

$$\operatorname{Re}^2 u + \operatorname{Im}^2 u \leq 1$$

$$\left(1 - \frac{4D\tau}{h^2} \sin^2 \frac{\varphi}{2}\right)^2 + \frac{a^2 \tau^2}{h^2} \sin^2 \varphi \leq 1$$

$$1 - \frac{8D\tau}{h^2} \sin^2 \frac{\varphi}{2} + \frac{16D^2\tau^2}{h^4} \sin^4 \frac{\varphi}{2} + \frac{a^2 \tau^2}{h^2} \sin^2 \varphi \leq 1$$

$$\sin^2 \frac{\varphi}{2} \stackrel{0}{=} m^2 \Rightarrow \sin^2 \varphi = 4 \sin^2 \frac{\varphi}{2} \left(1 - \sin^2 \frac{\varphi}{2}\right) = 4m^2(1-m^2)$$

$$\frac{16D^2\tau}{h^2} m^4 + 4a^2\tau m^2(1-m^2) - 8Dm^2 \leq 0$$

$$\frac{4D^2\tau}{h^2} m^2 + a^2\tau - a^2\tau m^2 \leq 2D$$

$$\left(\frac{4D^2\tau}{h^2} - a^2\tau\right) m^2 \leq 2D - a^2\tau$$

$$1) \frac{4D^2\tau}{h^2} > a^2\tau \Leftrightarrow 4D^2 > a^2h^2$$

$$m^2 \leq \frac{2D - a^2\tau}{\frac{4D^2\tau}{h^2} - a^2\tau}$$

$$m^2 = \sin^2 \frac{\varphi}{2} \leq 1 \Rightarrow \frac{2D - a^2\tau}{\frac{4D^2\tau}{h^2} - a^2\tau} \geq 1$$

$$2D - a^2\tau \geq \frac{4D^2\tau}{h^2} - a^2\tau$$

$$\boxed{\frac{2D\tau}{h^2} \leq 1}$$

$$2) \frac{4D^2\tau}{h^2} < a^2\tau \Leftrightarrow 4D^2 < a^2h^2$$

$$m^2 \leq \frac{2D - a^2\tau}{a^2\tau - \frac{4D^2\tau}{h^2}}$$

$$m^2 = \sin^2 \frac{\varphi}{2} \leq 1 \Rightarrow \frac{2D - a^2\tau}{a^2\tau - \frac{4D^2\tau}{h^2}} \geq 1$$

$$2D - 2a^2\tau + \frac{4D^2\tau}{h^2} \geq 0$$

$$\text{T.K. } D^2 < \frac{a^2h^2}{4}, D < \frac{ah}{2}, \text{ so } 0 \leq 2D - a^2\tau + \frac{2D^2\tau}{h^2} <$$

$$\frac{a^2\tau}{2} < \frac{ah}{2} \Rightarrow \boxed{\frac{a\tau}{h} < 1} < \frac{ah}{2} - a^2\tau + \frac{a^2h^2\tau}{2h^2}$$

$$3) \frac{4D^2\tau}{h^2} = a^2\tau \Leftrightarrow D = \frac{ah}{2}$$

$$0 \leq 2D - a^2\tau \Rightarrow ah \geq a^2\tau \Rightarrow \boxed{\frac{a\tau}{h} \leq 1}$$

Итого, условия выполнения:

$$\left[ \begin{array}{l} \left\{ \begin{array}{l} \frac{2\vartheta\tau}{h^2} \leq 1 \\ 4\vartheta^2 > a^2 h^2 \end{array} \right. \\ \\ \left\{ \begin{array}{l} \frac{a\tau}{h} \leq 1 \\ 4\vartheta^2 \leq a^2 h^2 \end{array} \right. \end{array} \right.$$