

GIST 8118 Module 5A

Image pre-processing

Geometric Transformations

Outline

- Lecture
 - Pre processing
 - Geometric
- Lab
 - Tutorial geometric correction

Pre Processing of images

- Corrections are made to allow for
 - distortions
 - errors
 - noise
- created during
 - scanning
 - transmission
 - recording
 - storage

Data Errors

- Internal errors are
 - systematic sensor errors
 - may be predicted
 - E.g. sensor recording high or low
 - generally corrected before you receive data
- External errors are
 - platform instability
 - atmospheric conditions
 - E.g. Lots of pollution (haze)
 - cannot be predicted
 - methods to correct
- Two types of errors
 - Radiometric (covered in 5B)
 - Geometric

GEOMETRIC CORRECTION

Image Rectification

- All remote sensing images are subject to some form of geometric distortions, variety of factors:
 - the perspective of the sensor optics,
 - the motion of the scanning system,
 - the motion and (in)stability of the platform,
 - the platform altitude, attitude, and velocity,
 - the terrain relief, and
 - the curvature and rotation of the Earth.

Geometry Errors

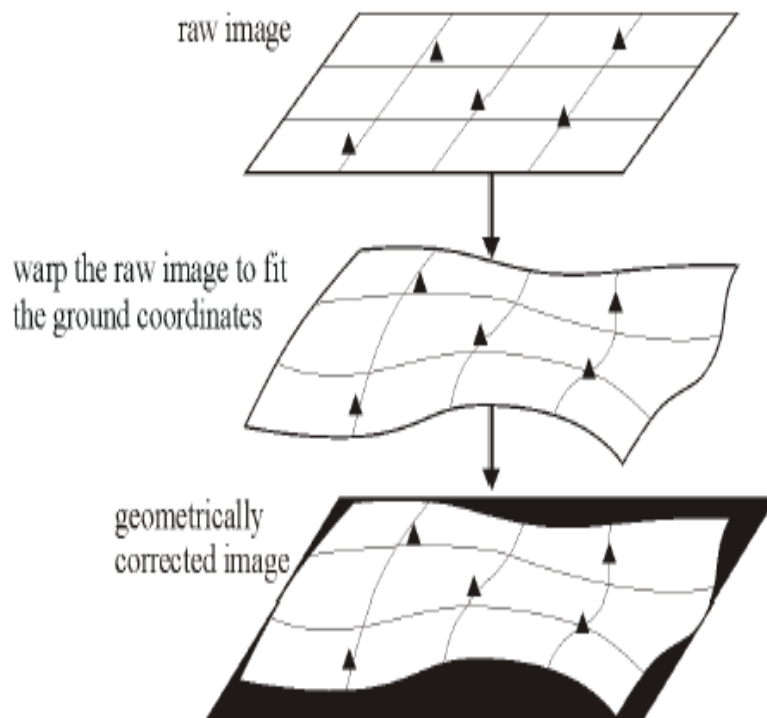
- Systematic errors
 - can be calculated and corrected using software without operator input
 - eg sensor geometry errors
- Non-systematic errors
 - are removed using Geometric rectification
 - e.g. sensor attitude / altitude

Geometric rectification

- an operator identifies known *control points*
 - on the source image using map coordinates
 - image to map
 - another image's coordinates
 - image to image
- process is often known as *warping*

