National University of Singapore School of Computing CS1010X: Programming Methodology Semester II, 2021/2022

Tutorial 2

Functional Abstraction, Recursion & Iteration

1. Define a function magnitude that takes in the coordinates of two points on a plane, (x1, y1) and (x2, y2), as arguments and returns the magnitude of the vector between them.

```
def magnitude(x1, y1, x2, y2):
    # Returns the magnitude of the vector
    # between the points (x1, y1) and (x2, y2).
>>> magnitude(2, 2, 5, 6)
5.0
```

- 2. A function can be viewed as a black box. All you need to know are the arguments it takes as input and what its output is.
 - (a) One way of calculating the area of a triangle is using the formula $area = \frac{1}{2} \times base \times height$.

Define a function area that calculates and returns the area of any given triangle using this formula.

Decide what arguments it requires as input and what its return value should be.

```
def area(<your arguments>):
    # Return area of the triangle using the formula
    # area = 1/2 * base * height.
```

(b) Another way of calculating the area of a triangle with sides A, B, C is using the trigonometric ratio sine to get $area = \frac{1}{2} \times A \times B \times sin(AB)$, where AB is the included angle between sides A and B.

The sin function is provided by the math package. You can call it by using sin after including the line from math import * at the top of your Python file. For information on how to use the math package, refer to

```
http://docs.python.org/3.6/library/math.html
```

Define a function area2 that calculates and returns the area of any given triangle using this formula.

Decide what arguments the function requires as input and what its return value should be.

```
def area2(<your arguments>):
    # Return area of the triangle using the formula:
    # area = 1/2 * A * B * sin(AB).
```

(c) Both functions calculate the same result. Can they be directly substituted for each other? Why?

(d) We can also calculate the area of triangle using Heron's Formula, $area = \sqrt{s(s-a)(s-b)(s-c)}$ where $s = \frac{a+b+c}{2}$. Assume you are given a function

herons_formula that takes 3 arguments a, b, c and returns the area of a triangle with sides of length a, b, c.

Define a function area3 that uses Heron's formula to calculate and return the area of a given triangle given the x,y coordinates of the 3 points of the triangle.

You may use the magnitude function defined in Question 1

```
def area3(x1, y1, x2, y2, x3, y3):
    # Return area of the triangle using Heron's formula.
```

3. For each of the questions below, what is printed when the expressions are evaluated?

```
(a) def foo1():
       i = 0
       result = 0
       while i < 10:
           result += i
           i += 1
       return result
   print(foo1())
(b) def foo2():
       i = 0
       result = 0
       while i < 10:
           if i == 3:
               break
            result += i
           i += 1
       return result
   print(foo2())
(c) def bar1():
       result = 0
       for i in range(10):
            result += i
       return result
   print(bar1())
(d) def bar2():
       result = 0
       for i in range(10):
           if i % 3 == 1:
               continue
            result += i
       return result
   print(bar2())
```

4. Write a function sum_even_factorials that finds the sum of the factorials of the even numbers that are less than or equal to n, where $n \ge 0$.

```
>>> sum_even_factorials(1)
1
>>> sum_even_factorials(3)
3
>>> sum_even_factorials(6)
747
```

5. Suppose we define the function:

```
def f(g):
    return g(2)

Then we have

def square(x):
    return x ** 2

>>> f(square)
4

>>> f(lambda z: z * (z + 1))
6
```

What happens if we (perversely) ask the interpreter to evaluate the combination f(f)? Explain.