## **Problem Set 1**

This problem set is meant to help you familiarize yourself with Python and Pandas. This is meant to be a very gentle introduction -- if you find this problem set to be difficult, you might want to consider taking a more introductory course.

# **Author and Acknowledgements**

Jon Atkins

After completing my answers, I consulted with Erin Jones and we compared and discussed our approaches to some problems but did not share code. Otherwise, I consulted only online resources.

#### **Before You Start**

For this problem set, you should download INF0251-PS1.ipynb from bCourses. Create a local copy of the notebook and rename it LASTNAME\_FIRSTNAME-PS1.ipynb. Then edit your renamed file directly in your browser by typing:

```
jupyter notebook <name_of_downloaded_file>
```

Make sure the following libraries load correctly (hit Ctrl-Enter).

```
In [ ]: #IPython is what you are using now to run the notebook
        import IPython
        print("IPython version: %6.6s (need at least 1.0)" % IPython.__version_
        # Numpy is a library for working with Arrays
        import numpy as np
                                   %6.6s (need at least 1.7.1)" % np.__version__)
        print("Numpy version:
        # SciPy implements many different numerical algorithms
        import scipy as sp
        print("SciPy version: %6.6s (need at least 0.12.0)" % sp.__version__)
        # Pandas makes working with data tables easier
        import pandas as pd
                                  %6.6s (need at least 0.11.0)" % pd.__version__)
        print("Pandas version:
        # Module for plotting
        import matplotlib
        print("Maplotlib version: %6.6s (need at least 1.2.1)" % matplotlib.__ver
        # SciKit Learn implements several Machine Learning algorithms
```

```
import sklearn
 print("Scikit-Learn version: %6.6s (need at least 0.13.1)" % sklearn.__versi
 # Seaborn for easier visualizations
 import seaborn as sns
 print("Seaborn version:
                                %6.6s" % sns.__version__)
IPython version:
                       8.20.0 (need at least 1.0)
                       1.26.3 (need at least 1.7.1)
Numpy version:
                      1.11.4 (need at least 0.12.0)
SciPy version:
SciPy version: 1.11.4 (need at least 0.12.0) Pandas version: 2.1.4 (need at least 0.11.0)
Maplotlib version:
                       3.8.0 (need at least 1.2.1)
Scikit-Learn version: 1.3.0 (need at least 0.13.1)
```

### Working in a group?

Seaborn version:

List the names of other students with whom you worked on this problem set:

- Person 1
- Person 2
- ...

## Introduction to the assignment

0.13.1

For this assignment, you will be using the California Housing Prices Dataset. Please read about the dataset carefully before continuing -- it is worth investing a few minutes up front otherwise you are likely to be hopelessly confused! We'll be coming back to this dataset repeatedly throughout the semester. Also, if you're new to analyzing data in Python, please make sure to read the relevant readings linked to on Canvas before beginning, otherwise you'll be stabbing in the dark.

Use the following commands to load the dataset:

```
In [ ]: from sklearn.datasets import fetch_california_housing
    cal_data = fetch_california_housing()
```

The following commands will provide some basic information about the data:

```
In []: print(cal_data.DESCR)
    print(cal_data.keys())
    print(cal_data.feature_names)
    print(cal_data.data.shape)
    print(cal_data.target.shape)
```

.. california housing dataset:

#### California Housing dataset

\*\*Data Set Characteristics:\*\*

:Number of Instances: 20640

:Number of Attributes: 8 numeric, predictive attributes and the target

#### :Attribute Information:

MedInc median income in block group

HouseAge median house age in block group
 AveRooms average number of rooms per household
 AveBedrms average number of bedrooms per household

Population block group population

- AveOccup average number of household members

block group latitude Latitude Longitude block group longitude

:Missing Attribute Values: None

This dataset was obtained from the StatLib repository. https://www.dcc.fc.up.pt/~ltorgo/Regression/cal housing.html

The target variable is the median house value for California districts, expressed in hundreds of thousands of dollars (\$100,000).

This dataset was derived from the 1990 U.S. census, using one row per census block group. A block group is the smallest geographical unit for which the U.S.

Census Bureau publishes sample data (a block group typically has a populatio

of 600 to 3,000 people).

A household is a group of people residing within a home. Since the average number of rooms and bedrooms in this dataset are provided per household, the

columns may take surprisingly large values for block groups with few househo lds

and many empty houses, such as vacation resorts.