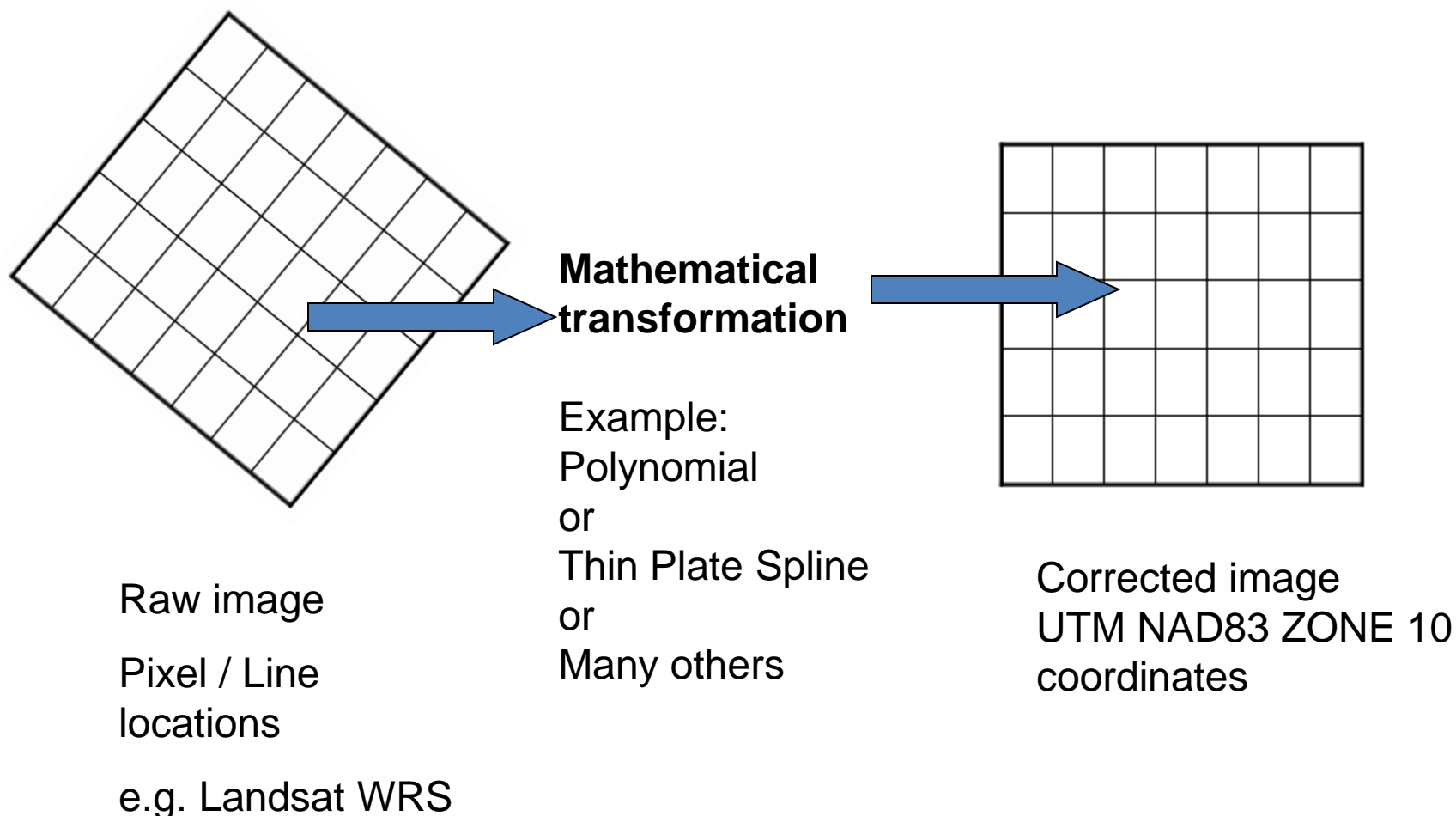
Two step process

Figure 8.2: The process of geometric correction

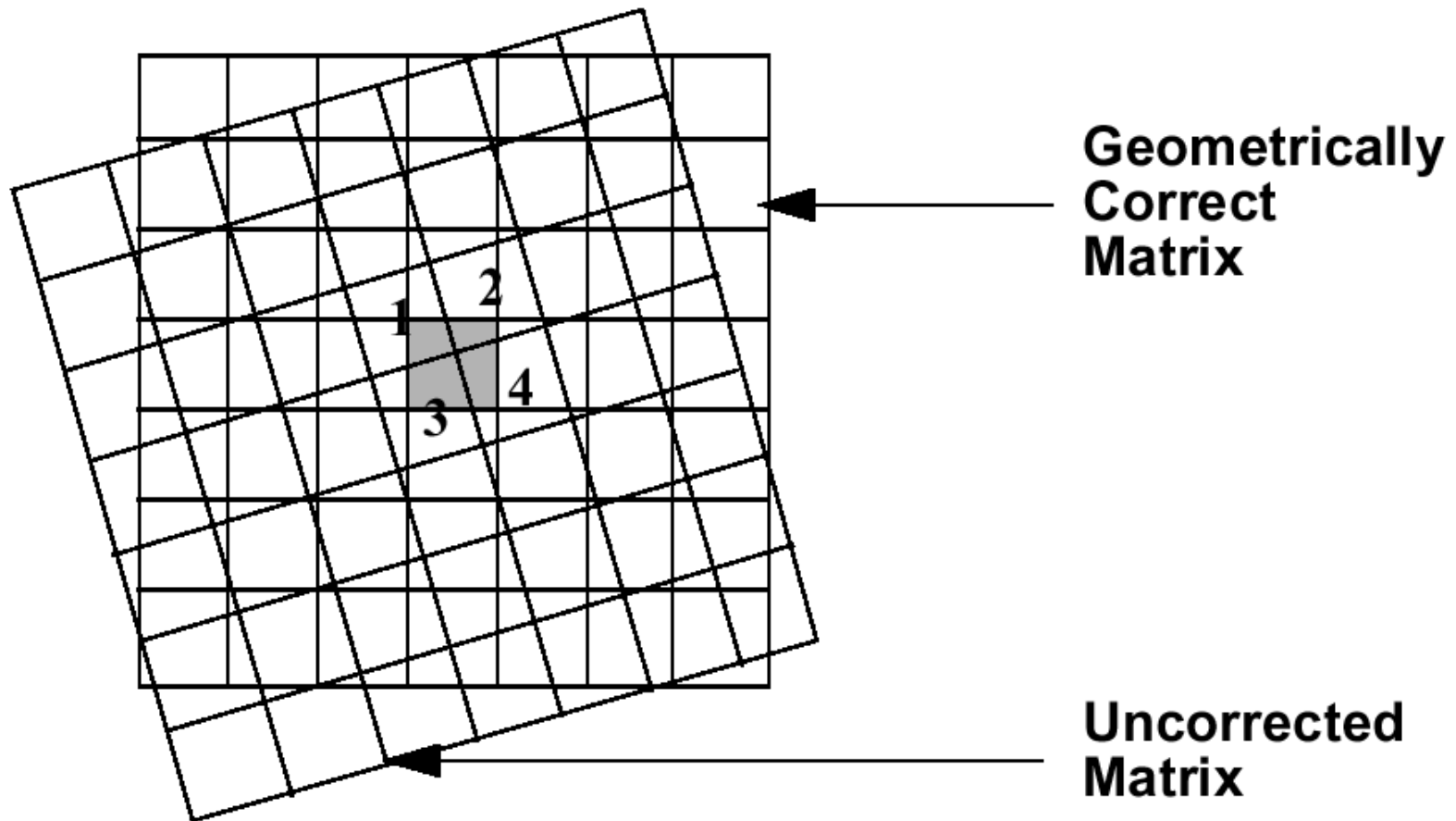


- Step 1: transformation of pixel coordinates
 - Determine transformation equation for pixel line location to georeferenced location
- Step 2: resampling
 - Determine the pixel value (DN) for each pixel in the corrected image

Step 1: Transformation of Pixel Coordinates



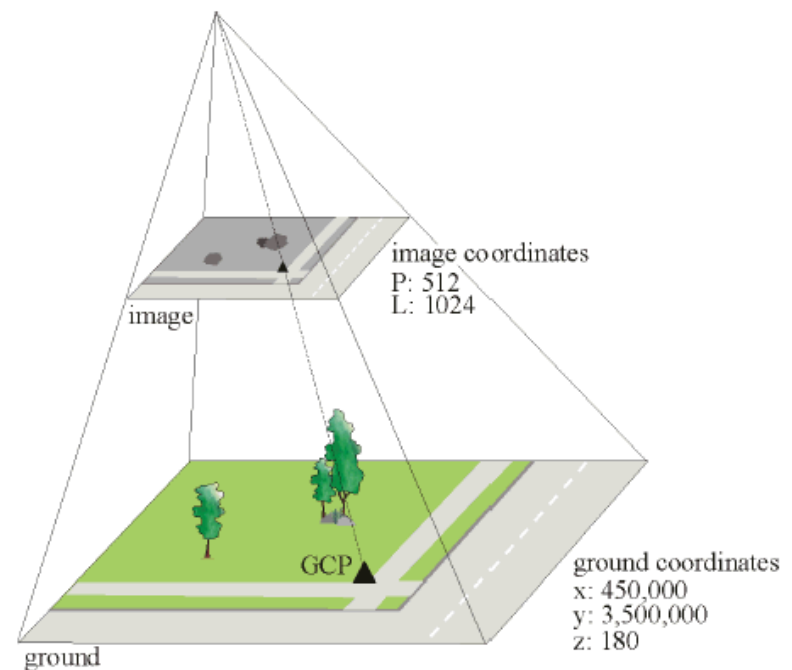
Transformed GRID



Mathematical Transformation

- Require
 - ground control points (GCP)
 - Pair of recognizable locations
 - One must have real world coordinate locations

