
Formulas for exercises:

- **Single line:** $R = R_{cond}$ $L = 0.2 \ln \frac{GMD}{GMR} [mH / km]$ $C = \frac{1000}{18 \ln \frac{GMD}{r_{cond}}} [nF / km]$ $GMD = \sqrt[3]{d_{AB} d_{BC} d_{CA}}$ $GMR = k_g r_{cond}$

- **Double line:** $R = \frac{R_{cond}}{2}$ $L = 0.2 \ln \frac{GMD}{GMR} [mH / km]$ $C = \frac{1000}{18 \ln \frac{GMD}{R_{eq}}} [nF / km]$ $GMD = \sqrt[3]{GMD_{AB} GMD_{BC} GMD_{CA}}$

$GMD_{ij} = \sqrt[4]{\prod d_{i-j}}$ $GMR = \sqrt[3]{GMR_A GMR_B GMR_C}$ $GMR_i = \sqrt[3]{k_g r_{cond} d_{i-i'}}$ $R_{eq} = \sqrt[3]{R_{eqA} R_{eqB} R_{eqC}}$ $R_{eqi} = \sqrt[3]{r_{cond} d_{i-i'}}$

- **Bundle line:** $R = \frac{R_{cond}}{n}$ $L = 0.2 \ln \frac{GMD}{GMR} [mH / km]$ $C = \frac{1000}{18 \ln \frac{GMD}{R_{eq}}} [nF / km]$

$GMD = \sqrt[3]{d_{AB} d_{BC} d_{CA}}$ $GMR = \sqrt[n]{n k_g r_{cond} r_{bundle}^{n-1}}$ $r_{bundle} = \frac{d_{bundle}}{2 \sin \frac{\pi}{n}}$ $R_{eq} = \sqrt[n]{n r_{cond} r_{bundle}^{n-1}}$

- **Transmission equation:** $\begin{pmatrix} \underline{V}_{in(s)} \\ \underline{I}_{in} \end{pmatrix} = \begin{pmatrix} \underline{A}_{11} & \underline{A}_{12} \\ \underline{A}_{21} & \underline{A}_{22} \end{pmatrix} \cdot \begin{pmatrix} \underline{V}_{out(s)} \\ \underline{I}_{out} \end{pmatrix}$

$\underline{S}_{out} = 3 \underline{V}_{out(s)} \underline{I}_{out}^* = \sqrt{3} \underline{V}_{out(l)} \underline{I}_{out}^* = P_{out} + jQ_{out}$ $\underline{S}_{in} = 3 \underline{V}_{in(s)} \underline{I}_{in}^* = \sqrt{3} \underline{V}_{in(l)} \underline{I}_{in}^* = P_{in} + jQ_{in}$

$\Delta V = \frac{V_o - V_f}{V_{ref}} 100$ $PF = \frac{P}{S}$ $\eta = \frac{P_{out}}{P_{in}} 100$ $\underline{V} = V \angle \alpha$ $\underline{V}_{(l)} = \sqrt{3} \underline{V}_{(s)}$

Long line	Medium line	Short line
$\underline{A}_{11} = \underline{A}_{22} = \cosh(\underline{\Theta})$	$\underline{A}_{11} = \underline{A}_{22} = 1 + \frac{\underline{Z}_t \underline{Y}_t}{2}$	$\underline{A}_{11} = \underline{A}_{22} = 1$
$\underline{A}_{12} = \underline{Z}_c \sinh(\underline{\Theta})$	$\underline{A}_{12} = \underline{Z}_t$	$\underline{A}_{12} = \underline{Z}_t$
$\underline{A}_{21} = \frac{\sinh(\underline{\Theta})}{\underline{Z}_c}$	$\underline{A}_{21} = \underline{Y}_t + \frac{\underline{Y}_t^2 \underline{Z}_t}{4}$	$\underline{A}_{21} = 0$
$\underline{Z}_c = \sqrt{\frac{\underline{Z}}{\underline{Y}}} = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$	$\underline{Z}_t = (R + j\omega L)l$	$\underline{Z}_t = (R + j\omega L)l$
$\underline{\Theta} = \beta l = l \sqrt{(R + j\omega L)(G + j\omega C)}$	$\underline{Y}_t = (G + j\omega C)l$	
$\underline{\beta} = \sqrt{\underline{Z} \underline{Y}} = \sqrt{(R + j\omega L)(G + j\omega C)}$		

NAME:

NIF:

The Power System – T3: Transmission and distribution of electricity**Exam 10/01/2017****Time: 17:00 – 17:55 h*****Part II: EXERCISES A (10 points)***

The power line of the figure is 200 km long and its rated voltage is 400 kV. Its conductor has the following characteristics: 54 Al + 7 Steel wires ($k_g=0,809$), outer diameter 30,42 mm, $R_{ca} = 0,062 \Omega/\text{km}$.

Calculate:

- The resistance, inductance and capacitance per length
- Its transmission matrix parameters
- The phase-to-phase voltage at the origin if the phase-to-phase voltage at the end is 395 kV when it is supplying a load of 200 MW with $\text{PF}=0,8$ (i).

