The Challenge:

For this Assignment, in a group of 3, you need to collect data and then build a model to predict price of a player IPL 2018 auction.

Training Data:

For training you need to collect numbers and statistics for at least 40 players. Your target (dependent variable)should be price. Typical independent variables include but not limited to International T20 Matches Played, ODI, Matches Played, Strike rates – batting, bowling etc.

Testing Data:

Test your model for each match in IPL 2018 auction data.

Data collection:

Data is collected from 3 websites:

- Wikipedia
- Howstat
- ipltickets.net

Data from Wikipedia is collected manually which contains list of all the players base price and sold out price from 2008 to 2017. The sold out and base price data of 2018 is scraped from ipltickets.net using R. Auction data(prices) are converted from \$(Dollar) to ₹(Rupee), converted into Net Present Value and then took the average of all the prices listing from 2008 to 2017.

The method of extracting data from websites is known as web scraping. Rvest is a package present in R language that is used to scrape data from html web pages. Web scraping packages can access the world wide web using Hypertext Transfer Protocol(HTTP) or through a web browser. Web pages are build using HTML or XHTML(text based mark-up languages). To extract particular type of data, HTML/CSS tags are required. Selector Gadget, an open source tool present in chrome extension, that makes CSS selector generation and discovery in a much easier way from complex websites.

Data Visualization:

Total of 48 players data is extracted from the website howstat and stored in excel file with each players data in each excel file. The whole extracted data is put together in one excel file with player names as rows and Variables in column which is done manually. There are 108 decision variables which are contributing to the output. All the categorical data(factors) is converted to numerical so that it can contribute to the model. For example, all the batsmen playing with left hand are assigned value of 1 and the batsmen playing with right hand are assigned a value of 2. Similar concept is applied to bowlers. All the non-filled values are given value 0 and all the NAs are converted to numerical.

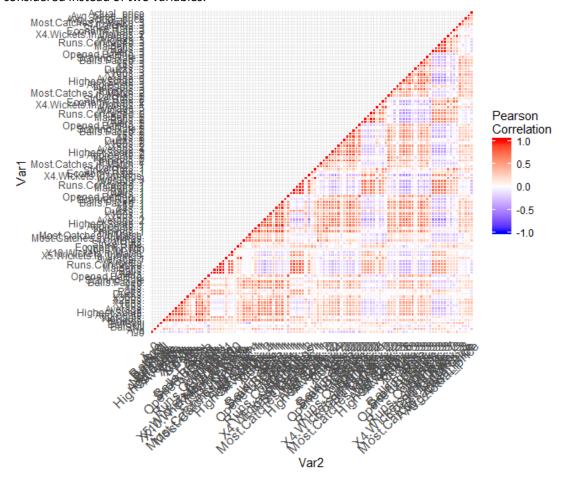
The 108 decision variables are PlayerName, DateofBirth, Age, BatSkill, BallSkill, Innings., Not.Outs., Aggregate., Highest.Score., Average., X50s., X100s., X200s., X300s., Ducks., Pairs., X4s., X6s., Balls.Faced., Scoring.Rate, Opened.Batting., Overs., Balls., Maidens., Runs.Conceded., Wickets., Average..1, X5.Wickets.in..Innings., X10.Wickets.in.Match., Best...Innings., Best...Match., None.for.100, Economy.Rate., Strike.Rate., Catches., Most.Catches.in.Innings., Most.Catches.in.Match., Innings..1, Not.Outs..1, Aggregate..1, Highest.Score..1, Average..2, X50s..1, X100s..1, Ducks..1, X4s..1, X6s..1, Balls.Faced..1, Scoring.Rate.1, Opened.Batting..1, Overs..1, Balls..1, Maidens..1, Runs.Conceded..1, Wickets..1, Average..3, X4.Wickets.in.Innings., Best., Economy.Rate..1, Strike.Rate..1, Catches..1, Most.Catches.in.Match..1, Innings..2, Not.Outs..2, Aggregate..2, Highest.Score..2, Average..4, X50s..2, X100s..2, Ducks..2, X4s..2, X6s..2, Balls.Faced..2, Scoring.Rate.2, Opened.Batting..2, Overs..2, Balls..2, Maidens..2, Runs.Conceded..2, Wickets..2, Average..5, X4.Wickets.in.Innings..1, Best..1, Economy.Rate..2, Strike.Rate..2, Catches..2, Most.Catches.in.Match..2, Innings..3, Not.Outs..3, Aggregate..3, Highest.Score..3, Average..6, X50s..3, X100s..3, Ducks..3, X4s..3, X6s..3, Balls.Faced..3, Scoring.Rate.3, Opened.Batting..3, Overs..3, Balls..3, Maidens..3, Runs.Conceded..3, Wickets..3, Average..7, X4.Wickets.in.Innings..2, Best..2,