Figure 5.1: The relationship between the ground coordinate system and the image coordinate system





- Polynomial equations fitted to GCP with least squares
 - also known as least square linear regression,
 - a line is fitted through a bunch of points
- 1st , 2nd, 3rd order transformations can be selected
- Depends on number of GCP and desired accuracy
- Website to view different polynomial equations
 - <http://zonalandeducation.com/mmts/functionInstitute/polynomialFunctions/graphs/polynomialFunctionGraphs.html>
- Good for images with high relief (mountains)

Transformation

- Want:
 - the best fit
 - between the image coordinates and the geo coordinates
- Find this by:
 - least-squares criteria
 - sum of the differences squared between each calculated geo coordinate and the actual geo coordinate for each control point
- Residual error
 - RMS

Finding a Transformation Equation

- GCP = two sets of coordinates
 - x_1, y_1 = image and x, y = geo coordinates
- Need a minimum of 3 GCPs
- Using the equations (1st order)
 - $X_1 = a_1X + a_2Y + a_3$ $Y_1 = b_1X + b_2Y + b_3$
 - find the coefficients of these equations
($a_1, a_2, a_3, b_1, b_2, b_3$) and the transformation is found.
 - a_1 = x scale a_2 = rotation
 - a_3 = translate b_1 = rotation
 - b_2 = y scale b_3 = translate

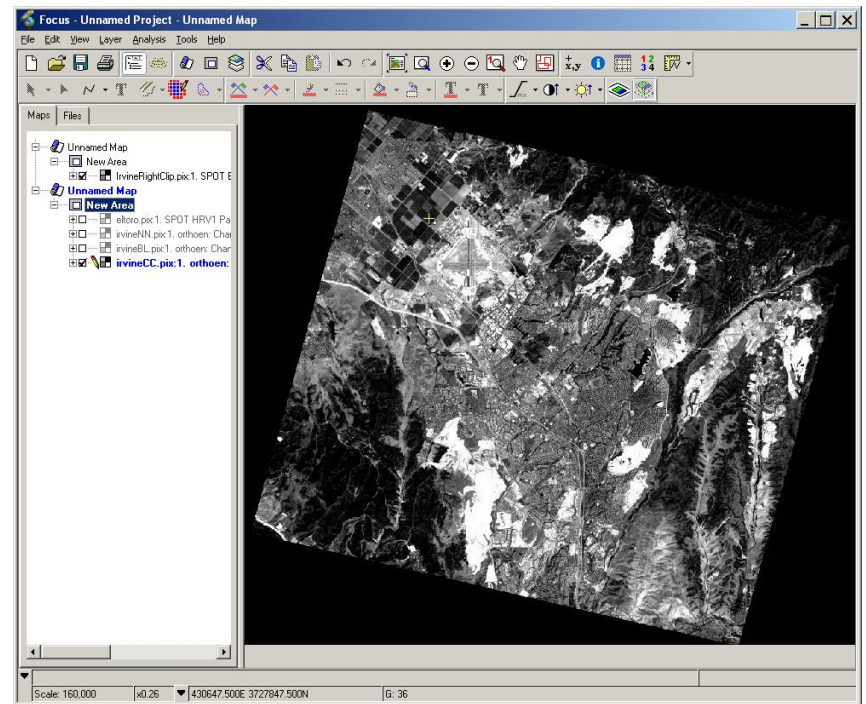
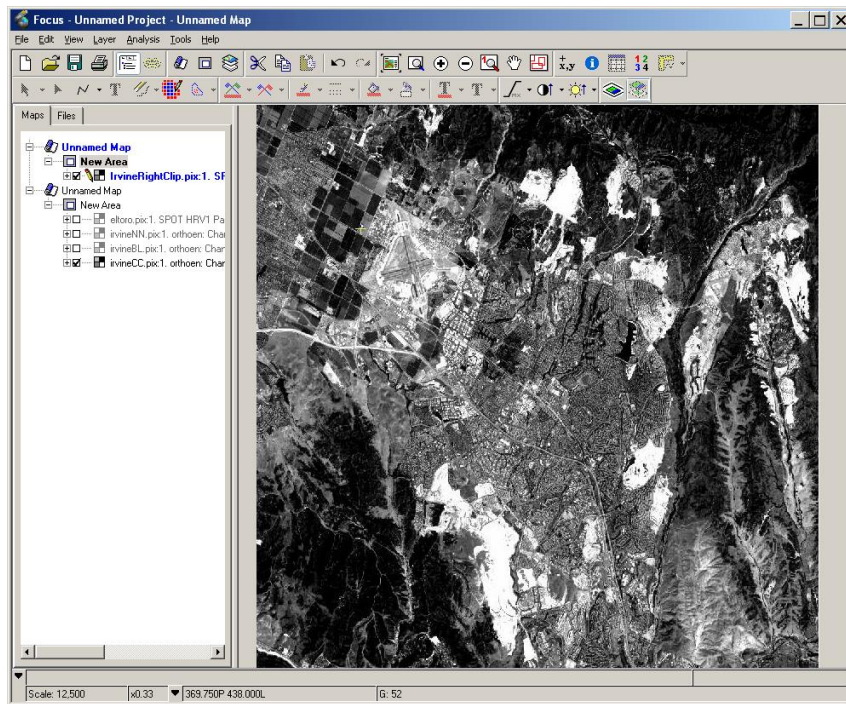
Thin Plate Spine

- All GCPs are used simultaneously to derive the transformation
- Derived functions have minimum curvature between control points
- Good for flat areas
- Not good in images with high relief

After Correction GRIDS are *different*

Original (clipped to look square)
Pixel/Line space

Corrected (black outline – *no data* in original) UTM space



Step 2 - Resampling

- Determine pixel values (DN) for new image
- for each new image row,col the equations are used to find the uncorrected image row,col
 - only the values calculated using the transformation will not be integers
 - Will not fit exactly at a row/col location
- decide what DN should be put into the new image using one of three interpolation methods
 - Nearest neighbour interpolation
 - Bilinear interpolation
 - Cubic convolution interpolation

Resample DN

- Find location in uv space for xy space (centre of pixel)
- Not exact match
 - (uv space not exactly centre)
- Need to determine the DN to enter in xy space

