

* the parameter :-

$$t=7, b=7, r=3, k=3$$

λ = no of blocks in which a pair of treatment occurs together.

$$\lambda = \frac{r(k-1)}{t-1} \Rightarrow \frac{3(3-1)}{7-1} = \frac{6}{6} = 1$$

Hypothesis :-

$$H_0: \quad$$

$$H_1: \quad$$

$$H_0^2: \quad$$

$$H_1^2: \quad$$

$$CF = \frac{G^2}{n} = \frac{Y_{..}^2}{b \times k} \Rightarrow \frac{(2715)^2}{7 \times 3} = \frac{7371225}{21}$$

$$CF = 351010.7143$$

Total sum of squares TSS

$$TSS = \sum_i \sum_j Y_{ij}^2 - CF$$

$$= 353611 - 351010.7143$$

$$TSS = 2600.2857$$

Blocks S.S (unadjusted)

$$BSS = \frac{\sum Y_{.j}^2}{k} - CF$$

$$= \frac{1056375}{3} - CF$$

$$BSS = 3527 - 1114.2857 //$$

Adjusted treatment totals

$$Q_i^0 = Y_i^0 - \frac{1}{K} \left(\sum_{j=1}^b I_{ij}^0 Y_{.j} \right)$$

where $I_{ij}^0 = \begin{cases} 1, & \text{if } i\text{th treatment appears in } j\text{th block} \\ 0, & \text{otherwise} \end{cases}$

$$Q_1 = 351 - \frac{1}{3} (1 \times 381 + 381 + 378)$$

$$Q_1 = -29$$

$$Q_2 = 365 - \frac{1}{3} (1 \times 381 + 402 + 372)$$

$$Q_2 = -20$$

$$Q_3 = 388 - \frac{1}{3} (1 \times 402 + 366 + 378)$$

$$= 6$$

$$Q_4 = 419 - \frac{1}{3} (1 \times 381 + 366 + 435)$$

$$Q_4 = 25$$

$$Q_5 = 438 - \frac{1}{3} (1 \times 402 + 435 + 381)$$

$$Q_5 = 32$$

$$Q_6 = 361 - \frac{1}{3}(1 \times 366 + 381 + 372)$$

$$Q_6 = -12$$

$$Q_7 = -2$$

\therefore adjusted treatments

$$T_{SS \text{ adj}} = \frac{K \sum Q_i^2}{\lambda t}$$

$$= \frac{3 \times 2963074}{1 \times 7}$$

$$= \frac{888}{7} = 1317.43$$

$$\text{unadjusted } T_{SS} = \frac{\sum Y_{ij}^2}{r} - CF$$

$$= \frac{1059145}{3} - 35100.7143$$

$$\text{unadjusted } T_{SS} = 2037.6190$$

$$ESS = T_{SS} - B_{SS}(\text{unadjusted}) - T_{SS}(\text{adjusted})$$

$$= 2600.2857 - 1114.2857 - 1317.43$$

$$ESS = 168.58$$

ANOVA.

d.f	S.S	MSS	F-ratio
$t-1=6$	1317.43	219.571	10.4197
$b-1=6$	1114.2857	185.7142	

$$(20-1) - (4-1) - (6-1) = 8$$

$$bK-1 = 20$$

$$168.58$$

$$2600.2857$$

$$21.0725$$

$$130.0142$$

$$F_{cal} > F_{0.05}(6,8)$$

$$F_{cal} > 3.58$$

$$10.4197 > 3.58$$

\therefore we reject H_0 , hence all concentrations are not same.

$$BSS(Adj) = TMS(Adj) + BSS(unaadjusted) - TMS(unaadj) = 394.0967$$

ANOVA.

d.f.	S.S	MSS	F-ratio
6	2037.6190	339.6031	
6	394.08	65.68	3.11
8	168.58	21.0725	
20	2600.2857	130.014	

$$F_{cal} > F_{0.05}(6,8)$$

$$F_{cal} > 3.58$$

$$3.11 < 3.58$$

\therefore we do not reject H_0 .
 \therefore all days are same.