Economy.Rate..3, Strike.Rate..3, Catches..3, Most.Catches.in.Match..3, Avg_actual_price, Avg_base_price, Actual_price.

The above data consists of information of the 48 players in all formats(Test, ODI, T20, IPL). Data of other league matches and domestic matches are not considered.

In the collected data, number of variables are more than the data collected which causes overfitting. So, to cut down the number of variables which were used for building the model, we searched for the dependencies and removed the unwanted columns. This can be determined from correlation matrix.

If the correlation between the two different variables is nearly equals one, then one variable is considered instead of two variables.



In the above figure, red colour indicates positive correlation and blue colour indicates negative correlation.

Considering correlation values which have values >0.95, this method is applied and the total number of variables are reduced to 89 variables. Then removing unwanted variables which contains almost all zeros or don't contribute to the output, It got reduced to 81 variables.

Building the Model, Results and Inferences:

After Collecting the Data and Pre processing it we have removed some unwanted variables even though fitting a linear model is not possible because:

1. Number of Variables > Number of Observations

so we cannot obtain adjusted R-square value for our model. To solve this problem we have to perform some feature selection methods such as Regularization

- 2. Subset Selection: identify a subset of predictors that strongly related to the response
 - 1. Best Subset Selection
 - 2. Stepwise Selection Forward Stepwise Selection; Hybrid Approaches
 - 3. Choosing the Optimal Model
 Cp, AIC, BIC, and Adjusted R2; Validation and Cross-Validation
- 3. **Shrinkage**: fit a model using all predictors by shrinking estimated coefficients towards zero to reduce variance. :**LASSO and Ridge Regression**
- Dimension Reduction: projecting the predictors(p) into a M dimensional subspace (M < p)
 :PCR and PLS

EXPLANATION:

1. Best Subset Selection:

There are total 81 variables after Data pre-processing and feature selection through Correlation Matrix.

INFERENCES: so it does an exhaustive search of 2^{81} possibilities as it was too large and takes more time

- 2. Stepwise Selection
 - Forward Stepwise Selection:

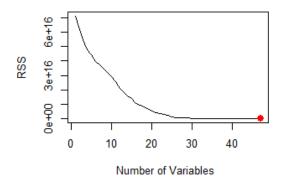
and Adjusted R-square Values and plotted the graphs shown below.

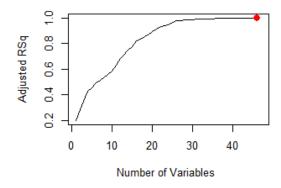
There are total 81 variables so somewhat forward selection is possible and sub-optimal compared to best-subset selection. I imported these four libraries MASS, ISLR, glmnet and leaps after I fitted my forward sub selection method to my data. The **Results** of my R squared value are:

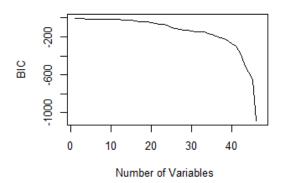
- [1] 0.2120351 0.3151020 0.3919882 0.4738682 0.5090502 0.5586925
- [7] 0.5843036 0.6134438 0.6451065 0.6739357 0.7167053 0.7637360
- [13] 0.7907350 0.8247233 0.8447335 0.8803454 0.8961865 0.9079563
- [19] 0.9199496 0.9392874 0.9520649 0.9625301 0.9677878 0.9743806
- [25] 0.9853158 0.9897711 0.9919145 0.9934025 0.9945347 0.9956926
- [31] 0.9962351 0.9968322 0.9972454 0.9979951 0.9984251 0.9990650
- [37] 0.9993750 0.9995630 0.9997386 0.9998639 0.9999258 0.9999864 [43] 0.9999988 0.9999998 1.0000000 1.0000000 1.0000000