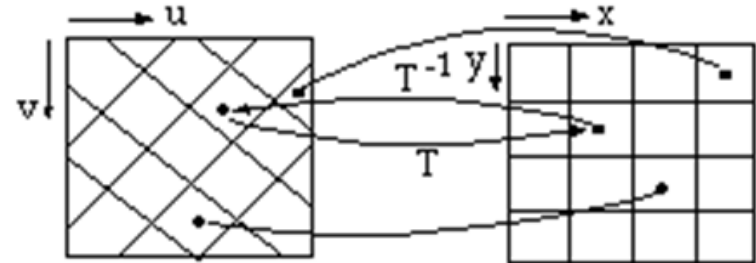


Image source

<http://www.cnr.berkeley.edu/~gong/textbook/chapter4/html/sect44.htm> 19

Resampling Example

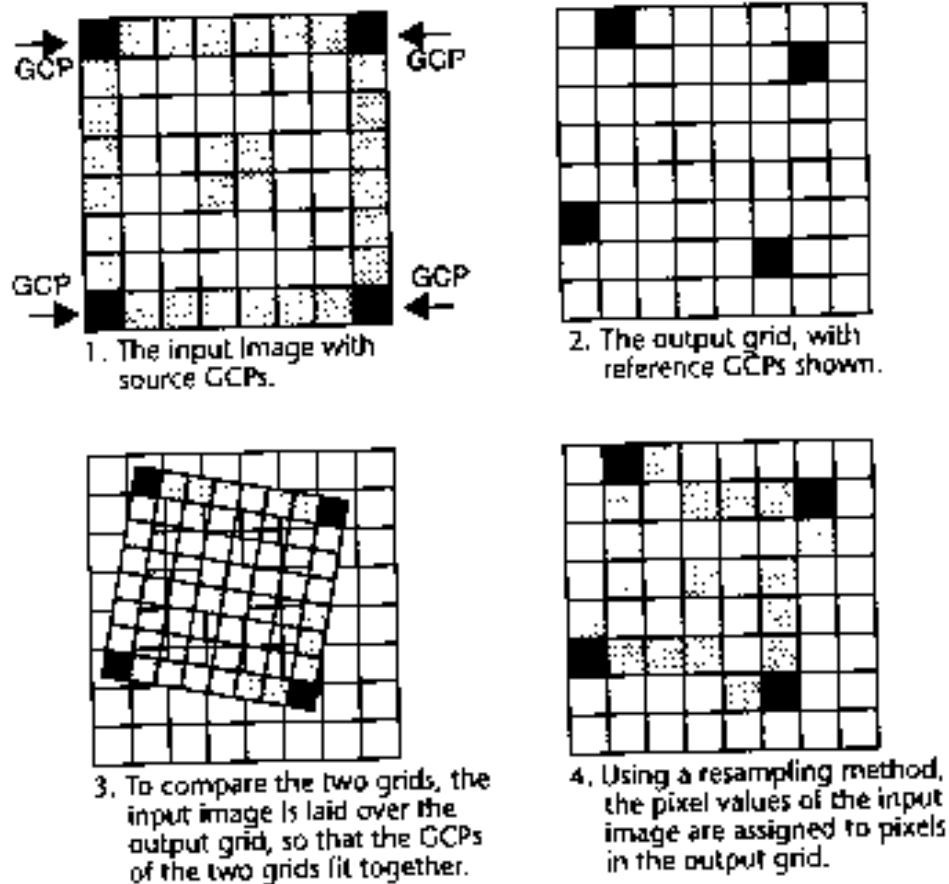
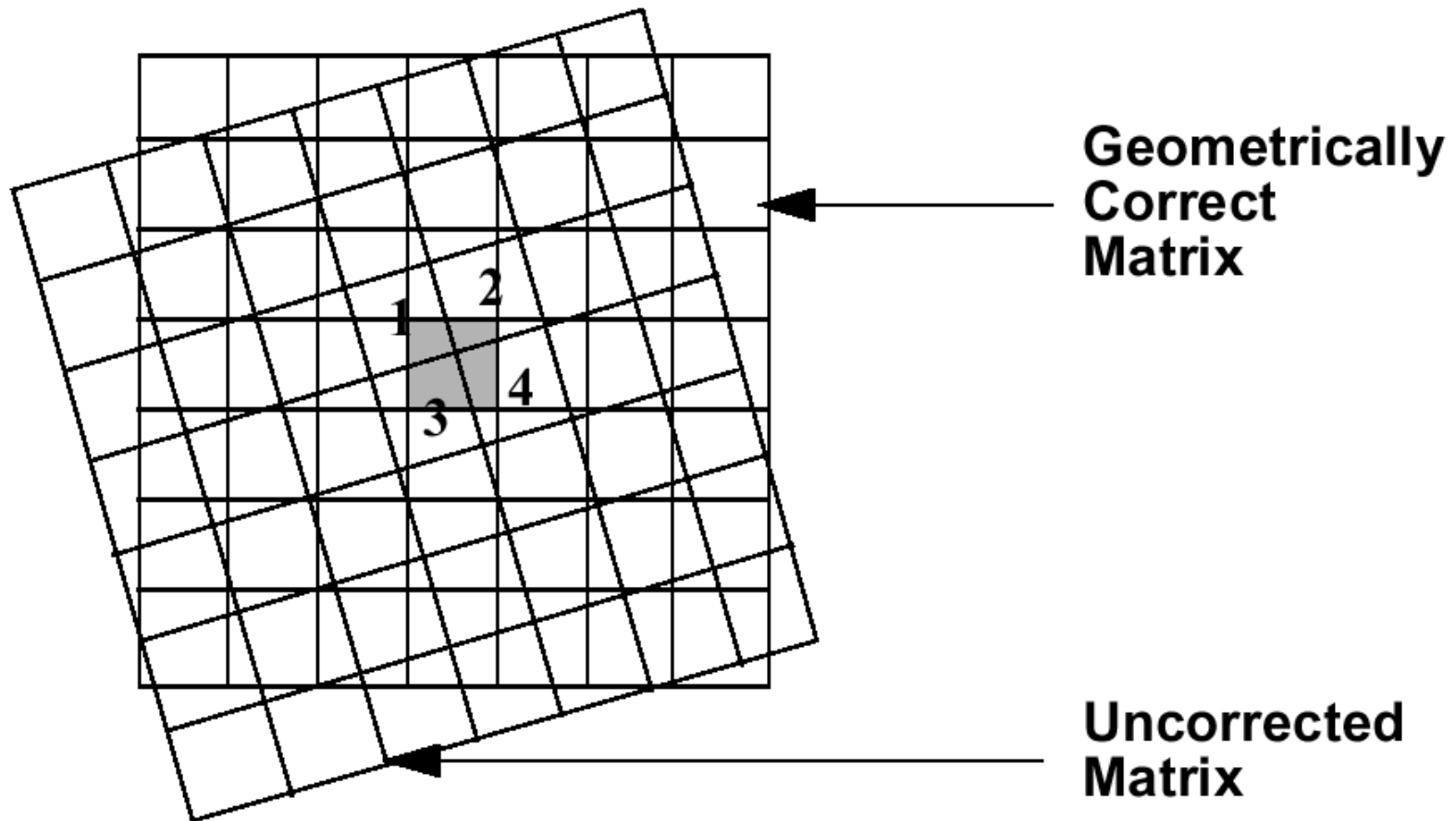