H_0^1 : all concentration (treatments) are same

H_1^1 : all concentration are not same.

H_0^2 : all days (blocks) are same

H_1^2 : all days (blocks) are not same

$$S.E(\bar{X}_i - \bar{X}_j) = \sqrt{\frac{2KMSSE}{\lambda t}} = \sqrt{\frac{2KMSSE}{\lambda t}}$$

$$\sqrt{\frac{2 \times 3 \times 21.0725}{1 \times 7}} = \sqrt{18.0621}$$

$$S.E(\bar{Q}_1 - \bar{Q}_0) = 4.211$$

③. Model :-

$$Y_{ijk} = \mu + \alpha_i + \beta_j + \delta_k$$

where, $\alpha_i =$, $\beta_j =$

$i = 1, \dots, t$

$j = 1, \dots, b$

$k = 1, \dots, \gamma$

Assumptions :-

Q.1) α_i 's, β_j 's & δ_k 's are fixed effect
 $\epsilon_{ijk} \sim N(0, \sigma^2)$

Hypothesis :-

H_0^1 : The four manual treatment are same

H_1 : The four manual treatment are not same.

H_0^2

H_1^2

$$\lambda = \frac{2(k-1)}{t-1} = \frac{3(3-1)}{4-1} = \frac{6}{3} = 2$$

H_0^3

H_1^3

$$t = 4, b = 4, \gamma = 3, K = 3, n = t \times b \times \gamma = 12$$

Treatments			
A	B	C	D
432	442	540	
468	490	562	340
568	584	556	384
1468	1516	1658	526
			1250

$$CF = \frac{G^2}{n} = \frac{34715664}{12} = 2892972$$

$$TSS = \sum \sum y_{ijk}^2 - CF$$

$$= 2961104 - CF$$

$$TSS = 68132$$

$$RSS = \sum \frac{Y_{..k}^2}{b} - CF$$

$$RSS = 30150$$

$$BSS(\text{unadj}) = \sum \frac{y_{.ij}^2}{k} - CF$$

$$BSS(\text{un}) = 11150.666$$

adjusted treatment totals

$$Q_i^0 = y_{i..} - \sum \frac{u_{ij}^0 y_{.j.}}{k}, \quad i=1, \dots, t$$

where $u_{ij}^0 = \begin{cases} 1, & \text{if } i\text{th treatment appears in block } j \\ 0, & \text{o.w} \end{cases}$

$$Q_1 = 1468 - \frac{(432 + 468 + 568)}{3} = 1468 - 486.67 = 981.33$$

$$Q_1 = 22.67$$

$$Q_2 = 9.33$$

$$Q_3 = 1658 - \frac{(1372 + 1572 + 1556)}{3}$$

$$Q_3 = 158$$

$$Q_4 = 1250 - \frac{(1372 + 1556 + 1392)}{3}$$

$$Q_4 = -190$$

adjusted T.S. is 24)

$$T_{adj} = \frac{k}{\lambda t} \sum_{i=1}^t Q_i^2$$

$$= \frac{3}{2 \times 4} \times 61664.9778$$

$$T_{adj} = 23124.3666$$

$$ESS = TSS - (RSS)_{unadj} - T_{adj} - RSS$$

$$= 68132 - 11150.666 - 23124.366 - 30150$$

$$ESS = 3706.974$$

ANOVA

Source	d.f.	S.S.	M.S.	F-ratio
Treat (adj)	4-1=3	23124.366	7708.122	6.23
Residual	3-1=2	30150	15075	
Block (unadj)	4-1=3	11150.66	3716.88	
Error	(3+2+3-11)=3	3706.974	1235.658	
Total	4-1=11	68132		

$F_{cal} > F_{\alpha}(1, 3)$
 $6.23 > 9.28$

\therefore we do not reject H_0 .

