

```
1 import numpy as np
2
3 class NeuralNetwork:
4     def __init__(self, input_size, hidden_size, output_size):
5         self.weights_hidden = np.random.randn(input_size, hidden_size)
6         self.biases_hidden = np.zeros((1, hidden_size))
7
8         self.weights_output = np.random.randn(hidden_size, output_size)
9         self.biases_output = np.zeros((1, output_size))
10
11        self.hidden_activations = None
12        self.hidden_activities = None
13        self.output_activations = None
14        self.output_activities = None
15
16    def sigmoid(self, x):
17        return 1 / (1 + np.exp(-x))
18
19    def forward_prop(self, x):
20        hidden_activities = np.dot(x, self.weights_hidden) + self.biases_hidden
21        hidden_activations = self.sigmoid(hidden_activities)
22
23        output_activities = np.dot(hidden_activities, self.weights_output) + self
24            .biases_output
25        output_activations = self.sigmoid(output_activities)
26
27        self.hidden_activations = hidden_activations
28        self.hidden_activities = hidden_activities
```

```
33     self.forward_prop(x)
34
35     # Backpropagation
36     output_error = y - self.output_activations
37     output_delta = output_error * (self.output_activations * (1 - self
38         .output_activations))
39
39     hidden_error = np.dot(output_delta, self.weights_output.T)
40     hidden_delta = hidden_error * (self.hidden_activations * (1 - self
41         .hidden_activations))
42
42     # Update weights and biases for output layer
43     self.weights_output += learning_rate * np.dot(self.hidden_activations.T,
44         output_delta)
44     self.biases_output += learning_rate * np.sum(output_delta, axis=0, keepdims=True
45         )
46
46     # Update weights and biases for hidden layer
47     self.weights_hidden += learning_rate * np.dot(x.T, hidden_delta)
48     self.biases_hidden += learning_rate * np.sum(hidden_delta, axis=0, keepdims=True
49         )
50
50     # Example usage:
51     nn = NeuralNetwork(input_size=2, hidden_size=3, output_size=1)
52     x_train = np.array([[0.5, 0.8]])
53     y_train = np.array([[1]])
54     nn.back_prop(x_train, y_train)
```