

## Task 2.2)

$$S_{xx}(t_1, t_2) = \sum_{x(t_2)=x_j} \sum_{x(t_1)=x_i} x_i \cdot x_j \cdot P(x(t_1)=x_i | x(t_2)=x_j) \cdot P(x(t_2)=x_j)$$

- $x(z_0, t_1) = -1, x(z_1, t_2) = 2, P(z_0) = 1/2$   
 $x(z_1, t_1) = 3, x(z_1, t_2) = 1, P(z_1) = 1/3$   
 $x(z_2, t_1) = 1, x(z_2, t_2) = -1, P(z_2) = 1/6$

- Determine  $P(x(t_2)=x_j)$ :

$$P(x(t_2)=2) = P(z_0) = 1/2$$

$$P(x(t_2)=1) = P(z_1) = 1/3$$

$$P(x(t_2)=-1) = 1/6$$

- Determine  $P(x(t_1)=x_i | x(t_2)=x_j)$ :

Conditional probability is 1, if  $x(t_1)=x_i$  and  $x(t_2)=x_j$  and 0 otherwise.

$$S_{xx}(t_1, t_2) = \cancel{0.02.01.0.0.0.0}$$

$$x(z_0, t_1) \cdot x(z_0, t_2) \cdot 1 \cdot P(z_0) +$$

$$x(z_1, t_1) \cdot x(z_1, t_2) \cdot 1 \cdot P(z_1) +$$

$$x(z_2, t_1) \cdot x(z_2, t_2) \cdot 1 \cdot P(z_2) =$$

$$-1 \cdot 2 \cdot \frac{1}{2} + 3 \cdot 1 \cdot \frac{1}{3} - 1 \cdot 1 \cdot \frac{1}{6} = -\frac{1}{6}$$