It can be downloaded/loaded using the :func:`sklearn.datasets.fetch\_california\_housing` function.

- .. topic:: References
  - Pace, R. Kelley and Ronald Barry, Sparse Spatial Autoregressions, Statistics and Probability Letters, 33 (1997) 291-297

dict\_keys(['data', 'target', 'frame', 'target\_names', 'feature\_names', 'DESC

['MedInc', 'HouseAge', 'AveRooms', 'AveBedrms', 'Population', 'AveOccup', 'L atitude', 'Longitude']

```
(20640, 8)
(20640,)
```

The following commands will put together the features and target into a pandas dataframe:

## Part 1: Descriptive analysis

## 1.1: Explore the data

Let's dig into the data a bit to see what we're dealing with. The first thing to do is to make sure you understand how the data is organized, what the data types are, whether there is any missing data, and so forth. Get your bearings on your own, then answer the following questions.

- 1.1.1: How many different variables are there in the dataset, and how many different observations?
- 1.1.2: What is the datatype of each variable?
- 1.1.3: Does the dataset contain any missing values?
- 1.1.4: How would you interpret the row index value?

```
In []: # Your code here

# 1.1.1
display(cal_df.shape)

# 1.1.2
display(cal_df.dtypes)

# 1.1.3
any(cal_df.isnull()) # I guess this dosn't work how I expected
cal_df.isnull().sum() # There are none
display(cal_df.isna().any()) # <- I guess its this

# 1.1.4
display(cal_df)</pre>
(20640, 9)
```

MedInc	float64				
HouseAge	float64				
AveRooms	float64				
AveBedrms	float64				
Population	float64				
Ave0ccup	float64				
Latitude	float64				
Longitude	float64				
MedHouseVal	float64				
dtype: object					
MedInc	False				
HouseAge	False				
AveRooms	False				
AveBedrms	False				
Population	False				
Ave0ccup	False				
Latitude	False				
Longitude	False				
MedHouseVal	False				
dtype: bool					

a cypc.	5000							
	MedInc	HouseAge	AveRooms	AveBedrms	Population	AveOccup	Latitude	Lo
0	8.3252	41.0	6.984127	1.023810	322.0	2.555556	37.88	
1	8.3014	21.0	6.238137	0.971880	2401.0	2.109842	37.86	
2	7.2574	52.0	8.288136	1.073446	496.0	2.802260	37.85	
3	5.6431	52.0	5.817352	1.073059	558.0	2.547945	37.85	
4	3.8462	52.0	6.281853	1.081081	565.0	2.181467	37.85	
•••	•••							
20635	1.5603	25.0	5.045455	1.133333	845.0	2.560606	39.48	
20636	2.5568	18.0	6.114035	1.315789	356.0	3.122807	39.49	
20637	1.7000	17.0	5.205543	1.120092	1007.0	2.325635	39.43	
20638	1.8672	18.0	5.329513	1.171920	741.0	2.123209	39.43	
20639	2.3886	16.0	5.254717	1.162264	1387.0	2.616981	39.37	

20640 rows × 9 columns

#### Provide your answers below:

- 1.1.1: 9 variables, 20640 observations
- 1.1.2: they're all 64-bit floating-point numbers
- 1.1.3: There are none
- 1.1.4: The row index is basically a numerical identifier of each row. Here it looks like they were added sequentially with none removed since, they go from 0 to n-observations 1.

### 1.2: Answer some basic questions

- 1.2.1: What is the average population per block group? What was California's total population in 1990 according to the Census?
- 1.2.2: What are the median house values in California's block groups with the lowest and highest populations?
- 1.2.3: Suggest 5 block groups that are likely to be vacation resorts. Do a quick Google search to validate your results.
- 1.2.4: How many census block groups are west of the city of Berkeley (lat: 37.871666, long: -122.272781)?
- 1.2.5: What fraction of block groups have an average number of household members greater or equal to 10?

```
In [ ]: # Your code here
        # 1.2.1
        np.mean(cal df['Population']) # 1425.48
        np.sum(cal_df['Population']) # 29,421,840
        # 1.2.2
        cal_df.iloc[np.argmax(cal_df['Population'])]['MedHouseVal'] # Max: 1.344
        cal_df.iloc[np.argmin(cal_df['Population'])]['MedHouseVal'] # Min: 3.5
        cal df.iloc[cal df['Population'].idxmax()]['MedHouseVal'] # Max: 1.344
        # 1.2.3 - Vacaction Resorts
        ### Methodology: based on the documentation of the dataset, we can assume th
        # The block groups with the 5 largest values for `AveBedrms`are here:
        print('Vaction resorts?')
        display(cal_df.sort_values('AveBedrms', ascending=False).head(5)[['Latitude'
        # # 1.2.4 - West of Berkeley
        cal_df.query("Longitude < -122.272781").shape[0] # 2167
        # # # 1.2.5 - Average Occupancy > 10??
        cal df.query("AveOccup > 10").shape[0]/cal df.shape[0] # 37
```

