Implementing Space-Time A*

1.1.

```
Start locations
Goal locations
@ @ @ @ @ @
0 . . . 1 0 0
0 0 0 . 0 0 0
<u>a</u> a a a a a
***Run Independent***
 Found a solution!
CPU time (s):
                 0.00
Sum of costs:
                 6
***Test paths on a simulation***
COLLISION! (agent-agent) (0, 1) at time 3.4
COLLISION! (agent-agent) (0, 1) at time 3.5
COLLISION! (agent-agent) (0, 1) at time 3.6
COLLISION! (agent-agent) (0, 1) at time 3.7
COLLISION! (agent-agent) (0, 1) at time 3.8
COLLISION! (agent-agent) (0, 1) at time 3.9
COLLISION! (agent-agent) (0, 1) at time 4.0
COLLISION! (agent-agent) (0, 1) at time 4.1
COLLISION! (agent-agent) (0, 1) at time 4.2
COLLISION! (agent-agent) (0, 1) at time 4.3
COLLISION! (agent-agent) (0, 1) at time 4.4
COLLISION! (agent-agent) (0, 1) at time 4.5
COLLISION! (agent-agent) (0, 1) at time 4.6
```

```
Start locations
Goal locations
@ @ @ @ @ @ @
@ . . . 1 0 @
***Run Prioritized***
 Found a solution!
CPU time (s):
                 0.00
Sum of costs:
                 6
[[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4)]]
***Test paths on a simulation***
COLLISION! (agent-agent) (0, 1) at time 3.4
COLLISION! (agent-agent) (0, 1) at time 3.5
COLLISION! (agent-agent) (0, 1) at time 3.6
COLLISION! (agent-agent) (0, 1) at time 3.7
COLLISION! (agent-agent) (0, 1) at time 3.8
COLLISION! (agent-agent) (0, 1) at time 3.9
COLLISION! (agent-agent) (0, 1) at time 4.0
COLLISION! (agent-agent) (0, 1) at time 4.1
COLLISION! (agent-agent) (0, 1) at time 4.2
COLLISION! (agent-agent) (0, 1) at time 4.3
COLLISION! (agent-agent) (0, 1) at time 4.4
COLLISION! (agent-agent) (0, 1) at time 4.5
COLLISION! (agent-agent) (0, 1) at time 4.6
```

```
Found a solution!
Sum of costs: 14
[[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 4), (1, 5), (1, 4), (1, 5), (1, 4), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4)]]
***Test paths on a simulation***
COLLISION! (agent-agent) (0, 1) at time 3.4 COLLISION! (agent-agent) (0, 1) at time 3.5
                                               (agent-agent) (0, 1) at time 3.5 (agent-agent) (0, 1) at time 3.6 (agent-agent) (0, 1) at time 3.7 (agent-agent) (0, 1) at time 3.8 (agent-agent) (0, 1) at time 3.9 (agent-agent) (0, 1) at time 4.0 (agent-agent) (0, 1) at time 4.1 (agent-agent) (0, 1) at time 4.2 (agent-agent) (0, 1) at time 4.3 (agent-agent) (0, 1) at time 4.4 (agent-agent) (0, 1) at time 4.4 (agent-agent) (0, 1) at time 4.5
  COLLISION!
COLLITSTON!
   OLLISION!
COLLISION!
   OLLISION!
COLLISION!
  COLLISION!
                                                 (agent-agent) (0, 1) at time 4
(agent-agent) (0, 1) at time 4
(agent-agent) (0, 1) at time 5
COLLISION!
  COLLISION!
                                                 (agent-agent) (0, 1) at time (agent-agent) (0, 1) at time (agent-agent) (0, 1) at time
  COLLISION!
                                             (agent-agent) (0, 1) at time 5.5 (agent-agent) (0, 1) at time 5.6 (agent-agent) (0, 1) at time 5.7 (agent-agent) (0, 1) at time 5.8 (agent-agent) (0, 1) at time 5.9 (agent-agent) (0, 1) at time 6.0 (agent-agent) (0, 1) at time 6.0 (agent-agent) (0, 1) at time 6.1 (agent-agent) (0, 1) at time 6.3 (agent-agent) (0, 1) at time 6.4 (agent-agent) (0, 1) at time 6.6 (agent-agent) (0, 1) at time 6.6 (agent-agent) (0, 1) at time 7.4 (agent-agent) (0, 1) at time 7.4 (agent-agent) (0, 1) at time 7.6 (agent-agent) (0, 1) at time 7.6 (agent-agent) (0, 1) at time 7.7 (agent-agent) (0, 1) at time 7.7 (agent-agent) (0, 1) at time 7.8 (agent-agent) (0, 1) at time 8.0 (agent-agent) (0, 1) at time 8.0 (agent-agent) (0, 1) at time 8.1 (agent-agent) (0, 1) at time 8.1 (agent-agent) (0, 1) at time 8.2 (agent-agent) (0, 1) at time 8.3 (agent-agent) (0, 1) at time 8.6 (agent-agent) (0, 1) at time 8.6 (agent-agent) (0, 1) at time 9.7 (agent-agent) (0, 1) at time 9.8 (agent-agent) (0, 1) at time 9.4 (agent-agent) (0, 1) at time 9.4 (agent-agent) (0, 1) at time 9.6 (agent-agent) (0, 1) at time 9.7 (agent-agent) (0, 1) at time 9.9 (agent-agent) (0, 1) at time 9.7 (agent-agent) (0, 1) at time 9.9 (agent-agent) (0, 1) at time 10.0 (agent-a
 COLLISION!
  COLLISION!
COLLISION!
   OLLISION!
  COLLISION!
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COLLISION!
COLLISION!
COLLISION!
  COLLISION!
COLLISION!
COLLITSTON!
COLLITSTON!
 COLLISION!
                                                                                                              (0, 1) at time 11.3
(0, 1) at time 11.4
(0, 1) at time 11.5
                                                  (agent-agent)
                                                 (agent-agent)
(agent-agent)
  COLLISION!
    OLLISION!
                                                                                                              (0, 1) at time 11.6
(0, 1) at time 11.7
(0, 1) at time 11.8
                                                  (agent-agent)
                                                 (agent-agent)
(agent-agent)
  COLLISION!
    OLLISION!
                                                                                                              (0, 1) at time 11.9
(0, 1) at time 12.0
(0, 1) at time 12.1
                                                 (agent-agent)
(agent-agent)
(agent-agent)
COLLISION!
    OLLISION!
  COLLISION! (agent-agent) (0, 1) at time 12.1 COLLISION! (agent-agent) (0, 1) at time 12.2 COLLISION! (agent-agent) (0, 1) at time 12.3 COLLISION! (agent-agent) (0, 1) at time 12.4 COLLISION! (agent-agent) (0, 1) at time 12.6 COLLISION! (agent-agent) (0, 1) at time 12.6 COLLISION! (agent-agent) (0, 1) at time 12.7
COLLISION!
```