INFERENCES : Around the value of 47 variable my R-square is one. Then I caluculated Cp ,AIC, BIC

Results: The value for no. of variables to be selected with respect to RSS, Adj-Rsq ,AIC, BIC are 46,47,47,47







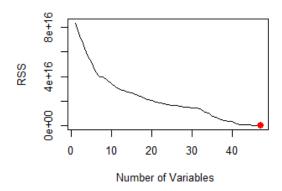
• Backward Stepwise Selection:

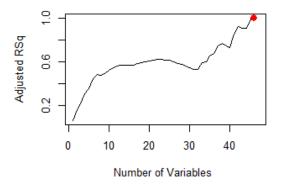
There are total 81 variables so somewhat forward selection is possible and sub-optimal compared to best-subset selection. I imported these four libraries MASS, ISLR, glmnet and leaps.after I fitted my forward sub selection method to my data. The **Results** of my R squared value are:

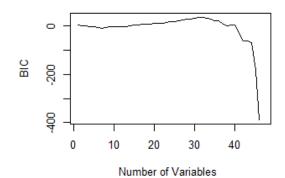
- [1] 0.07549438 0.19059802 0.26105340 0.36398809 0.42176749 0.51227930 0.55 811232 0.56341333 0.58844882 0.62317512 0.64917184 0.67082237
- [13] 0.68369024 0.69298204 0.70281065 0.71559091 0.73330893 0.74745732 0.7 6090538 0.77357731 0.78598367 0.79638026 0.80515193 0.81194089
- [25] 0.81721418 0.81941688 0.82305436 0.82819557 0.83225888 0.83615819 0.8 4019996 0.85042134 0.87663834 0.88795410 0.91104193 0.92313541
- [37] 0.94525115 0.95476606 0.95676101 0.95936791 0.98055137 0.99117147 0.9 9182551 0.99373246 0.99944547 0.99999318 1.00000000

INFERENCES: Around the value of 47 variable my R-square is one. Then I caluculated Cp ,AIC, BIC and Adjusted R-square Values and plotted the graphs shown below.

Results : The value for no. of variables to be selected with respect to RSS, Adj-Rsq ,AIC, BIC are 46,47,47,47







The coefficients for Forward Selection are :

(Intercept)	Age	BatSkill	Not.Outs.	Average.
3.599193e+08	-1.313532e+07	1.896013e+06	-4.977653e+06	-9.893500e+05
X100s.	X200s.	Ducks.	X4s.	X5.Wickets.inInnings.
7.016832e+05	-1.072329e+07	4.586512e+06	2.149855e+05	1.269615e+06
Catches.	Most.Catches.in.Match.	Innings1	Aggregate1	X100s1
5.207062e+05	5.417648e+06	-7.384170e+05	2.102876e+04	1.630994e+06
X4s1	X6s1	Scoring.Rate.1	Balls1	Wickets1
-1.990923e+05	-3.019331e+04	3.585931e+05	-1.719196e+04	8.511551e+05
X4.Wickets.in.Innings.	Catches1	Most.Catches.in.Match1	Innings2	Not.Outs2
-4.418767e+04	1.972435e+05	-6.379551e+06	2.911570e+05	4.851188e+06
Highest.Score2	X100s2	Ducks2	X4s2	Scoring.Rate.2
7.525621e+04	2.430669e+07	-7.774533e+06	5.326568e+04	4.892544e+04
Balls2	Maidens2	X4.Wickets.in.Innings1	Catches2	Most.Catches.in.Match2
5.226780e+03	-7.282122e+04	-1.346415e+03	-1.948616e+06	-2.508181e+07
Aggregate3	X50s3	X100s3	Ducks3	X4s3
-9.231417e+04	-3.118612e+04	-2.430973e+06	2.599360e+06	7.042428e+05
X6s3	Balls.Faced3	Opened.Batting3	X4.Wickets.in.Innings2	Strike.Rate3
1.877267e+05	6.159030e+04	-9.241382e+05	1.219648e+07	-2.247826e+05
Catches3	Avg_actual_price	Avg_base_price		
1.339555e+06	1.004284e+00	-5.867239e-01		