Vaction resorts?

	Latitude	Longitude
1979	38.80	-120.08
1914	38.91	-120.10
11862	40.27	-121.25
12447	33.97	-114.49
9676	37.64	-119.02

Out[]: 0.0017926356589147287

Provide your answers below:

- 1.2.1: Mean: 1,425.48; Total: 29,421,840
- 1.2.2: Max: 1.344; Min: 3.5
- 1.2.3: the 5 pairs of lat/long listed above are in order:
  - 1979: the base of Sierra-at-Tahoe Ski Resort
  - 1914: Mt. Tallac (Tahoe)
  - 11862: A resort on Lake Almanor
  - 12447: A section of the colorado river on the border with Arizona (possibly a relic of the reporting on the Colorado River Reservation?)
  - 9676: The base village at Mammoth Mountain ski resort
- 1.2.4: 2167
- 1.2.5: 37/20640 = 0.001793

## 1.3: Summary statistics

Create a clean, organized table that shows just the following information (no more, no less) for each variable in the dataset. Note that your table should have K rows (one for each variable) and 7 columns, ordered as below:

- The name of the variable
- The number of observations with non-missing values
- The mean of the variable
- The standard deviation of the variable
- The minimum value of the variable
- The median of the variable
- The maximum value of the variable

Out[]:

	median	min	std	mean	n non- missing	var	
15	3.534800	0.499900	1.899776	3.870671	20640.0	MedInc	0
52	29.000000	1.000000	12.585253	28.639486	20640.0	HouseAge	1
14	5.229129	0.846154	2.474113	5.429000	20640.0	AveRooms	2
34	1.048780	0.333333	0.473899	1.096675	20640.0	AveBedrms	3
35682	1166.000000	3.000000	1132.434688	1425.476744	20640.0	Population	4
1243	2.818116	0.692308	10.385798	3.070655	20640.0	AveOccup	5
41	34.260000	32.540000	2.135901	35.631861	20640.0	Latitude	6
-114	-118.490000	-124.350000	2.003483	-119.569704	20640.0	Longitude	7
Ĺ	1.797000	0.149990	1.153928	2.068558	20640.0	MedHouseVal	8

### 1.4 Simple Linear Regression

Estimate a linear regression of the median house value (the dependent variable) on the population (the independent variable), with no other control variables. Interpret the coefficients and standard errors. Based on this analysis, can you conclude anything about the causal effect of decreasing the population on the median housing value?