Figure 14: Resampling

Determine the new DN



Nearest neighbour interpolation

- Just take closest pixel DN
- Advantages
 - no change in pixel DN
 - good if you classify
 - Fast
 - Can use on GIS data
 - ie classified rasters
- Problems
 - May lose or duplicate pixels
 - Not smooth - can get a staircase effect

Bilinear interpolation

- Use the four nearest pixels DN around the calculated location
- Average their values weighted by their distance from the calculated value Bilinear interpolation
- Advantage:
 - Smoother output
 - Accurate representation
- Disadvantage:
 - is slower than nearest neighbour
 - modifies image DN to new values

Bilinear calculation

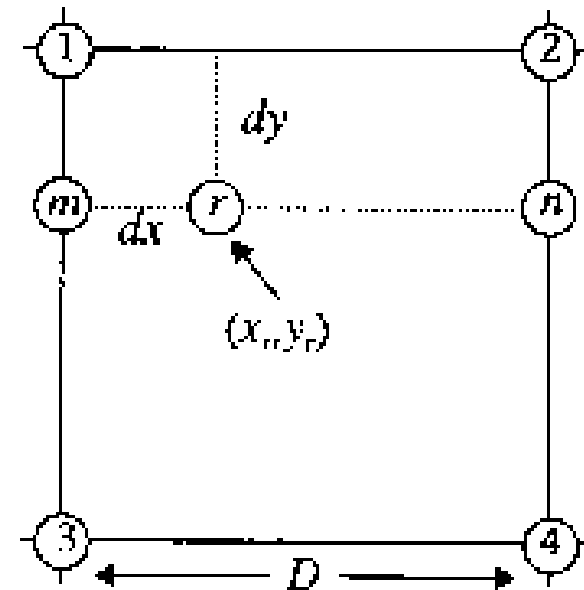
$$BV_{wt} = \sum_{k=1}^4 (Z_k / D_k^2) / \sum_{k=1}^4 (1 / D_k^2)$$

where :

BV_{wt} = weighted average of new brightness

D = distance from point to data point

Z = the surrounding data point values



r is the location of the retransformed coordinate

Figure 16: Bilinear Interpolation

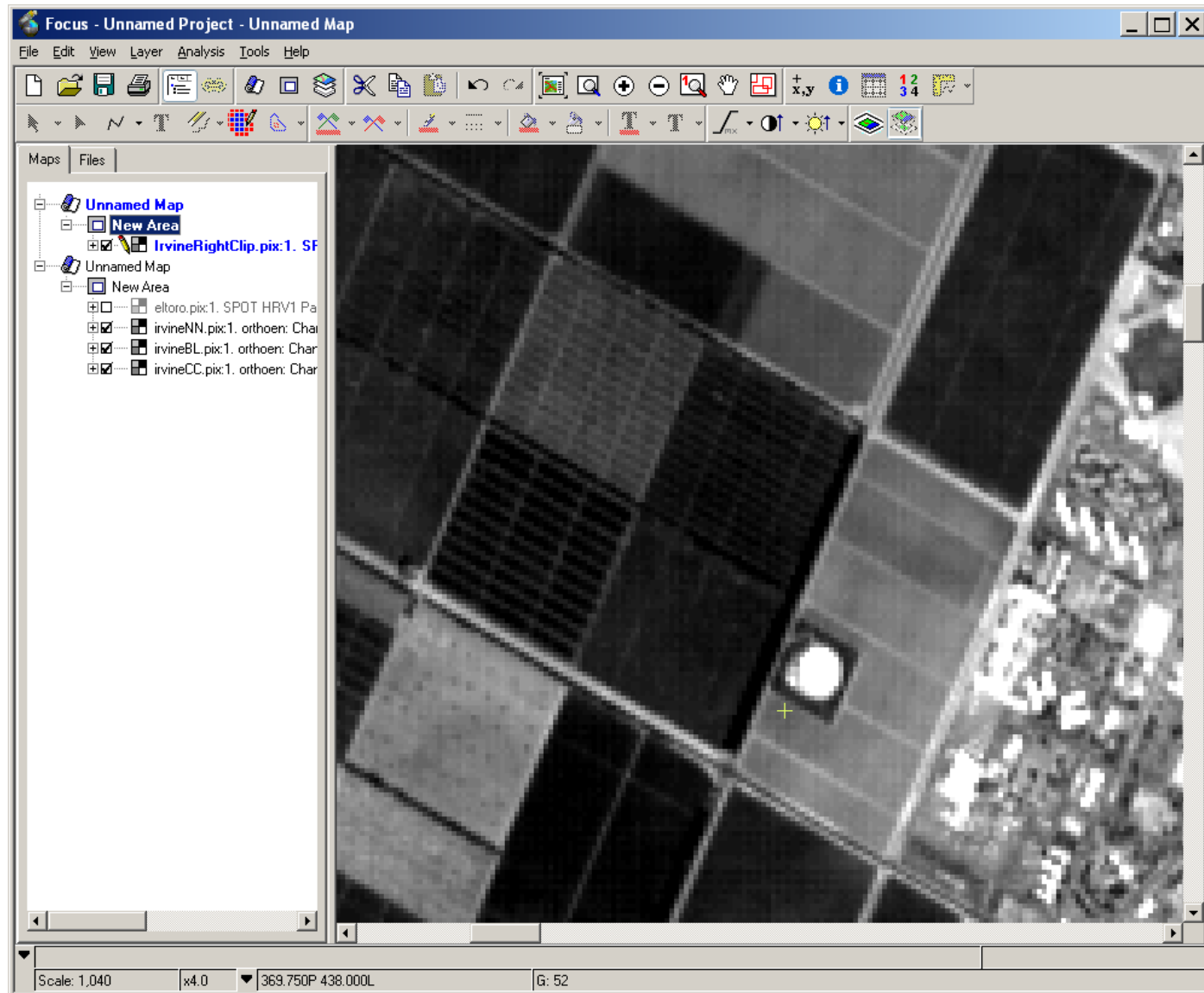
Cubic convolution interpolation

- Uses the 16 nearest pixel DN around the calculated value
- Use a cubic equation to find 4 new pixel values, then another cubic equation to find the required pixel value
- Cube function used to weight the input values pixels further away have exponentially less weight
- Advantage
 - accurate matching of input/output pixel values
 - Useful if a major grid size change is needed
- Disadvantage
 - Slow
 - Alters DN values

