle \Downarrow \langle S_2; 0 \rangle} \text{ If True}$$

$$\frac{\langle S;e\rangle \Downarrow \langle S_1;g_1\rangle \qquad \langle S_1[g\mapsto g(S_1) \land \neg g_1];c_2\rangle \Downarrow \langle S_2;s_2\rangle}{\langle S; \text{if } e \ c_1 \ \text{else} \ c_2\rangle \Downarrow \langle S_2;0\rangle} \text{ IfFalse}$$

2.6 Memory

$$\frac{x \in \text{dom } \rho(S) \qquad \rho(S)[x] = s}{\langle S; x \rangle \Downarrow \langle S; s \rangle} \text{ VAR}$$

$$\frac{\langle S;e\rangle \Downarrow \langle S';s\rangle \qquad \text{toOffset}(s) = (\text{ptr }\alpha + s_2) \qquad \rho(S')[\alpha] = s_1}{\langle S;*e\rangle \Downarrow \langle S'; \text{sel}(s_1,s_2)\rangle} \text{ DerefStack}$$

$$\frac{\langle S; e \rangle \Downarrow \langle S'; s \rangle \qquad \text{toOffset}(s) = (\text{ptr } \alpha + s_2) \qquad \mu(S')[\alpha] = s_1}{\langle S; *e \rangle \Downarrow \langle S'; \text{sel}(s_1, s_2) \rangle} \text{ Derefheap}$$

$$\frac{\rho(S_1)[x] = \operatorname{ptr} \ \alpha \qquad \rho(S_1)[\alpha] = s \qquad \forall i \in \{1..n\}. \langle S_i; e_i \rangle \Downarrow \langle S_{i+1}; s_i \rangle}{\langle S_1; x \, [e_1] \dots [e_n] \rangle \Downarrow \langle S_{i+1}; Sel(s, (s_1, ..., s_n)) \rangle} \text{ SelLocal}$$

$$\frac{\rho(S_1)[x] = \operatorname{ptr} \ \alpha \qquad \mu(S_1)[\alpha] = s \qquad \forall i \in \{1..n\}. \langle S_i; e_i \rangle \Downarrow \langle S_{i+1}; s_i \rangle}{\langle S_1; x \, [e_1] \, . \, [e_n] \rangle \Downarrow \langle S_{i+1}; Sel(s, (s_1, .., s_n)) \rangle} \text{ SelGlobal}$$

$$\frac{x \not\in \mathrm{dom}\ (\rho(S)) \qquad \mathrm{dim}(\tau) = 0}{\langle S; \tau \ x; \rangle \Downarrow \langle S[\rho \mapsto \rho[x \mapsto 0]]; 0 \rangle} \ \mathrm{DeclareLocal1}$$

$$\frac{x \not\in \text{dom }(\rho(S)) \quad \text{dim}(\tau) > 0 \quad \alpha \text{ is fresh}}{\langle S; \tau \ x; \rangle \Downarrow \langle S[\rho \mapsto \rho[x \mapsto \text{ptr } \alpha, \alpha \mapsto \text{NewArr } \tau]]; \text{ptr } \alpha \rangle} \text{ DeclareLocal2}$$

$$\frac{x \in \text{dom } (\rho(S)) \quad \langle S; e \rangle \Downarrow \langle S'; s \rangle}{\langle S; x = e; \rangle \Downarrow \langle S'[\rho \mapsto \rho[x \mapsto s]]; s \rangle} \text{ AssignLocal}$$

$$\frac{\rho(S_1)[x] = \operatorname{ptr} \alpha \qquad \rho(S_1)[\alpha] = s \qquad \forall i \in \{1..n\}. \langle S_i; e_i \rangle \Downarrow \langle S_{i+1}; s_i \rangle \qquad \langle S_{n+1}; e_v \rangle \Downarrow \langle S'; s' \rangle}{\langle S_1; x \llbracket e_1 \rrbracket \ldots \llbracket e_n \rrbracket = e_v \rangle \Downarrow \langle S'[\rho \mapsto \rho(S')[\alpha \mapsto \operatorname{upd}(s, (s_1, .., s_n), s')]]; s' \rangle} \text{ UPDLOCAL}$$

$$\frac{\rho(S_1)[x] = \operatorname{ptr} \ \alpha \qquad \mu(S_1)[\alpha] = s \qquad \forall i \in \{1..n\}. \langle S_i; e_i \rangle \Downarrow \langle S_{i+1}; s_i \rangle \qquad \langle S_{n+1}; e_v \rangle \Downarrow \langle S'; s' \rangle}{\langle S_1; x \llbracket e_1 \rrbracket \ldots \llbracket e_n \rrbracket \ = \ e_v \rangle \Downarrow \langle S'[\mu \mapsto \mu(S')[\alpha \mapsto \operatorname{upd}(s, (s_1, ..., s_n), s')]]; s' \rangle} \text{ UpdGlobal }$$

$$\frac{\rho(S)[x] = s}{\langle S; +\!\!\!+\!\!\!+ x\rangle \Downarrow \langle S[\rho \mapsto \rho(S)[x \mapsto s+1]]; s+1\rangle} \text{ IncPreLocal}$$

$$\frac{\rho(S)[x] = s}{\langle S; x + + \rangle \Downarrow \langle S[\rho \mapsto \rho(S)[x \mapsto s + 1]]; s \rangle} \text{ IncPostLocal}$$