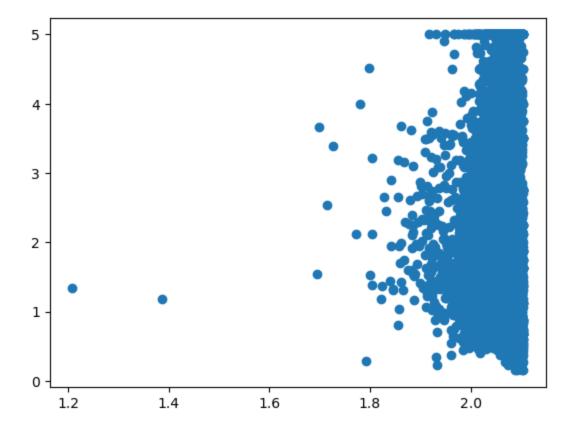
#### OLS Regression Results

===========							
==							
Dep. Variable: 01		MedHouse	eVal	R-squ	ared:		0.0
Model:			0LS	Adj.	R-squared:		0.0
01				_	•		
Method:		Least Squa	ares	F–sta	tistic:		12.
55 Date:		Wed, 24 Jan 2	2024	Prob	(F-statistic	):	0.0003
98					(. 5:4:15:16	, .	0.0003
Time:		10:37	7:16	Log-L	ikelihood:		-3223
<ol><li>6.</li><li>No. Observation</li></ol>	16 '	20	0640	AIC:			6.448e+
04	13.	20	7040	AIC.			0144001
Df Residuals:		20	0638	BIC:			6.449e+
04 Df Model:			1				
Covariance Type	<b>:</b> :	nonrol	_				
=======================================			=====	=====	========	=======	=======
==	coef	std err		+	D~ I + I	[0 025	0.97
5]	COCT	Stu CII			17[0]	[0:023	0.97
 const	2.1044	0.013	163	.012	0.000	2.079	2.1
30		0.000					
Population -2.5	512e-05	7 <b>.</b> 09e-06	-3	<b>.</b> 542	0.000	-3 <b>.</b> 9e-05	-1 <b>.</b> 12e-
######################################		=========		=====	========	=======	=======
==							
Omnibus: 08		2387	069	Durbi	n-Watson:		0.3
Prob(Omnibus):		0.	.000	Jarqu	e-Bera (JB):		3301.8
67							
Skew:		0.	967	Prob(	JB):		0.
00 Kurtosis:		3.	311	Cond.	No.		2.93e+
03		5.		201141			2.3301
=======================================				=====	=======	=======	=======
==							

#### Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 2.93e+03. This might indicate that there are
- strong multicollinearity or other numerical problems.

Out[]: <matplotlib.collections.PathCollection at 0x28e5a65a0>



Write your response here.

There appears to be a very minimal relationship between MedHouseValue and Population. This is evidenced by the extremely low R^2 value, which tells us that the % of the variance in MedHouseValue explained by Population is about .001. The coefficient for the Population value is thus extremely small in magnitude and the model tells us that essentially House Value cannot be explained by population alone. However, this small coefficient ( -2.512e-05 ) does appear to have a very small std.Error ( 7.09e-06 ) and be statistically significant at almost any reasonable significance level ( p-value of the Population coefficient is ~ 0.000 and the overall f-statistic is 0.000398, both of which are significantly smaller than .05 or .01). This all tells us that, while the relationship is very very minor, we can somewhat confidentally say that there is a small negative relationship between Population and MedianHouseValue, however we can say nothing about whether this relationship is causal in any way.

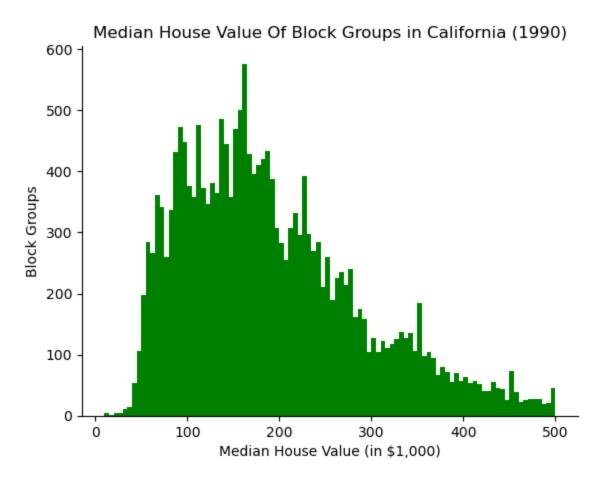
# Part 2: Histograms and Scatterplots

## 2.1: Histogram of housing prices

Below you will find some very basic code to make a very basic histogram of median housing prices (the "target" variable) for your dataset. Your first task is to make this

graph look pretty by doing the following:

- 1. Add appropriate labels to the x and y axes, make sure to include units
- 2. Change the bin width on the histogram to be \$5,000
- 3. Remove the axes on the top and right side of the plot window
- 4. Change the color of the bars to be green
- 5. Add an appropriate title