The four manual treatments are same.

$$\begin{aligned}
 S.E(\hat{\alpha}_i - \hat{\alpha}_j) &= \sqrt{\frac{2K MSSE}{\lambda t}} \\
 &= \sqrt{\frac{2 \times 3 \times \frac{1}{2} \times \frac{35.638}{108.125}}{2 \times 4}} \\
 &= \sqrt{\frac{5.78109}{2}} = \sqrt{2.890545} = 1.700154 \\
 S.E(\hat{\alpha}_i - \hat{\alpha}_j) &= 30.44 //
 \end{aligned}$$

② ANOVA TABLE

S.V.	d.f.	Sum of S	M.S	F value	P-value
Treat	4	7.6133	1.9033	3.1263	0.04445
Block	9	3.5124	0.39027	0.6410	0.74734
Residual	16	9.7409	0.60881		

Hypothesis

H_0 : Treatment effects are same v/s

H_1 : Treatment effects are not same.

Conclusion :- $F_1 = 3.1263$
 $F_1 > F_{cal}$

$$3.12637, F_2(4,16)$$

$$3.12637, 3.01$$

Hence we reject H_0 , Hence all the treatment effect are not same.

$$F_2 > F_{cal}$$

$$0.6410 > F(9,16)$$

$$0.6410 > 2.54$$

we do not reject H_0 , Hence all the treatment effect are same.

P-4

(1)
(i)

the model is

$$y_{ij}^0 = \mu + \alpha_i^0 + \beta(x_{ij}^0 - \bar{x}_{..}) + \varepsilon_{ij}^0 \quad \begin{matrix} i=1, \dots, t \\ j=1, \dots, r \end{matrix}$$

where

y_{ij}^0 :- value of observation for the j th response variable for the i th treatment

μ :- overall mean

α_i^0 :- i th treatment effect

β :- linear regression coefficient of Y on X

x_{ij}^0 :- j th observation on the covariate for the i th treatment.

$\bar{x}_{..}$:- sample mean of x observations

ε_{ij}^0 :- random errors.

assumptions

$$\varepsilon_{ij}^0 \sim N(0, \sigma^2)$$

$$\sum \varepsilon_{ij}^0 = 0$$

calculation

$$\sigma = 5, t = 3, n = \sigma \times t = 5 \times 3 = 15$$

$$X_{..} = 185$$

$$Y_{..} = 714.9$$

$$CF_{xx} = \frac{X_{..}^2}{n} = \frac{185^2}{15} = 2281.666$$

$$CF_{yy} = \frac{Y_{..}^2}{n} = \frac{714.9^2}{15} = 34072.134$$

$$CF_{xy} = \frac{X_{..} Y_{..}}{n} = \frac{185 \times 714.9}{15} = 8817.1$$

$$TSS_{xx} = \sum \sum X_{ij}^2 - CF_{xx} = 2317 - 2281.666$$

$$TSS_{xx} = 35.334$$

$$TSS_{yy} = \sum \sum Y_{ij}^2 - CF_{yy}$$

$$TSS_{yy} = 49.296$$

$$TSS_{xy} = \sum \sum X_{ij} Y_{ij} - CF_{xy}$$

$$= 8783.4 - CF_{xy} = -33.7$$

$$T_{r.s.s}_{\frac{y}{x}} = \frac{\sum Y_{ij}^2}{t} - CF_{yy} =$$

$$= \frac{102263.52}{3} - 34072.134 = 15.706$$

$$T_{x,SSx} = \frac{\sum X_i^2}{2} - CF_{xx}$$

$$= \frac{11427}{5} - 2281.666$$

$$= 1527.334 - 3.734$$

$$T_{x,SSy} = \frac{\sum X_i \cdot Y_i}{2} - CF_{xy}$$

$$= \frac{44056.3}{5} - CF_{xy}$$

$$= -5.84$$

$$E_{yy} = T_{SSyy} - T_{x,SSyy}$$

$$= 49.296 - 15.706$$

$$= 33.59$$

$$E_{xx} = T_{SSxx} - T_{x,SSxx}$$

$$= 35.334 - 3.734$$

$$= 31.6$$

$$E_{xy} = T_{SSxy} - T_{x,SSxy}$$

$$= -33.7 - (-5.84)$$

$$= -27.86$$

(ii) Hypothesis

$$H_0: \beta = 0 \quad \text{vs} \quad H_1: \beta \neq 0$$

H_0 : there is no effect of covariate.