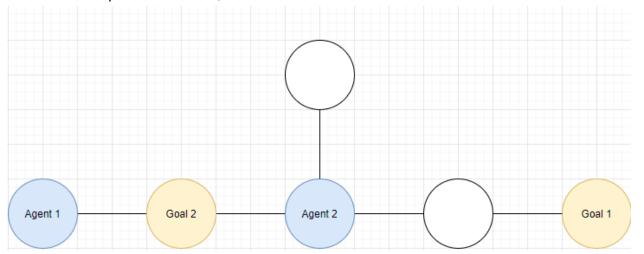
- 1.4. Agent 0 at time step 10 is on its goal. I made a lower bound using the timesteps given in the constraints. If there are constraints, I set my lower bound variable "earliest_goal_timestep" to the max timestep in the constraint table with the assumption that the solution path accounts for all obstacles. As long as the goal path time is ≥ earliest_goal_timestep we can assume the found path has avoided all obstacles. If there are no constraints, we set the lowerbound to 0.
- 1.5. The set of constraints set to achieve a proper solution is the following:

{'agent': 1,'loc': [(1,3),(1,4)],'timestep': 2} {'agent': 1,'loc': [(1,3)],'timestep': 2} {'agent': 1,'loc': [(1,3),(1,2)],'timestep': 2}

Implementing Prioritized Planning

2.3. Yes, it reported back with No Solutions as shown below:

2.5. Here is an MAPF instance which prioritized planning does not find an (optimal or suboptimal) collision-free solution for a given ordering of the agents. This can only be solved with priority 1 > 2, but if we switch the priorities to 2 > 1, it cannot solve it.