The coefficients for backward Selection are:

(Intercept)	Age	BatSkill	Ballskill	Innings.	Not.Outs.
-1112595763.1	49630645.5	-142226860.6	81065344.7	-116579080.1	90891749.2
Aggregate.	Highest.Score.	Average.	X100s.	X200s.	X300s.
4344493.9	2450587.0	2805858.5	-306723931.9	-566805011.4	-970708324.7
Ducks.	X4s.	X6s.	Scoring.Rate	Balls.	Maidens.
192723139.9	-13738818.5	74242481.8	-4764862.3	247201.8	-11534232.2
Wickets.	Average1	X5.Wickets.inInnings.	Economy.Rate.	Strike.Rate.	Catches.
1672651.0	-36524155.6	30548414.9	-210736407.9	18248667.8	-9260092.4
Most.Catches.in.Innings.	Most.Catches.in.Match.	Innings1	Aggregate1	Highest.Score1	X50s1
642331497.0	-275506984.4	193150.3	-228504.2	-11607630.1	-39781153.3
X100s1	X4s1	X6s1	Scoring.Rate.1	Balls1	Wickets1
82103701.9	2744258.9	-11700832.1	7273064.2	256372.4	4788908.2
X4.Wickets.in.Innings.	Economy.Rate1	Strike.Rate1	Catches1	Most.Catches.in.Match1	Innings2
-161176571.4	77560974.4	-1057449.0	9315293.9	-192311522.5	-24313447.5
Not.Outs2	Aggregate2	Highest.Score2	X100s2	Ducks2	X4s2
-3093897.8	1369684.6	2969598.5	-387271042.1	-277657217.7	11424988.7

Choosing the Optimal Model

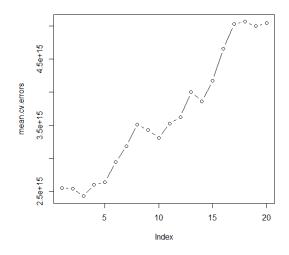
RESULTS:

Now we performed validation and cross validation Validation errors for Forward Model:

```
[1] 1.888615e+15 3.037862e+15 3.037862e+15 3.426095e+15 3.424984e+15 [6] 2.570951e+15 2.957942e+15 2.894986e+15 3.604158e+15 5.093671e+15 [11] 5.163444e+15 4.480094e+15 4.526668e+15 4.397623e+15 4.595657e+15 [16] 4.658251e+15 4.489039e+15 4.871431e+15 4.895542e+15 4.999805e+15
```

Cross Validation errors for Forward Model:

```
2.558191e+15 2.550505e+15 2.432548e+15 2.603644e+15 2.646736e+15
                                      8
                                                   9
                                                                10
2.949860e+15 3.189391e+15 3.514536e+15 3.429724e+15 3.315093e+15
          11
                       12
                                     13
                                                  14
                                                                15
3.530362e+15 3.622608e+15 4.002320e+15 3.865699e+15 4.172183e+15
          16
                       17
                                     18
                                                  19
                                                                20
4.655979e+15 5.028398e+15 5.062948e+15 4.997043e+15 5.040219e+15
```

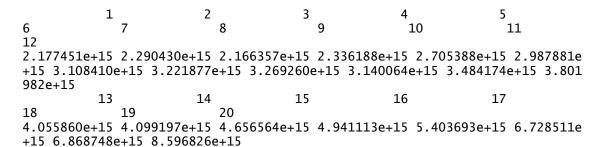


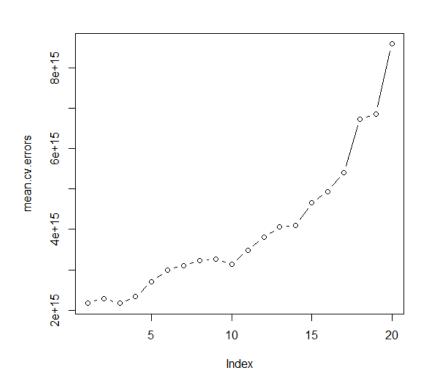
RESULTS:

Now we performed validation and cross validation Validation errors for Backward Model:

[1] 1.977368e+15 2.013289e+15 2.108028e+15 2.432386e+15 2.048173e+15 2.334 597e+15 2.243229e+15 2.617105e+15 2.848129e+15 4.978366e+15 5.016402e+15 [12] 4.939363e+15 3.653868e+15 4.698750e+15 5.188497e+15 9.626109e+15 1.00 3001e+16 1.252285e+16 1.252285e+16 3.566437e+16

Cross Validation errors for Backward Model:





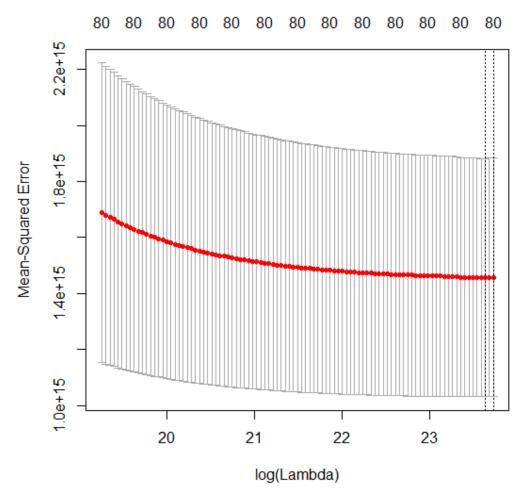
INFERENCES: The errors are in the range of e+15 because the predictor values taken are in crores (e+8) so in Normal terms if predictor values are in range of 0 to 1 then the errors are in range of e-2. The errors for both Models are around 0.217 %

3. Ridge Regression:

Shrinks the regression coefficients by imposing a penalty on their size and L2 Norm.we split the data into 1:1 ratio of training and testing set. Then we will try to find the best lamda value

for regression using mean squared error. If the lamba =0 then ridge regression is nothing but normal regression

RESULTS AND INFERENCES:



From the graph best lamda value = 18335537823
As Lamda is Large , so almost all of the coefficients will be reduced to negligible .From the ridge prediction the mean square error is 0.24 % .The coefficients for prediction of best Lamda value :

-3.098365e+03 8.181040e+01 5.628185e+02 Scoring.Rate Balls. Maidens. 2.091047e+01 -3.809815e+00 -1.083982e+02 Wickets. Average1 X5.Wickets.inInnings. -2.147169e+02 2.455434e+02 -1.516524e+03	(Intercept) 5.729701e+07 Ballskill 5.525616e+02 Aggregate. 1.214067e+01 X100s. 5.483216e+03 Ducks.	Age -7.343799e+03	Batskill 6.204467e+03 Not.Outs. -1.039347e+03 Average. 1.719877e+03 X300s. -5.049980e+04 X6s.
	-3.098365e+03	8.181040e+01	5.628185e+02
	Scoring.Rate	Balls.	Maidens.
	2.091047e+01	-3.809815e+00	-1.083982e+02
	Wickets.	Average1	X5.wickets.inInnings.

9.191338e+03	-5.294415e+00	7.119654e+02
Most.Catches.in.Innings.	Most.Catches.in.Match.	Innings1
1.312986e+04	8.084573e+03	1.954533e+02
Aggregate1	Highest.Score1	X50s1
1.023773e+01	4.710751e+02	1.703433e+03
X100s1	X4s1	X6s1
4.925367e+03	8.530789e+01	3.712605e+02
Scoring.Rate.1	Balls1	Wickets1
3.886524e+02	-1.035934e+01	-4.084956e+02
X4.Wickets.in.Innings.	Economy.Rate1	Strike.Rate1
-5.956189e+03	2.653117e+03	9.025077e+02
	Most.Catches.in.Match1	Innings2
5.437021e+02	-1.960974e+03	1.060070e+03
Not.Outs2	Aggregate2	Highest.Score2
4.864185e+03	3.319876e+01	5.754113e+02
X100s2	Ducks2	X4s2
3.455290e+03	2.059992e+03	3.584045e+02
X6s2	Scoring.Rate.2	Balls2
4.969612e+02	3.341090e+02	-4.531072e+01
Maidens2	Wickets2	Average5
-8.187025e+02	-1.055832e+03	9.690965e+02
X4.Wickets.in.Innings1	Economy.Rate2	Strike.Rate2
-3.339538e+04	-2.215802e+03	1.092168e+03
Catches2	Most.Catches.in.Match2	Innings3
2.248174e+03	4.441328e+04	6.055946e+02
Not.Outs3	Aggregate3	Highest.Score3
2.165473e+03	2.467565e+01	5.932971e+02
X50s3	X100s3	Ducks3
3.177591e+03	2.721089e+04	6.590851e+02
X4s3	X6s3	Balls.Faced3
2.118648e+02	4.814622e+02	3.200464e+01
Scoring.Rate.3	Opened.Batting3	Balls3
9.022595e+02	-1.776393e+02	-2.341419e+01
Maidens3	Wickets3	X4.Wickets.in.Innings2
-1.181649e+04	-4.473150e+02	-5.203384e+03
Economy.Rate3	Strike.Rate3	Catches3
-2.452062e+03	2.975215e+02	1.551515e+03
Most.Catches.in.Match3	Avg_actual_price	Avg_base_price
3.491090e+04	1.278153e-03	1.539084e-03

4. LASSO regression

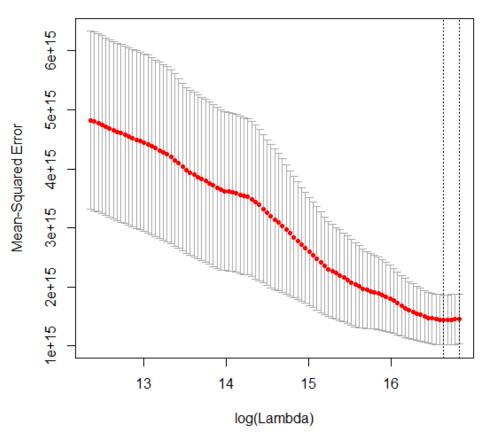
Produce simpler and more interpretable models with subset of predictors which is drawback of ridge regression Interpretation becomes difficult when p is quiet large and it uses L1 norm

RESULTS AND INFERENCES:

From the graph best lamda value = 16706659

As Lamda is Large , so almost all of the coefficients will be reduced to zero . From the LASSO prediction the mean square error is $0.24\,\%$. The coefficients for prediction of best Lamda value :

(Intercept)	Most.Catches.in.Match2	Avg_base_price
5.524990e+07	3.999852e+05	1.086991e-01

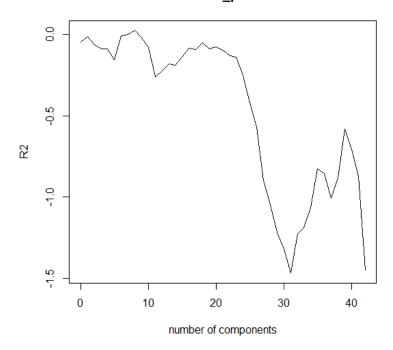


5. Principal Components Regression:

Transform the predictors and fit least squares model using transformed variables. If p is large relative to n, selecting a value of M « p significantly reduce variance of fitted coefficients So we fitted the PCR, cross validated and observed our Adjusted R-Squared values as below table : **RESULTS :**

```
Fit method: svdpc
Number of components considered: 42
VALIDATION: RMSEP
Cross-validated using 10 random segments.
       (Intercept)
                   1 comps 2 comps
                                         3 comps
                                                   4 comps
                                                             5 comps
                                                                        6 comps
                                                                                           8 comps
                                                                                                      9 comps 10 comps 11 comps 12 comps 13 comps
          44296626 41662485 42372264 42795311 43157594 43749164
                                                                      41703038 41882843 40331290
                                                                                                    41201824 42613815 41854015 41956226 43590414
          44296626 41567436 42242955 42631157 42987235 43621637
adjcv
                                                                      41291213 41365813 40240877
                                                                                                    40855860 42185149 41911595 40980499 42999642
       14 comps 15 comps 16 comps 17 comps 18 comps 19 comps 20 comps
                                                                                                 23 comps
                                                                                                           24 comps
                                                                                                                     25 comps
                                                                                                                                26 comps 27 comps
                                                                             21 comps
                                                                                       22 comps
                           47985645
                46974284
                                     47170547
                                               46937715
                                                         47385985
                                                                   48482240
                                                                             47984541
                                                                                        50691569
                                                                                                  50683241
                                                                                                            51721596
                                                                                                                      51951866
                                                                                                                                51683249
      45640184 45945453
                          46445736
                                     46127014
                                               45775911
                                                         46313056
                                                                   47417391
                                                                             47053573
                                                                                        49396524
                                                                                                  49401692
                                                                                                            50159357
       29 comps
                30 comps
                           31 comps
                                     32 comps
                                               33 comps
                                                         34 comps
                                                                   35 comps
                                                                              36 comps
                                                                                        37 comps
                                                                                                  38 comps
                                                                                                            39 comps
                                                                                                                      40 comps
                                                                                                                                41 comps
                                                                                                                                          42 comps
       59030501
                61108522 61655974 61821332
                                               55825092
                                                         54114843
                                                                   53387044
                                                                             53932612
                                                                                        52881907
                                                                                                  54964991
                                                                                                            53215542
                                                                                                                      53651538
                                                                                                                                56011315
                                                                                                                                          62825602
adjcv 58571852 59152360 60270573 60012835
                                               54514932
                                                         51858803
                                                                   51110498
                                                                             51714650
                                                                                        50940375
                                                                                                 52910220
                                                                                                            51569699
                                                                                                                      51796641
TRAINING: % variance explained
              1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8 comps 30.28 45.11 54.17 60.31 65.49 69.66 72.86 75.95
                                                                                      9 comps 10 comps 11 comps
78.62 80.91 83.12
                                                                                                                   12 comps 13 comps 14 comps 15 comps 84.91 86.53 88.10 89.29
Actual_price
                         14.25
                                  16.15
                                           16.31
                                                    17.02
                                                             31.33
                                                                       33.05
                                                                                33.27
                                                                                         36.21
                                                                                                   36.77
                                                                                                             36.85
                                                                                                                       46.39
                                                                                                                                 46.95
                                                                                                                                                      52.14
                                  18 comps
                                            19 comps
                                                      20 comps
                                                                21 comps
                                                                          22
                                                                             comps
                                                                                                         25
                                                                                                            comps
                 90.40
                           91.48
                                     92.31
                                               93.12
                                                         93.84
                                                                   94.46
                                                                             95.06
                                                                                        95, 62
                                                                                                  96.14
                                                                                                            96, 61
                                                                                                                      97.05
                                                                                                                                97.41
                                                                                                                                          97.74
                                                                                                                                                     98.06
Actual_price
                 55.46
                           55.47
                                     57.00
                                               58.63
                                                         59.55
                                                                    60.05
                                                                             62.36
                                                                                        62.67
                                                                                                  64.06
                                                                                                            64.13
                                                                                                                      64.40
                                                                                                                                64.40
                                                                                                                                          64.65
                                                                                                                                                     64.81
              30 comps
                        31 comps
                                  32 comps
                                            33 comps
                                                      34 comps
                                                                35 comps
                                                                                    37
                                                                                               38 comps
                                                                                                                   40 comps
                                                                          36
                                                                             comps
                                                                                        comps
                                                                                                            comps
                                                                                                                             41 comps
                                                                                                                                          comps
                           98.57
                                     98.77
                                               98.95
                                                         99.11
                                                                    99.26
                                                                              99.38
                                                                                        99.49
                                                                                                            99.66
                                                                                                                      99.73
                                                                                                                                99.80
                                                                                                                                           99.85
Actual_price
                 75.48
                           75.79
                                     80.71
                                               81.98
                                                         89.42
                                                                    90.56
                                                                              90.65
                                                                                        90.79
                                                                                                  91.93
                                                                                                            91.93
                                                                                                                      93.40
                                                                                                                                96.03
                                                                                                                                          96.12
```

Actual_price



INFERENCES:

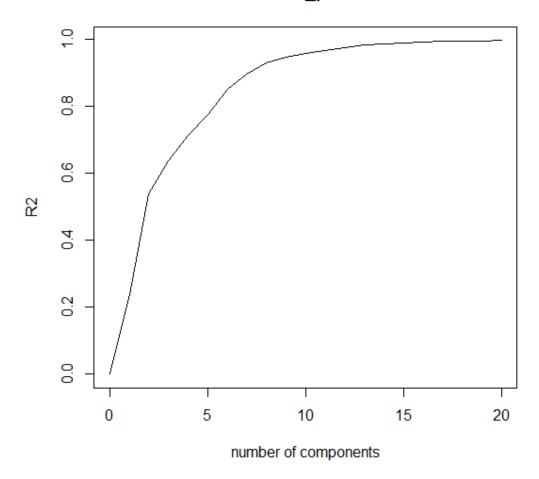
The mean value of Error in PCR is around 0.17 so far the best And from the graph the first 30 principal components are chosen because around that value adjusted R square Value is Approximately one. Note that here graph is reverse because R2 is in negative terms

6. Partial Least Squares:

A supervised alternative to PCR ,find directions that help explain both the response and the predictors , place highest weight on the variables that are most strongly related to the response. So we fitted the PLS, cross validated and observed our Adjusted R-Squared values as below table : **RESULTS :**

```
Data: X dimension: 24 80
       Y dimension: 24 1
Fit method: kernelpls
Number of components considered: 20
VALIDATION: RMSEP
Cross-validated using 10 random segments.
      (Intercept) 1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8 comps 9 comps 10 comps 11 comps 12 comps 13 comps
CV
        38884930 50688423 44090647 49885684 53447959 54012087 52672146 53697305 53969249 54634114 55133663 55394040 55456735 55500321
        38884930 48135138 43257195 48104620 50825785 51185267 49878580 50811028 51069746 51686348 52162685 52401619 52457995 52499497
adjcv
      14 comps 15 comps 16 comps 17 comps 18 comps 19 comps 20 comps
     55541799 55577803 55595906 55596046 55594658 55594138 55594171
adjcv 52538679 52573004 52590155 52590190 52588860 52588362 52588394
TRAINING: % variance explained
            1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps 8 comps 9 comps 10 comps 11 comps 12 comps 13 comps 14 comps 15 comps
             9.878 39.98
                            50.83 59.41 64.57 69.53 73.76
                                                                     77.57
                                                                                                83.39
                                                                                                                 86.72
                                                                                                                        89.71
                                                                                                                                   91.37
                                                                             79.85
                                                                                       81.86
                                                                                                        85.11
                     59.46
Actual_price 50.214
                              78.13
                                      90.10
                                             94.54
                                                     97.34
                                                             98.50 99.00
                                                                             99.40
                                                                                       99.69
                                                                                                99.90
                                                                                                         99.97
                                                                                                                 100.00
                                                                                                                         100.00
                                                                                                                                  100.00
            16 comps 17 comps 18 comps 19 comps 20 comps
              92.83
                       94.58
                                96.06
                                         97.05
                                                  98.19
Actual_price 100.00
                      100.00
                               100.00
                                        100.00
                                                 100.00
```

Actual_price



INFERENCES:

The mean value of Error in PLS is around 0.16 so far the best. And from the graph the first 15 principal components are chosen because around that value adjusted R square Value is Approximately one.

Based on the Adjusted R-Squares and Mean Value of error We choose PLS is a best model for prediction and it makes sense because we have only 48 observations but 109 variables so from reducing the dimensions drastically and taking into consideration of all Variable the error has been better compared to other Models.