H_1 : the effect of covariate is there

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$$SSE = E_{yy} - \frac{E_{xy}^2}{E_{xx}} \Rightarrow 33.159 - \frac{(-27.86)^2}{31.6}$$

$$= 33.15 - 24.5626$$

$$SSE = 8.5874$$

$$MSE = \frac{SSE}{n-t-1} = \frac{8.5874}{15-3-1} = 0.78$$

$$F_{cal} = \frac{E_{xy}^2 / E_{xx}}{MSE} \sim F_{(1, n-t-1)}$$

$$= \frac{24.5626}{0.78} \sim F_{(1, 11)}^{(0.05)}$$

$$= 31.49$$

$$\therefore F_{(1, 11)}^{(0.05)} = 4.84$$

$$\therefore F_{cal} > F_{tab}$$

$$31.49 > 4.84$$

Conclusion

\therefore we reject H_0

\therefore the effect of covariate is there.

(ii) $H_0: \alpha_1 = 0 \quad \forall i \neq 1$ ^{not} significant.
~~Use the glue formulations are~~
 H_0 : there is no significant difference in the glue formations.

$H_1: \alpha_1 \neq 0$
 there is a significant difference in glue formations.

$$\begin{aligned}
 SSE' &= TSS_{YY} - \frac{TSS_{XY}^2}{TSS_{XX}} \\
 &= 49.296 - \frac{(-33.7)^2}{35.334} \\
 &= 49.296 - 32.1415 \\
 SSE' &= 17.1545
 \end{aligned}$$

$$F_0 \frac{(SSE' - SSE) / (t-1)}{MSE} \sim F(t-1, n-t-1)$$

$$F_0 = \frac{(17.1545 - 8.5874) / 3-1}{0.78}$$

$$F_0 = \frac{4.28355}{0.78} = 5.491$$

$$F(t-1, n-t-1) \Rightarrow F(3-1, 15-3-1) \Rightarrow F(2, 11) = 3.98$$

ANOVA Table

$$\therefore F_{cal} > F_{tab}$$

$$\therefore 5.491 > 3.98$$

\therefore we reject H_0
 \therefore there is a significant difference in glucose formation.

ANCOVA Table.

Sum of Squares and
Cross Products.

	x	xy	y	d.f	adjusted treatment SS for regression	MSS	F
Treat	3.734	-5.84	15.706	1	SSE = 8.5874	0.78	F ₀ = 5.49
Error	31.6	-27.86	33.15	4-1=3	SSE = 17.1545		
Total	35.334	-33.7	49.296	4-2=2	Tot SS = SSE + SSE = 4.28355		
				t-1=2			

(10) SE of $\text{adj}(\bar{y}_{i.} - \bar{y}_{j.}) = \sqrt{MSE \left(\frac{2}{8} + \frac{\bar{x}_{i.} - \bar{x}_{j.}}{E_{xx}} \right)}$

$\bar{y}_{i.} \rightarrow$ 1 treatment mean.
 $\bar{y}_{j.} \rightarrow$ 2 treatment mean.

$$= \sqrt{MSE \left(\frac{2}{5} + \frac{6}{31.6} \right)}$$

$$= 0.68$$

Q. The linear model is,

$$y_{ij} = \mu + \alpha_i + \beta_j + \gamma_{ij} + \beta(x_{ij} - \bar{x}_{..}) + \epsilon_{ij}$$

$i = 1, \dots, t$
 $j = 1, \dots, b$

where, $\gamma_{ij} =$, $\mu =$, $\alpha_i =$, $\beta_j =$, $\beta =$, $\epsilon_{ij} =$

Hypothesis.