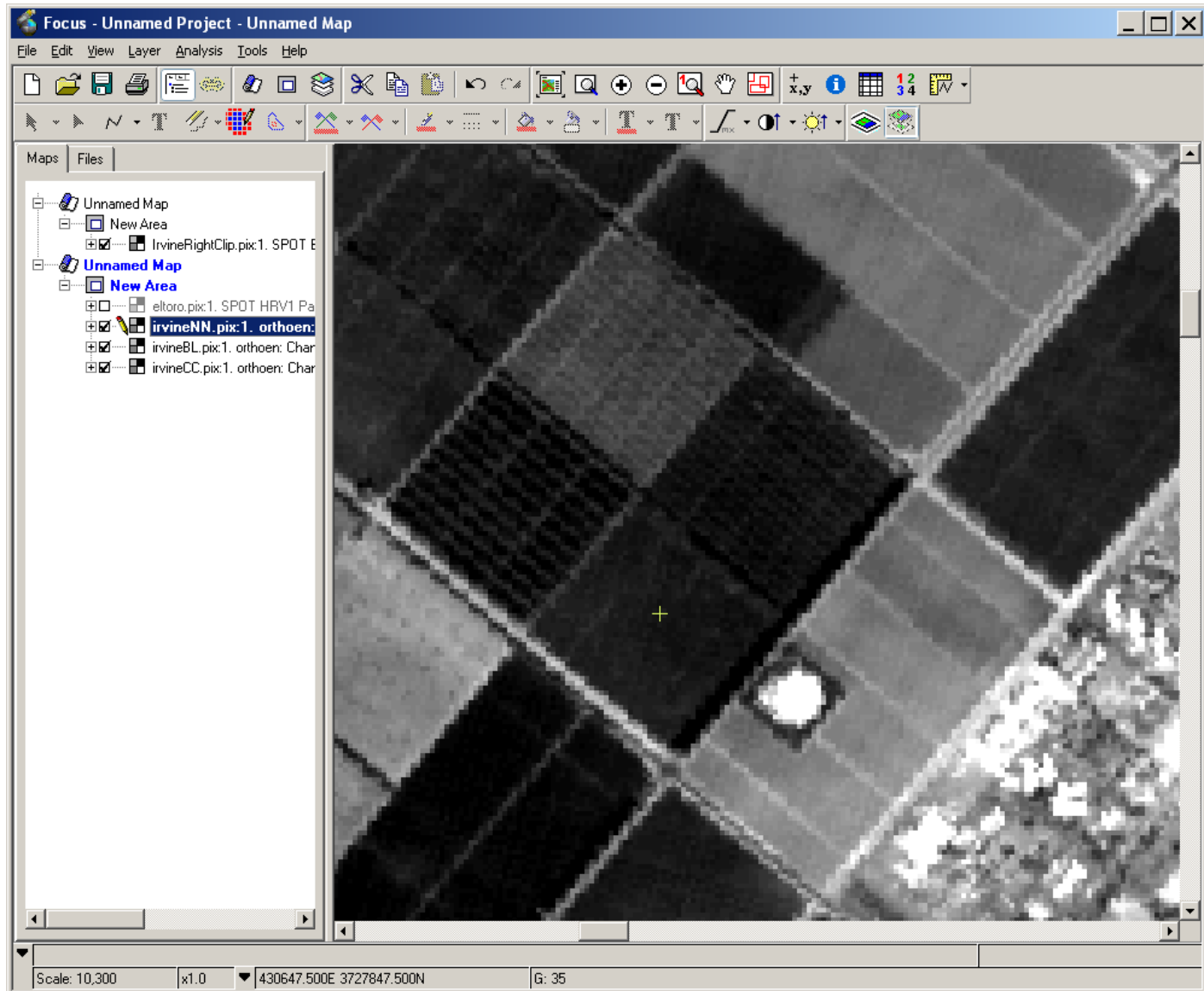
Compare three methods

Method	Technique	Advantages	Disadvantages
Nearest Neighbour	Transfer grey level of nearest pixel	Simple and grey levels unaltered	Image blocky; pixels may be offset by up to half a pixel
Bi-Linear Interpolation	Transfer proximity weighted average of 4 nearest pixels	Smoother and more accurate image than NN	Grey values are altered; some blurring and slower than NN
Cubic Convolution	Transfer evaluated weight of 16 nearest pixels	Very smooth image and most accurate	Grey values are altered and slower method

