Statistical Inference - Data Science - Quiz 2 - Coursera

Statistical Inference Quiz 2

This is Quiz 2 from the Statistical Inference course in the Data Science Specialization from John's Hopkins.

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1 . CWhat is the variance of the distribution of the average an IID draw of n observations from a population with mean μ and variance $\sigma 2$.
• σ2/n
2. Suppose that diastolic blood pressures (DBPs) for men aged 35-44 are normally distributed with a mean of 80 (mm Hg) and a standard deviation of 10. About what is the probability that a random 35-44 year old has a DBP less than 70?
• 16%

```
pnorm(70, mean = 80, sd = 10)
## [1] 0.1586553
```

3. Brain volume for adult women is normally distributed with a mean of about 1,100 cc for women with a standard deviation of 75 cc. What brain volume represents the 95th percentile?

approximately 1223

```
qnorm(0.95, mean = 1100, sd = 75)
## [1] 1223.364
```

4. Refer to the previous question. Brain volume for adult women is about 1,100 cc for women with a standard deviation of 75 cc. Consider the sample mean of 100 random adult women from this population. What is the 95th percentile of the distribution of that sample mean?

· approximately 1112 cc

```
qnorm(0.95, mean = 1100, sd = 75/sqrt(100))
## [1] 1112.336
```

- 5. You flip a fair coin 5 times, about what's the probability of getting 4 or 5 heads?
 - 19%

```
#Probability of being stricly greater than 3 heads (4 or 5)
pbinom(3, size = 5, prob = 0.5, lower.tail = FALSE)
## [1] 0.1875
```

- **6.** The respiratory disturbance index (RDI), a measure of sleep disturbance, for a specific population has a mean of 15 (sleep events per hour) and a standard deviation of 10. They are not normally distributed. Give your best estimate of the probability that a sample mean RDI of 100 people is between 14 and 16 events per hour?
 - 68% (within 1 sd)

```
pnorm(16, mean = 15, sd = 1) - pnorm(14, mean = 15, sd = 1)
## [1] 0.6826895
```

7. Consider a standard uniform density. The mean for this density is .5 and the variance is 1 / 12. You sample 1,000 observations from this distribution and take the sample mean, what value would you expect it to be near?

0.5

```
x <- rnorm(1000, mean=.5, sd=sqrt(1/12))
mean(x)
## [1] 0.4846762</pre>
```

8. The number of people showing up at a bus stop is assumed to be Poisson with a mean of 5 people per hour. You watch the bus stop for 3 hours. About what's the probability of viewing 10 or fewer people?

0.12

```
ppois(10,15,lower.tail = TRUE)
## [1] 0.1184644
```