$H_0: \beta = 0$ vs $H_1: \beta \neq 0$

408 $n = 3, b = 4, n = cb = 12.$

$$CF_{xx} = \frac{X_{..}^2}{n} = \frac{290^2}{12} = 7008.33$$

$$CF_{yy} = \frac{Y_{..}^2}{n} = \frac{483^2}{12} = \frac{233289}{12} = 19440.75$$

$$CF_{xy} = \frac{X_{..}Y_{..}}{n} = \frac{290 \times 483}{12} = \frac{140070}{12} = 11672.5$$

$$TSS_{xx} = \sum \sum X_{ij}^2 - CF_{xx} \\ = 7262 - CF_{xx} = 253.67$$

$$TSS_{yy} = \sum \sum Y_{ij}^2 - CF_{yy}$$

$$TSS_{yy} = 19781 - 19440.75 = 340.25$$

$$TSS_{xy} = \sum \sum X_{ij}Y_{ij} - CF_{xy} \\ = 11949 - 11672.5$$

$$TSS_{xy} = 276.5$$

$$Tr_{yy} = \frac{\sum Y_{i.}^2}{b} - CF_{yy}$$

$$= \frac{78597}{4} - 19440.75$$

$$= 19649.25 - 19440.75$$

$$Tr_{yy} = 208.5$$

$$Tr_{xx} = \frac{\sum X_{i.}^2}{b} - CF_{xx} \Rightarrow$$

$$Tr_{xx} = \frac{28468}{4} - CF_{xx} = 7117 - CF_{xx} = 108.67$$

$$T_{xy} = \frac{\sum x_i \cdot y_i}{n} - CF_{xy} = \frac{47292}{4} - CF_{xy}$$

$$T_{xy} = 11823 - CF_{xy} \Rightarrow 150.5 //$$

$$B_{yy} = \frac{\sum y_i^2}{n} - CF_{yy} = \frac{520952463}{3} - CF_{yy}$$

$$= 19487.666 - CF_{yy}$$

$$B_{yy} = 46.9166$$

$$B_{xx} = \frac{\sum x_i^2}{n} - CF_{xx} = \frac{21146}{5} - CF_{xx} = 40.33$$

$$B_{xy} = \frac{\sum x_i \cdot y_i}{n} - CF_{xy}$$

$$= \frac{35140}{3} - 11672.5 = 11713.33 - CF_{xy}$$

$$B_{xy} = 40.833 //$$

$$E_{yy} = TSS_{yy} - TSS_{yy} - B_{yy}$$

$$= 340.25 - 208.5 - 46.9166$$

$$= 84.8334$$

$$E_{xx} = TSS_{xx} - TSS_{xx} - B_{xx}$$

$$= 253.67 - 108.67 - 40.33$$

$$= 104.67$$

$$E_{xy} = TSS_{xy} - TSS_{xy} - B_{xy}$$

$$= 276.5 - 150.5 - 40.833$$

$$= 85.167$$

$$\beta^1 = \frac{E_{xy}}{E_{xx}} = \frac{85.167}{104.67} = 0.8136 //$$

P-2

the model.

$$y_{ij}^0 = \mu + \alpha_i + \beta_j + \varepsilon_{ij}^0 \quad \begin{matrix} i=1, \dots, t \\ j=1, \dots, b \end{matrix}$$

$$\alpha_i^0 = \quad, \quad \beta_j = \quad, \quad \varepsilon_{ij}^0$$

Assumptions

— u —

Hypothesis :-

$$H_0^1 = \alpha_1 = \alpha_2 = \dots = \alpha_t = 0$$

$$H_1^1 = \text{(unreliable)}$$

$$H_0^2 = \beta_1 = \beta_2 = \dots = \beta_b = 0$$

$$H_1^2 =$$

estimate the missing observation:

$$\hat{y}_{ij}^1 = \frac{t y_{i.} + b y_{.j} - y_{..}}{(b-1)(t-1)}$$

where,

$y_{i.}$ = sum of known observations for i^{th} .

$y_{.j}$ = sum of known observation for j^{th} .