### 2.2: Histogram of average occupancy

Now use your histograming skills to create a fine looking histogram of the average number of household members ("AveOccup"). In the same figure, plot the mean and median values of this variable. (Hint: applying a very common transformation to the data might make things easier).

```
In []: # enter your code here

# Calculate Mean AvgOccup
### Note: I'm going to assume we want to weight this by number of households
mean_avgOccup_hh = np.average((cal_df['AveOccup']), weights=(cal_df['Populat

### If we just want the median avg occupancy for a block group, that value i
mean_avgOccup_bg = np.average(cal_df['AveOccup'])

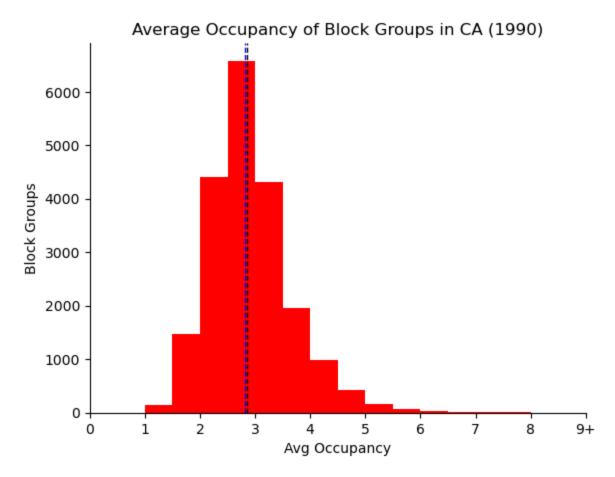
# Calculate Median AvgOccup
### For Median, if we wanted to weight them, that's a pretty complicated fun
median_avgOccup = (cal_df['AveOccup']).median()

print(f"mean_hh: \t{round(mean_avgOccup_hh, 2)}\nmean_bg: \t{round(mean_avgOccup_hh, 2)}\nmean_bg: \t{round(mean_avgOccup_hh, 2)}\nmean_bg: \tau{nud(mean_avgOccup_hh, 2)}\nmean_bg: \tau{nud(mean
```

```
# Set Binwidth
#bin_width = .1 # 5000/100000 # 5,
\#bins = np.arange(np.floor(np.min(X) - np.min(X) % bin width), np.floor(np.min(X) % bin width), n
print(f"max val: \t{np.max(X):.2f}")
# Note there are a handful of ones with huge AveOccup. Looking at their lat/
cal_df.iloc[np.argmax(cal_df['AveOccup'])] # Max: 1.344
display(cal_df.sort_values('AveOccup', ascending = False).head(10))
# Lets put them all into a bin of their own of 6+ (because this is where thi
max val = 8
X = np.where(X > max val, max val+1, X)
# Make the Hsitogram
ax.hist(X, bins = np.arange(1,max val+1, .5), color = 'red')
ax.set_ylabel('Block Groups')
ax.set_xlabel('Avg Occupancy')
ax.set_title('Average Occupancy of Block Groups in CA (1990)')
# Edit last label to be the right size
labels = [item.get_text() for item in ax.xaxis.get_ticklabels()]
labels[-1] = f''\{max\_val+1\}+''
ax.xaxis.set_ticks(np.arange(0, max_val+2))
ax.xaxis.set_ticklabels(labels)
# *Note*: We could alternatively log-scale them, which would make the graph
# but I think that will make things very hard to interpret since the scale w
# Add Mean/Median Lines
ax.axvline(mean_avg0ccup_hh, color='k',linestyle='dashed', linewidth=1)
ax.axvline(median avg0ccup, color='b',linestyle='dashed', linewidth=1)
# Remove axes
ax.spines[['right','top']].set_visible(False)
plt.show()
```

mean\_hh: 2.85
mean\_bg: 3.07
median\_hh: N/A
median\_bg: 2.82
max val: 1243.33

	MedInc	HouseAge	AveRooms	AveBedrms	Population	AveOccup	Latitude
19006	10.2264	45.0	3.166667	0.833333	7460.0	1243.333333	38.32
3364	5.5179	36.0	5.142857	1.142857	4198.0	599.714286	40.41
16669	4.2639	46.0	9.076923	1.307692	6532.0	502.461538	35.32
13034	6.1359	52.0	8.275862	1.517241	6675.0	230.172414	38.69
9172	4.2391	5.0	5.123810	0.933333	8733.0	83.171429	34.47
12104	1.6250	8.0	7.600000	0.950000	1275.0	63.750000	33.97
16420	5.7485	26.0	5.366667	0.900000	1542.0	51.400000	37.89
8874	9.3370	52.0	7.285714	1.214286	1154.0	41.214286	34.06
13366	4.2578	36.0	5.258824	1.117647	2886.0	33.952941	33.94
5986	1.8750	52.0	4.500000	1.206349	2688.0	21.333333	34.10



