



**UNIVERSIDAD NACIONAL AUTÓNOMA DE MÉXICO**  
**POSGRADO EN CIENCIAS FÍSICAS**

**OPTICAL RESPONSE OF PARTIALLY EMBEDDED  
NANOSPHERES**

**TESIS**  
**QUE PARA OPTAR POR EL GRADO DE:**  
**MAESTRO EN CIENCIAS (FÍSICA)**

**PRESENTA:**  
**JONATHAN ALEXIS URRUTIA ANGUIANO**

**TUTOR:**  
**DR. ALEJANDRO REYES CORONADO**  
FACULTAD DE CIENCIAS, UNAM

**MIEMBROS DEL COMITÉ TUTOR**  
**DRA. CIRLALI SÁNCHEZ-AKÉ**  
INSTITUTO DE CIENCIAS APLICADAS Y TECNOLOGÍA, UNAM  
**DR. GIUSEPPE PIRRUCCIO**  
INSTITUTO DE FÍSICA, UNAM

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# Abstract/Resumen

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# Introduction

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It is recommended to fill in this part of the document with the following information:

- Your field: Context about the field your are working  
**Plasmonics -> Metamaterials -> Biosensing**
- Motivation: Background about your thesis work and why did you choose this project and why is it important.  
**Fabrication -> Partially embedded NPs -> No analytical (approximated) method physically introduces the incrustation degree. There are numerical solutions and Effective Medium Theories approaching the problem but the later only as a fitting method.**
- Objectives: What question are you answering with your work.  
**Can optical non invasive tests (IR-Vis) retrieve the average incrustation degree for monolayers of small spherical particles?**
- Methology: What are your secondary goals so you achieve your objective. Also, how are you answering yout question: which method or model.  
**Bruggeman homogenization theories on bidimensional systems?  
Is the dipolar approximation is enough or do we need more multipolar terms?  
Do we need the depolarization factors?**
- Structure: How is this thesis divides and what is the content of each chapter.





# Optical properties of single plasmonic nanoparticles

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## 1.1 Mie Theory: Quasi-static Approximation

## 1.2 Depolarization Factors

## 1.3 Substrate effects



# Collections: Effective Medium Theories

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## 2.1 3D theories: summary

### 2.1.1 Bruggemann & Maxwell Garnett

## 2.2 2-D Arrays

### 2.2.1 Island Theory

### 2.2.2 Dipolar Model



## Results and discussion

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- 3.1 Single particle: Incrustation degree (COMSOL + approximate solutions)
- 3.2 Analytical extention to a monolayer



# Conclusions

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# Finite Element Method

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# List of Figures