$y_{..}$ = sum of all known observations

Given, $b=4$, $t=3$

$$\hat{y}_{22}^1 = \frac{3(109.4) + 4(58.7) - 377}{3 \times 2}$$

$$g'_{22} = \frac{186}{6}$$

$$g'_{22} = 31$$

	A	B	C	Σy_2
1	32.4	35.6	38.7	106.7
2	29.9	31	29.9	89.7
3	36.5	37.6	29.1	103.2
4	34.4	36.2	37.8	108.4
Σy_2	132.1	140.4	135.5	

$$C.F = \frac{Y_{..}^2}{b \times c} = \frac{(408)^2}{4 \times 3} = \frac{166464}{12} = 13872$$

$$SST_y = \frac{\sum Y_{ij}^2}{b} - C.F$$

$$= \frac{132.1^2 + 140.4^2 + 135.5^2}{4} - C.F$$

$$= 13880.705 - 13872$$

$$SST_y = 8.705$$

$$SSB = \frac{\sum Y_{.j}^2}{b} - C.F$$

$$= \frac{(106.7^2 + 89.7^2 + 103.2^2 + 108.4^2)}{3} - C.F$$

$$TSS =$$

$$SSB = 13943.9266 - 13872$$

$$SSB = 71.926$$

$$SST = \sum y_i^2 - CF$$

$$= 14014.72 - 13872$$

$$SST = 142.72$$

$$SSE = TSS - (SST_y + SSB)$$

$$= 142.72 - 8.705 - 71.926$$

$$SSE = 62.089$$

ANOVA TABLE

SV	d.f	S.S.	MSS	F-ratio
Treatment	$t-1 = 2$	8.705	4.3525	0.3505
Block	$b-1 = 3$	71.926	23.9753	1.93072
Error	$(t-1)(b-1) = 5$	62.089	12.4178	
Total	$bt-2 = 10$	142.72	14.272	

For treatment: $F_{0.05}(2,5)$
 $F_{cal} > F_{0.05}(2,5)$
 $0.3505 > 5.79$

\therefore we don't reject H_0 for treatment
Hence μ 's differ significantly

Find value

$$F_{(1, 10)} = 5.101$$

$$F_{(1, 10)} = 5.101$$

$$F_{(1, 10)} = 5.101$$

in the next step we have

Hence $F_{(1, 10)} = 5.101$

standard error of difference between means

$$SE(\bar{Y}_A - \bar{Y}_B) = \sqrt{\frac{1.455}{10}}$$

$$= \sqrt{\frac{1.455}{10}}$$

$$= \sqrt{\frac{1.455}{10}}$$

$$= \sqrt{0.1455}$$

$$SE(\bar{Y}_A - \bar{Y}_B) = 0.381$$

and error of difference between means

$$SE(\bar{Y}_A - \bar{Y}_B) = \sqrt{\frac{1.455}{10}}$$

$$= \sqrt{0.1455}$$

$$SE(\bar{Y}_A - \bar{Y}_B) = 0.381$$

$$\frac{1}{2^2(2-1)}$$

$$= \frac{(3.86)^2}{2^2(2-1)}$$

$$\lambda = \frac{\delta(k-1)}{(l-1)}$$

$$\lambda = \frac{\delta(4-1)}{(4-1)}$$

②. LSD.
are missing observations.

$$y_{ijk}^{(0)} = \frac{m(y'_{i..} + y'_{.j.} + y'_{.k.}) - 2(y'_{...} + \text{initial estimate})}{(m-1)(m-2)}$$

$$y^{(0)} = \frac{\sum y'_{i..}}{m-1}$$

	A	B	C	D	E	F	
	92	220	160	149	282	98	
	74	213.15	228	168	238	282	445.15
	119.5	176	276.9	188	278	118	
	64	222	213	104	295	163	
	66	188	187	90	242	96	
	124	109	195	79	211	90	
$y'_{i..}$	420	915	1262	778	1546	847	
	530.5	1123.15					
	220	98	149	92	282	160	$y'_{.j.}$
	74	238	213.15	228	282	168	990
	188	279	118	278	176	119.5	1639
	295	222	64	104	213	163	1061
	187	90	242	96	66	188	869
	90	124	195	109	79	211	808
$y'_{.k.}$	1054	1051	768	907	1098	890	1009.5
			781.15				