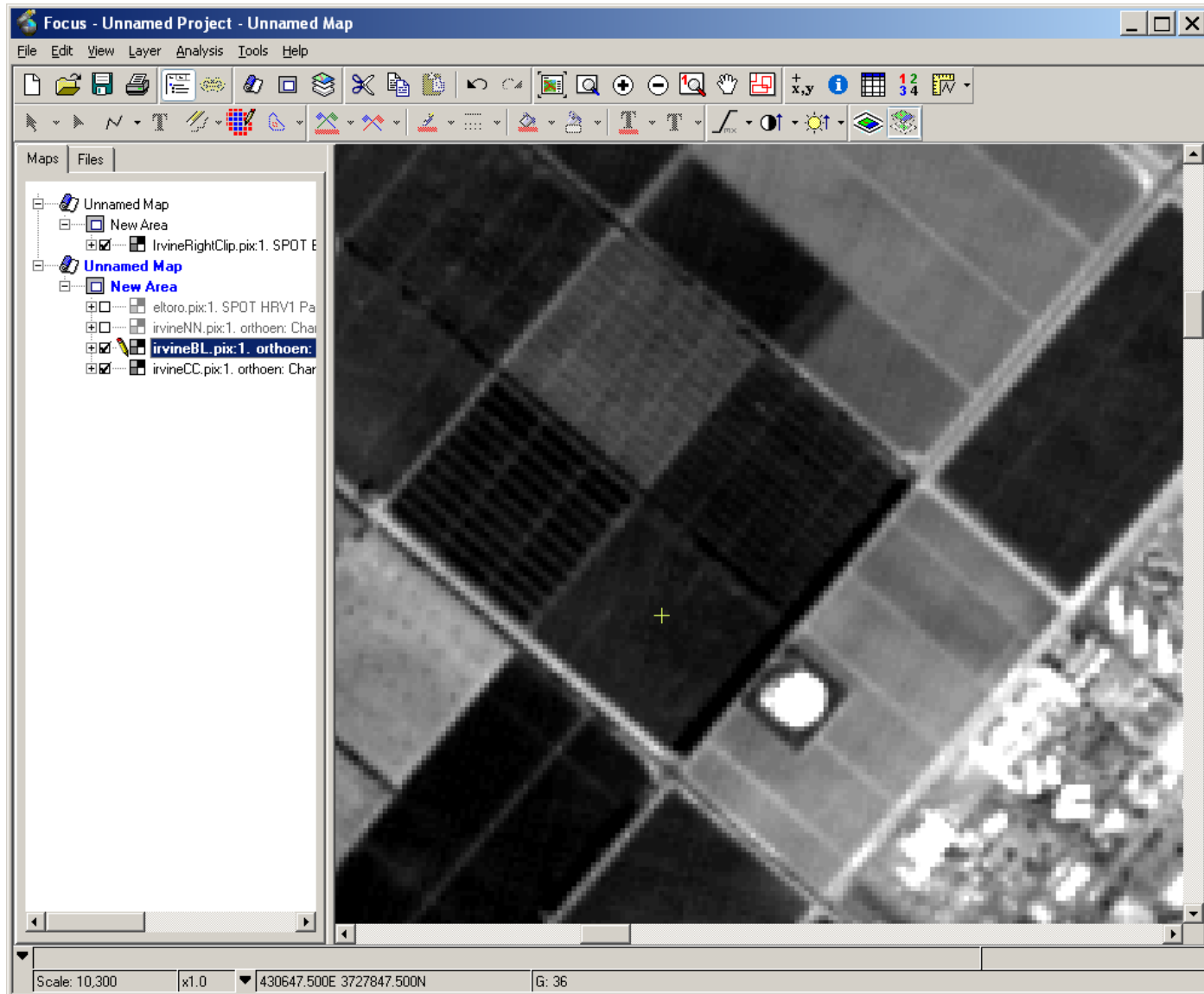
Original



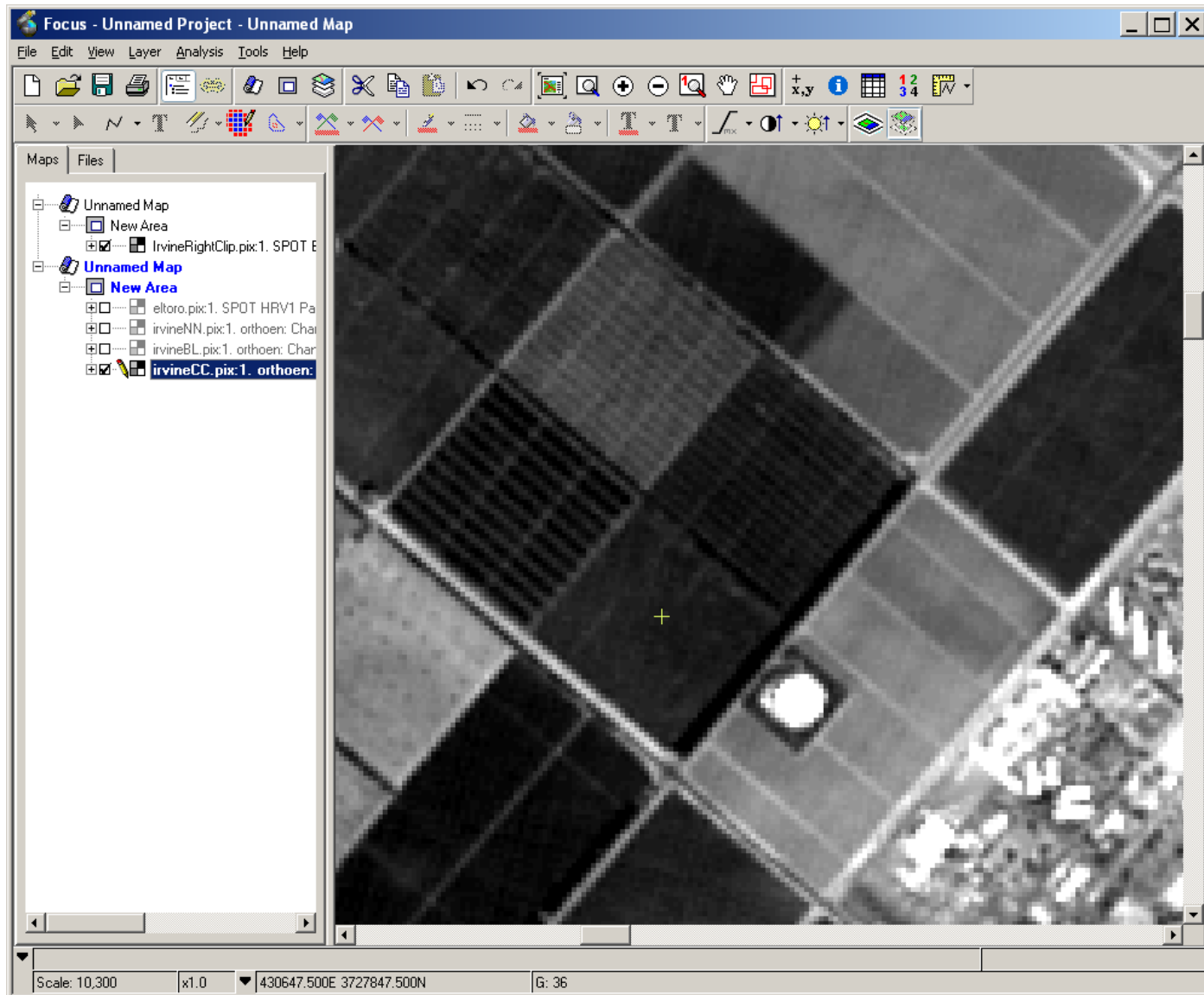
NN

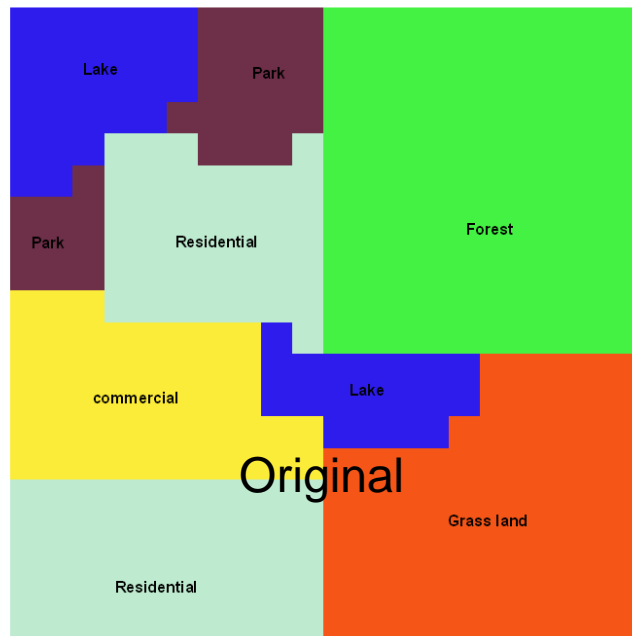


Bi-Linear

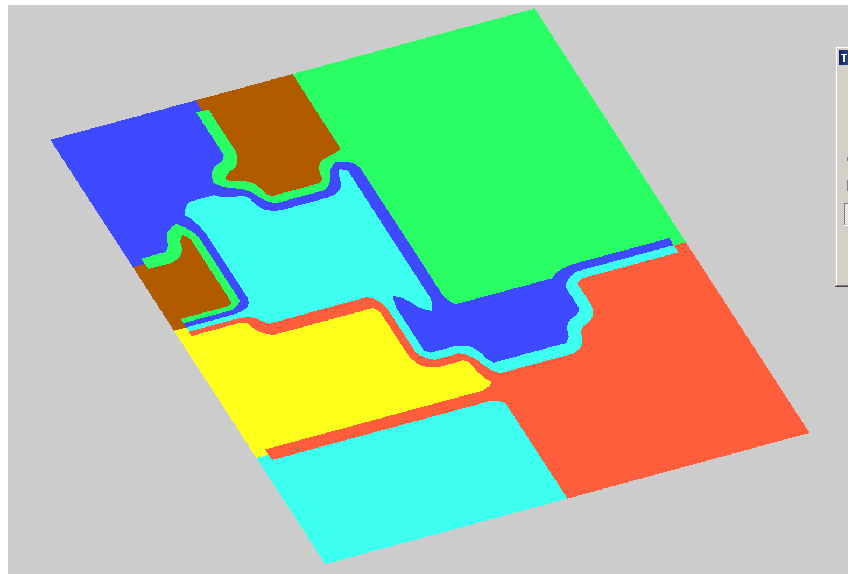