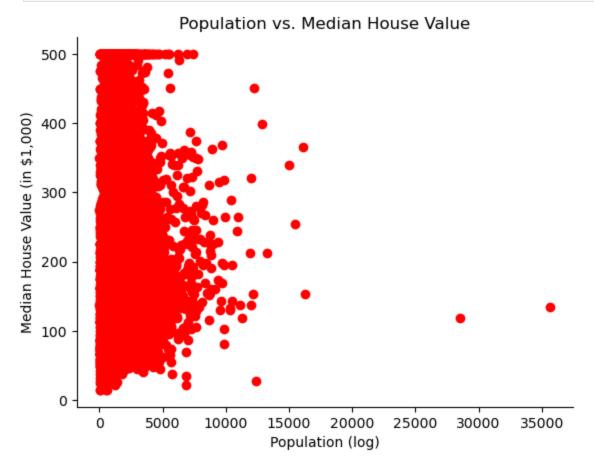
# 2.3: Scatter plot of housing prices and population

Use matplotlib to create a scatter plot that shows the relationship between the block group median house value (y-axis) and the block group population (x-axis). Properly label your axes, and make sure that your graphic looks polished and professional.

```
In []: # enter your code here
ax, fig = plt.subplots()

fig.scatter(cal_df['Population'], cal_df['MedHouseVal'] * 100, color = 'r')
fig.set_xlabel('Population (log)')
fig.set_ylabel('Median House Value (in $1,000)')
fig.set_title('Population vs. Median House Value')

# Remove axes
fig.spines[['right','top']].set_visible(False)
```



## 2.4: Interpret

What do you observe in the above scatter plot? Does there appear to be a relationship between median house value and population in California? Calculate the correlation between these two variables. Do you think this relationship is causal, or just a correlation? Justify your position and compare to your answer in section 1.4.

```
In []: # enter your code here
# There does not appear to be much of a relationship at all between the two
print(f"Correlation: {cal_df['Population'].corr(cal_df['MedHouseVal']):.4f}"
cal_df[cal_df['Population'] > 3000]
```

Correlation: -0.0246

Out[ ]:

	MedInc	HouseAge	AveRooms	AveBedrms	Population	AveOccup	Latitude
95	2.0096	36.0	2.294016	1.066294	3469.0	1.493328	37.80
185	2.1917	43.0	4.844029	1.091795	4367.0	3.547522	37.79
283	5.9849	22.0	6.528724	1.041179	4985.0	2.534316	37.79
460	1.4012	52.0	3.105714	1.060000	3337.0	9.534286	37.87
485	1.6307	35.0	2.962687	1.001148	3276.0	1.880597	37.86
•••		•••	•••	•••		•••	•••
20544	2.0650	23.0	4.803493	1.013646	6330.0	3.455240	38.55
20563	3.1250	9.0	5.148007	1.119593	6837.0	2.899491	38.67
20567	5.3064	15.0	6.423585	0.992453	3060.0	2.886792	38.66
20604	2.3496	17.0	4.551392	0.962527	3265.0	3.495717	39.12
20629	2.0943	28.0	5.519802	1.020902	6912.0	3.801980	39.12

1357 rows × 9 columns

Write your thoughts here (1-2 paragraphs). The correlation is very small here, as described in 1.4 above, and this tells us there is a very weak linear relationship between the two variables. However, as we determined above, this relationship is significant at almost any reasonable significance level and as such, it is not a neglible effect. The relationship tells us that, on the whole, for every individual person in a block group compared to a hypothetically similar, we can expect the Median House Value in the block group with one additional person to be slightly lower.

While we can say that this relationship holds across the state, we *cannot*, however, imply that Population is the 'cause' of the drop in Median House Value, as correlation does not imply causation. As such, they could both just as reasonably be influenced by unforeseen other factors. We can speculate however, it is the definition census block group that is causing some of the confusion here. Since block groups are generally defined to encompass 600-3000 people, size of block group should not have much effect. However, with a small preference for maintaining continuity decade-over-decade, the block groups with more than 3000 people are most likely either special cases (like the prisons or barrackses - often in low-cost-of-living areas), and, as such, could cause some unexpected results. Furthermore, there is plenty that would go into defining block groups that could correlate with either political power or the rapid growth of an area - both of which could have significant correlations with House values. All to say, there are some arguments to be made for not looking for relationships with Population-size at a geographic level that is defined by population-size.