Implementing Conflict-Based Search (CBS)

3.3. Here is the transcript:

```
Start locations
 Goal locations
 ***Run CBS***
Generate node 0
 Expand node 0
 Expanding node {'cost': 6, 'constraints': [], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, 'loc': [(1, 4)], 'timestep': 3}]}
Generate node 1
 Generate node 2
Expanding node { 'cost': 7, 'constraints': [{'agent': 0, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, 'loc': [(1, 4)], 'timestep': 4}]}
  enerate node
 Generate node 4
Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4), (1, 3), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, 'loc': [(1, 3), (1, 4)], 'timestep': 3}]}

Generate node 5
 Generate node 6
 expand node 3
 Expanding node {'cost': 8, 'constraints': [{'agent': 0, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 0, 'loc': [(1, 4)], 'timestep': 4, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 3), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, 'loc': [(1, 4)], 'timestep': 5}]}
 Generate node 8
 Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 4), (1, 3)], 'timestep': 3, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 3), (1, 3), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, 'loc': [(1, 3)], 'timestep': 2}]}

Generate node 9
Expand node 10

Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 4), (1, 3)], 'timestep': 2, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4), (1, 5), (1, 4)]], 'collisions': [{'a1': 0, 'a2': 1, Generate node 11
 Generate node 12
 expand node 12
 Expand node 12

Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 4), (1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 5), (1, 4)], 'timestep': 4, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (1, 4), (1, 5)], 'timestep': 2}]}
 Generate node 13
Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 3), (1, 2)], 'timestep': 2, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 2), (1, 2), (1, 3), (1, 4)]], 'collisions' [{'a1': 0, 'a2': 1, 'loc': [(1, 2)], 'timestep': 1}]}

Generate node 15

Generate node 15

Generate node 15
  enerate node 16
 expand node 16
Expanding node 16

Expanding node {'cost': 8, 'constraints': [{'agent': 1, 'loc': [(1, 4)], 'timestep': 3, 'positive': False}, {'agent': 1, 'loc': [(1, 4), (1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 3)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 5), (1, 4)], 'timestep': 4, 'positive': False}, {'agent': 1, 'loc': [(1, 3), (1, 2)], 'timestep': 2, 'positive': False}, {'agent': 1, 'loc': [(1, 2)], 'timestep': 1, 'positive': False}], 'paths': [[(1, 1), (1, 2), (1, 3), (1, 4), (1, 5)], [(1, 2), (1, 3), (2, 3), (1, 3), (1, 4)]], 'collisions': []}
  Found a solution!
 CPU time (s):
                                          0.01
 Sum of costs:
 xpanded nodes: 9
  enerated nodes: 17
  **Test paths on a simulation***
```

Implementing CBS with Disjoint Splitting

4.3. With standard splitting my implementation generated 29 nodes, expanding 15, with a sum of costs at 10. Disjoint splitting generated 5 nodes, expanding 5 nodes, with a sum of costs at 10 as well. Below is a picture of the output for disjoint splitting:

```
***Import an instance***
Start locations
@ @ @ @ @ @
 . 1 . . . @
            @
 Goal locations
0 0 0 0 0 0
 . . . . . @
           99
 . . . 1 . @
@ @ @ @ @ @
@ @ @ @ @
***Run CBS***
Generate node 0
Expand node 0
Running Disjoint Splitting
Generate node 1
Expand node 1
Running Disjoint Splitting
Generate node 2
Expand node 2
Running Disjoint Splitting
Generate node 3
Expand node 3
Running Disjoint Splitting
Generate node 4
Expand node 4
Found a solution!
CPU time (s):
                 0.00
Sum of costs:
                 10
Expanded nodes: 5
Generated nodes: 5
***Test paths on a simulation***
```