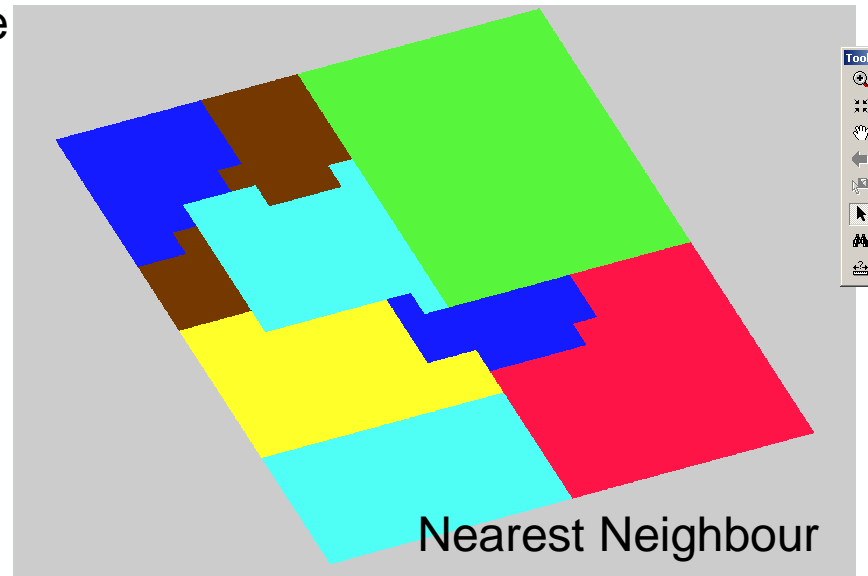


Cubic

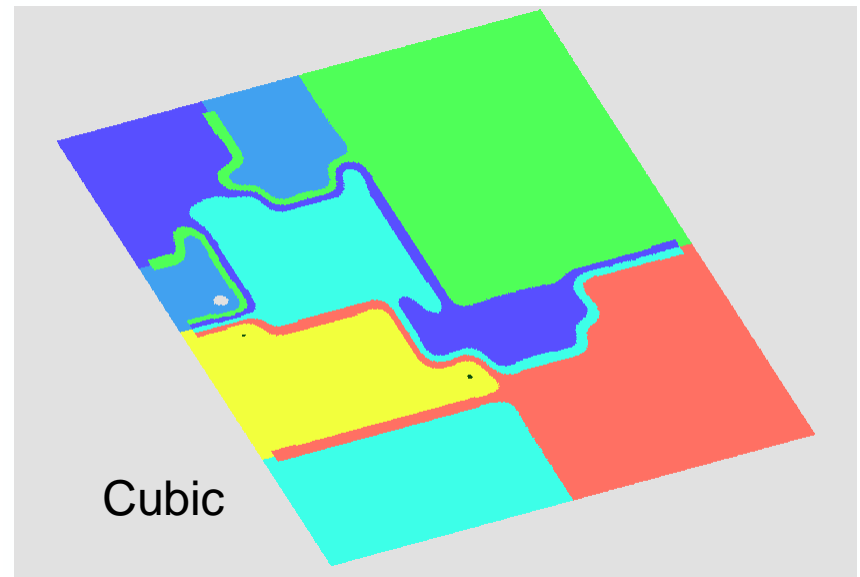




Resample
with
classified
data



Bi-Linear



Cubic

- End of lecture
- On to practical Exercises.