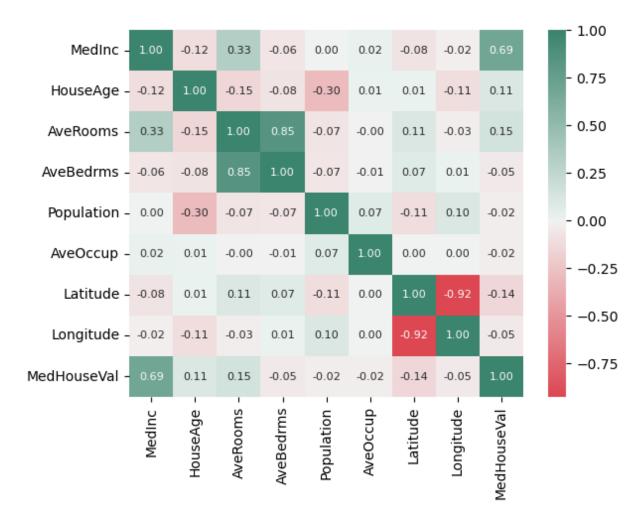
Note: it can be seen in the above, and other plots, but I remain unclear why the maximum MedHouseVal appears to be capped at exactly 500,000. This looks like an articifical

boundary that could have an important impact on statistical measures here.

### 2.5 Correlation Matrix

Calculate the correlation of every pair of variables in the dataset. Create a  $K \times K$  matrix where the value in the (i,j) cell is the correlation between the ith and jth variable. Show off your skills by coloring the cell so that large positive correlations appear green and large negative correlations appear red (use a gradient to make this pretty). What two variables appear to me most positively and negatively correlated? Explain these results.

Out[]: <Axes: >



Write your response here. The two most corellated values appear to be Average Number of Rooms and Average Number of Bedrooms, with a value of .85. This makes a lot of sense intuitively and is not that interesting in my opinion. However, Median Income and Median Household Value are also fairly highly corellated (.69) and that represents a bit more of an interesting relationship, which we'll explore below.

As for Negative corellation, Latitude and Longitude appear to be very strongly negatively corelated, which is interesting but simply a reflection of the diagonal directionality of the shoreline, the Nevada border and ultimately the fault-lines underlying the state's mountain ranges. That it shows up so strongly is fairly interesting but it is just a function of the map, not of the housing market itself. Beyond that, there is a noticable negative correlation between <code>Population</code> of a block-group and <code>HouseAge</code>. As mentioned above, the defininition of a block group (as it is theoretically defined by size), should not generally correlate with much on its own. However, when it does, it is most likely a relic of some of the process that went into its definition. As noted above, a reason why a block group might be larger than the "ideal size" of <code>1500</code>, is because it grew significantly in recent years. e.g. If it was defined in 1980 as a 1500-person block group, but then grew significantly but not above the <code>3000</code> -person threshold (which itself is apparently not strict), it would maintain its territorial integrity

but have lots of new housing - thus reducing the <code>HouseAge</code> . This, as noted above could have all sorts of impact on housing prices that may or may not be expected in the investigation.

As for no correllations. It is somewhat interesting the Averge Number of Bedrooms as essentially 0 correlation with Median House Value, since more bedrooms would normally imply a larger house, however that makes sense at the block group level since location is a much stronger determinant of value than size is.

### 2.6 Create your own (creative and effective) visualization

Use another type of graph or chart to illustrate an interesting pattern in the data. Be creative in your visualization, and make sure to produce a "publication-quality" graph. Points will be given for useful and creative graphs; points will be deducted for confusing issues like unlabeled axes. If you're new to data visualization, this guide is a good place to start.

```
In [ ]: # enter your code here
        # Let's here explore the relationship between Median Income and Median Housi
        ax, fig = plt.subplots()
        fig = sns.scatterplot(
            x = 'MedInc',
            y = 'MedHouseVal',
            size = 'Population',
            data = cal df,
            sizes = (3,80)
        # Labels
        fig.set_xlabel('Median Income')
        fig.set_ylabel('Median House Value')
        fig.set_title('CA Median Income vs. Median Household Value')
        # Fix Axes
        fig.spines[['right','top']].set_visible(False)
        # Create a trendline
        model = sm.OLS(cal_df['MedHouseVal'], sm.add_constant(cal_df['MedInc']))
        results = model.fit()
        x = np.arange(0, 14, .01)
        trendline = results.params['MedInc'] * x + results.params['const']
        fig.plot(x, trendline, color = 'r', label = 'trendline')
        plt.show()
```