test
result
19.37, df = 10, p-value < 2.2e-16

$$SS_{w/c} = \frac{(386)^2}{2^2(2-1)} = \dots$$

For missing value of A,

$$\hat{y}_{ijk}^1 = \frac{6(420 + 1039 + \cancel{768} + 890) - 2(5768 + 84)}{5 \times 4}$$

$$= \frac{11362 - 11704}{20}$$

$$\hat{y}_{ijk}^1 = \cancel{82.4} \frac{2390}{20}$$

$$\hat{y}_{A36} \hat{y}_{ijk}^1 = 119.5$$

For missing value of B,

$$\hat{y}_{ijk}^1 = \frac{6(915 + 768 + 990) - 2(5768 + 119.5)}{20}$$

$$= \frac{16038 - 11775}{20}$$

$$\hat{y}_{B23} = 213.15 //$$

A	B	9	20	E	WF
92	220	160	149	6	✓

$$CF = \frac{\sum \sum y_{ij.}^2}{m \times r} = \frac{(6100.65)^2}{6 \times 6} = 1033831.401$$

$$SST = \sum \sum \sum y_{ijk}^2 - CF$$

$$= (220^2 + 984 + \dots + 211^2) - CF$$

$$= (61077.925 + 472808.25 + 274693) - CF$$

$$= 1208579.173 - 1033831.401$$

$$\lambda = \frac{0.1}{(6-1)}$$

$$SST = 174747.7715$$

$$SSR = \frac{\sum y_j^2}{m} - CF$$

$$= \frac{6325439.173}{6} - CF$$

$$= 1054239.862 - 1033831.401$$

$$SSR = 20408.46108$$

$$SSC = \frac{\sum y_{..k}^2}{m} - CF$$

$$= \frac{6225515.573}{6} - CF$$

$$= 1037585.929 - CF$$

$$SSC = 3754.5277$$

$$SSt_r = \frac{\sum y_{i..}^2}{m} - CF$$

$$= \frac{6869235.673}{6} - CF$$

$$= 1144872.612 - 1033831.401$$

$$SSt_r = 111041.211$$

$$SSE = SST - SSR - SSC - SSt_r$$

$$= 174747.7715 - 20408.46108 - 3754.5277 - 111041.211$$

$$SSE = 39543.57162$$

S.V
treatment
low
within
Error
total

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del



$$SS_{w/t} = \frac{(SP6)^2}{2^2(2-1)} = \dots$$

$$TSS = \dots$$

ANOVA TABLE

S.V	d.f.	S.S	MSS	F-ratio
treatment	$t-1=5$	111041.2111	22208.24222	70.20182
row	$r-1=5$	20408.46108	4081.6922	12.9025
column	$c-1=5$	3754.5277	750.90554	2.37366
Error	$(t-1)(r-1)(c-1)=125$	39543.57162	316.3485	
Total	$t \times r \times c - 2 = 214$	174747.7715	816.5783	

Row: Since, $12.9025 > 4.39$, we ~~reject~~ H_0 ,
 Column: Since, $2.37 < 4.39$ we don't reject H_0
 Treatment: Since, $70.2018 > 4.39$ we reject H_0 .

P-3

i) the linear model

$$Y_{ij} = \mu + \alpha_i + \beta_j + \varepsilon_{ij} \quad \begin{matrix} i=1, \dots, t \\ j=1, \dots, b \end{matrix}$$

where,

Y_{ij} : observations for i th treatment in the j th block if it exists.

$$\mu = \text{grand mean}, \quad \alpha_i = \text{treatment effect}, \quad \beta_j = \text{block effect}, \quad \varepsilon_{ij} = \text{error}$$

Assumption

same as RBD - u - u -

hypothesis and parameters:-

1. ε_{ij} 's are i.i.d random variables with $N(0, \sigma^2)$ dist.
2. Treatment & block effects are fixed effects
3. All the observations are independent.

$$\lambda = \frac{\sigma^2(k-1)}{(t-1)}$$