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Hoja de Trabajo No. 1

① $\lim_{t \rightarrow 0} r(t) = \left\langle \frac{t+1}{t-1}, \frac{\sqrt{9+t}-3}{t}, t^3+1 \right\rangle$

Para $\uparrow \lim_{t \rightarrow 0} \frac{t+1}{t-1} = \frac{0+1}{0-1} = -1$

Para $\uparrow \lim_{t \rightarrow 0} \frac{\sqrt{9+t}-3}{t} = \lim_{t \rightarrow 0} \frac{\sqrt{9+t}-3}{t} \cdot \frac{\sqrt{9+t}+3}{\sqrt{9+t}+3} = \lim_{t \rightarrow 0} \frac{\sqrt{9+t}-3}{t} \cdot \frac{\sqrt{9+t}+3}{\sqrt{9+t}+3} = \lim_{t \rightarrow 0} \frac{9+t-9}{t(\sqrt{9+t}+3)} = \lim_{t \rightarrow 0} \frac{t}{t(\sqrt{9+t}+3)} = \lim_{t \rightarrow 0} \frac{1}{\sqrt{9+t}+3} = \frac{1}{1\sqrt{9+0}+3} = \frac{1}{6} = 0.16666$

$\lim_{t \rightarrow 0} t^3+1 = 0^3+1 = 1$

Para $\uparrow \lim_{t \rightarrow 0} t^3+1 = 0^3+1 = 1$

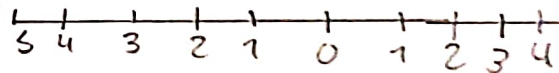
$\lim_{t \rightarrow 0} \langle -1, 0.1667, 1 \rangle$

② Dominio de $R(t) = \langle t \sin t \sin(t+1), \sqrt{6-t}, \cos(t-1) \rangle$

Para $\uparrow t \in \mathbb{R}$
en todos los reales

$\{t \mid t \in \mathbb{R}\}$
 $(-\infty, \infty)$

$\begin{matrix} -\infty & 1 & 0 & (\infty, \infty) \\ -\sqrt{6} & 0 & \sqrt{6} & (-\sqrt{6}, \sqrt{6}) \\ 0 & & & (-\infty, \infty) \end{matrix}$



Para $\uparrow \sqrt{6-t^2}$

$6-t^2 \geq 0$

$-t^2 \geq -6$

$t^2 \leq 6$

$t \leq \pm \sqrt{6}$

$-\sqrt{6} \leq t \leq \sqrt{6}$

$[-\sqrt{6}, \sqrt{6}]$

2.4498

$[-2.4498, 2.4498]$