

VIT UNIVERSITY

APPLICATIONS OF DIFFERENTIAL EQUATIONS

MAT2002

experiment-10

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1. Solve the difference equation $y_{n+2} - y_{n+1} - y_n = 0; y_0 = 0; y_1 = 1$ using Matlab code

CODE:

```
clc
clear all
syms n k1 k2 m
assume(n,'integer')
a=input('Enter the coefficient of y(n+2):');
b=input('Enter the coefficient of y(n+1):');
c=input('Enter the coefficient of y(n):');
g=input('Enter the coefficient of non-homogenous part:');
r=subs(solve(a*m^2+b*m+c,m));
if imag(r)~=0
    rho=sqrt(real(r(1))^2+imag(r(1))^2);
    theta=atan(abs(imag(r(1)))/real(r(1)));
    y1=(rho^n)*cos(n*theta);
    y2=(rho^n)*sin(n*theta);
elseif r(1)==r(2)
    y1=r(1)^n;
    y2=n*r(1)^n;
else
    y1=r(1)^n;
    y2=r(2)^n;
end
Co=det([y1,y2;subs(y1,n,n+1),subs(y2,n,n+1)]);
%Casoratian of the solutions
y_c=k1*y1+k2*y2;
disp('Complementary Solution is :');
disp(y_c);
if(g~=0)
    y11=subs(y1,n,n+1);
    y21=subs(y2,n,n+1);
    Co1=subs(Co,n,n+1);
    u1=simplify(symsum(-g*y21/Co1,n))
    u2=simplify(symsum(g*y11/Co1,n))
    y_p=simplify(u1*y1+u2*y2);
    y=y_c+y_p;
else
    y=y_c;
end
check=input('If the problem has initial conditions then enter 1 else 0:');
if(check==1)
```

```

yval1=input('Enter the initial condition at n=0:');
yval2=input('Enter the initial condition at n=1:');
cond1=strcat(char(subs(y,n,0)), '=',num2str(yval1));
cond2=strcat(char(subs(y,n,1)), '=',num2str(yval2));
[k1,k2]=solve(cond1,cond2);
y=subs(y);
end
disp(collect(collect(y,y1),y2))
if(check~=0)
    nrange=0:10;
    Y=subs(y,n,nrange);
    stem(nrange,Y);
    set(gca,'XTick',linspace(0,10,11))
    xlabel('n');
    ylabel('y(n)');
end

```

1. Solve the difference equation $y_{n+2} - y_{n+1} - y_n = 0; y_0 = 0; y_1 = 1$ using Matlab code

INPUT:

Enter the coefficient of $y(n+2)$:1
Enter the coefficient of $y(n+1)$:-1
Enter the coefficient of $y(n)$:-1
Enter the coefficient of non-homogenous part:0

If the problem has initial conditions then enter 1 else 0:1

Enter the initial condition at $n=0$:0

Enter the initial condition at $n=1$:1

OUTPUT:

Complementary Solution is :

$k1*(1/2 - 5^{(1/2)}/2)^n + k2*(5^{(1/2)}/2 + 1/2)^n$

Y=

$(5^{(1/2)}/5)*(5^{(1/2)}/2 + 1/2)^n + (-5^{(1/2)}/5)*(1/2 - 5^{(1/2)}/2)^n$

Command Window

```

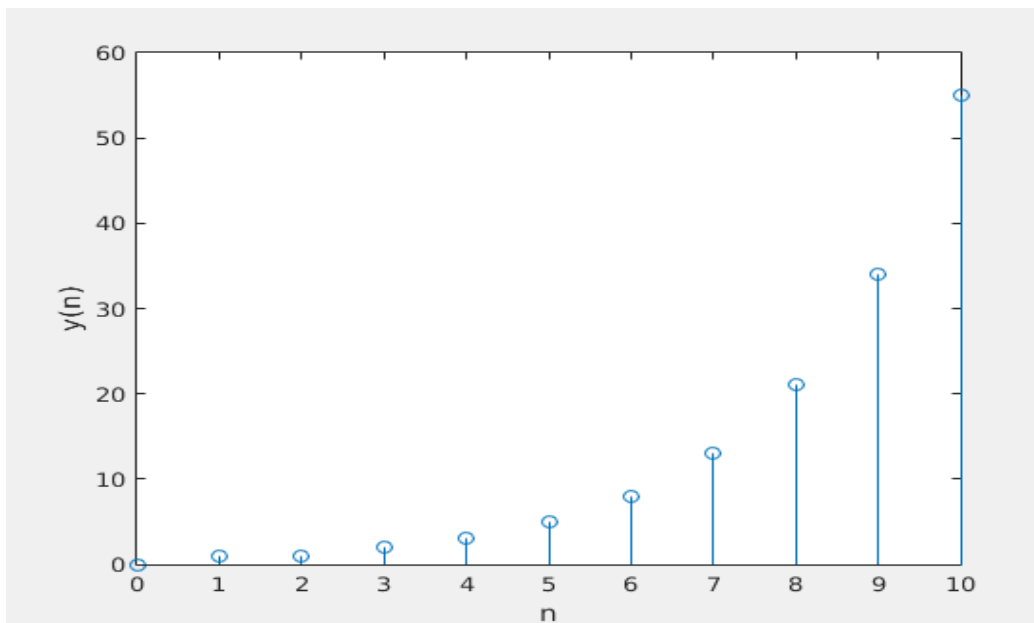
Enter the coefficient of y(n+2):1
Enter the coefficient of y(n+1):-1
Enter the coefficient of y(n):-1
Enter the coefficient of non-homogenous part:0
Complementary Solution is :
k1*(1/2 - 5^(1/2)/2)^n + k2*(5^(1/2)/2 + 1/2)^n

If the problem has initial conditions then enter 1 else 0:1
Enter the initial condition at n=0:0
Enter the initial condition at n=1:1
(5^(1/2)/5)*(5^(1/2)/2 + 1/2)^n + (-5^(1/2)/5)*(1/2 - 5^(1/2)/2)^n

```

 >>

GRAPH:



2. Solve the difference equation $y_{n+2} + 6y_{n+1} + 8y_n = 0$; $y_0 = 0$; $y_1 = 1$ using Matlab code

INPUT:

Enter the coefficient of $y(n+2)$:1

Enter the coefficient of $y(n+1)$:6

Enter the coefficient of $y(n)$:8

Enter the coefficient of non-homogenous part:0

If the problem has initial conditions then enter 1 else 0:1

Enter the initial condition at $n=0$:0

Enter the initial condition at $n=1$:1

OUTPUT:

Complementary Solution is :

$$(-2)^n k_2 + (-4)^n k_1$$

Y=

$$(-2)^{n/2} - (-4)^{n/2}$$

GRAPH:

