

Assignment 3

Jatin Tarachandani

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1 Problem Statement

Let A_1, A_2, \dots, A_n be n independent events which the probability of occurrence of the event A_i is given by $Pr(A_i) = 1 - \frac{1}{\alpha^i}, \alpha > 1, i = 1, 2, \dots, n$. Then the probability that at least one of the events occurs is:

1. $1 - \frac{1}{\alpha^{\frac{n(n+1)}{2}}}$

2. $\frac{1}{\alpha^{\frac{n(n+1)}{2}}}$

3. $\frac{1}{\alpha^n}$

4. $1 - \frac{1}{\alpha^n}$

$$Pr(A_1 \cup A_2 \cup \dots \cup A_n) = 1 - Pr(A'_1) \cdot Pr(A'_2) \dots \cdot Pr(A'_n) \quad (2.0.5)$$

$$= 1 - \frac{1}{\alpha^1} \cdot \frac{1}{\alpha^2} \dots \cdot \frac{1}{\alpha^n} \quad (2.0.6)$$

$$= 1 - \frac{1}{\alpha^{\frac{n(n+1)}{2}}} \quad (2.0.7)$$

The probability that at least one of the specified events occurs is $1 - \frac{1}{\alpha^{\frac{n(n+1)}{2}}}$.

2 Solution

$$Pr(A'_i) = 1 - Pr(A_i) \quad (2.0.1)$$

$$= \frac{1}{\alpha^i} \quad (2.0.2)$$

for all i in $\{1, 2, 3, \dots, n\}$.

The probability that at least one event occurs is $Pr(A_1 \cup A_2 \cup \dots \cup A_n)$.

$$Pr(A_1 \cup A_2 \cup \dots \cup A_n) = 1 - Pr((A_1 \cup A_2 \cup \dots \cup A_n)') \quad (2.0.3)$$

Using de Morgans laws,

$$Pr(A_1 \cup A_2 \cup \dots \cup A_n) = 1 - Pr(A'_1 \cap A'_2 \cap \dots \cap A'_n) \quad (2.0.4)$$

Because all the n events are independent,