

Ejercicio 5

Problema: Minimizar: $Z = 6x_1 + 7x_2$

Sa: $11x_1 + 13x_2 \geq 22$

$9x_1 - 16x_2 \geq 48$

$x_1, x_2 \geq 0$

Maximizar: $Z = 22y_1 + 48y_2$

Sa: $11y_1 + 9y_2 \leq 6$

$13y_1 - 16y_2 \leq 7$

$y_1, y_2 \geq 0$

Inicial

→

Base	Z	y_1	y_2	s_1	s_2	R
Z	1	-22	-48	0	0	0
s_1	0	11	9	1	0	6
s_2	0	13	-16	0	1	7

$y_1 = -22$

$y_2 = -48$

→ $\frac{6}{9} = \frac{2}{3}$ (para s_1)

$\left(\frac{7}{-16} \rightarrow \text{descartado, es negativo}\right)$

1er Iteration

Base	Z	y_1	y_2	s_1	s_2	R
Z	1	-130/9	0	48/9	0	0
s_1	0	11/9	1	1/9	0	6
s_2	0	173/144	0	-16/9	1	7

$$\frac{\frac{2}{3}}{\frac{11}{9}} = \frac{2}{3} \times \frac{9}{11} = \frac{18}{33} = \frac{6}{11} \text{ para } y_2$$

$$\frac{\frac{48}{173}}{\frac{144}{144}} = \frac{48}{173} \times \frac{144}{144} = \frac{11376}{8304} \approx 1.37 \text{ para } s_2$$

Base	Z	y_1	y_2	s_1	s_2	R
Z	0	286/11	176/11	0	154/11	1
s_1	1	4/11	1/11	0	6/11	0
s_2	0	-173/11	-16/11	1	48/11	0

Soluzioni Optima

$$y_1 = \frac{6}{11}, y_2 = 0$$

$$x_1 = 11y_1 + 9y_2 = 11\left(\frac{6}{11}\right) + 9(0) = 6$$

$$x_2 = 13y_1 - 16y_2 = 13\left(\frac{6}{11}\right) + 16(0) = \frac{78}{11} \approx 7.09$$

Valor Optimo:

$$Z = 6x_1 + 7x_2 = 6(6) + 7\left(\frac{78}{11}\right) = 36 + \frac{546}{11} = 85.64$$

Resultado final \rightarrow

$$x_1 = 6$$

$$x_2 = \frac{78}{11} \approx 7.09$$

$$\text{Valor optimo} \Rightarrow Z = 85.64$$