

Actividad 9.1

if fibonacci (int n) {

if (n == 0) cond1

return 0; ret1

else if (n == 1) cond2

return 1; ret2

else

return fibonacci(n-1) + fibonacci(n-2)

}

$$T(n) = \begin{cases} n=0: T(\text{cond}_1) + T(\text{cond}_1) = t + t = 2t \\ n=1: T(\text{cond}_1) + T(\text{cond}_2) + T(\text{cond}_2) = t + t + t = 3t \\ n>1: T(\text{cond}_1) + T(\text{cond}_2) + T(n-1) + T(n-2) = 3t + T(n-1) + T(n-2) \end{cases}$$

$$\begin{aligned} T(n) &= 3t + \underline{T(n-1)} + \underline{T(n-2)} \\ &= 3t + [3t + T(n-2) + T(n-3)] + [3t + T(n-3) + T(n-4)] \\ &= 9t + T(n-2) + 2T(n-3) + T(n-4) \end{aligned}$$

$$\begin{aligned} &= 9t + [3t + T(n-3) + T(n-4) + 2] + 2[3t + T(n-4) + T(n-5)] + [3t + T(n-5) + T(n-6)] \\ &= 24t + T(n-3) + 3T(n-4) + 3T(n-5) + T(n-6) \end{aligned}$$

No heavy pattern

$$T(n-1) > T(n-2) \rightarrow 3t + T(n-1) + T(n-1) > 3t + T(n-1) + T(n-2)$$

Recurrence

$$\begin{aligned} T(n) &= 3t + T(n-1) + T(n-1) = 3t + 2T(n-1) \\ &= 3t + 2[3t + 2T(n-2)] = (1+2)3t + 2^2 T(n-2) \\ &= (1+2)3t + 2^2[3t + 2T(n-3)] = (1+2+3)3t + 2^3 T(n-3) \\ &= (1+2+3)3t + 2^3[3t + 2T(n-4)] \end{aligned}$$

K-ésimma expansion

$$T(n) = (2^0, 2^1, 2^2, \dots, 2^{k-1}) 3t + 2^n (T(n-n))$$

$$\begin{array}{l} T(0) = 2t \\ T(1) = 3t \end{array} \xrightarrow{\quad} \begin{array}{l} n = k = 0 \\ n = 1 \end{array}$$

Substitue en (K)

$$T(n) = (2^0, 2^1, 2^2, \dots, 2^{k-1}) 3t + 2^n T(0)$$

$$= (2^0 + 2^1 + 2^2 + \dots + 2^{k-1}) 3t + 2^n (T(0))$$

$$T(n) = (2^0, 2^1, 2^2, \dots, 2^{k-1}) 3 + 2^n + 1$$

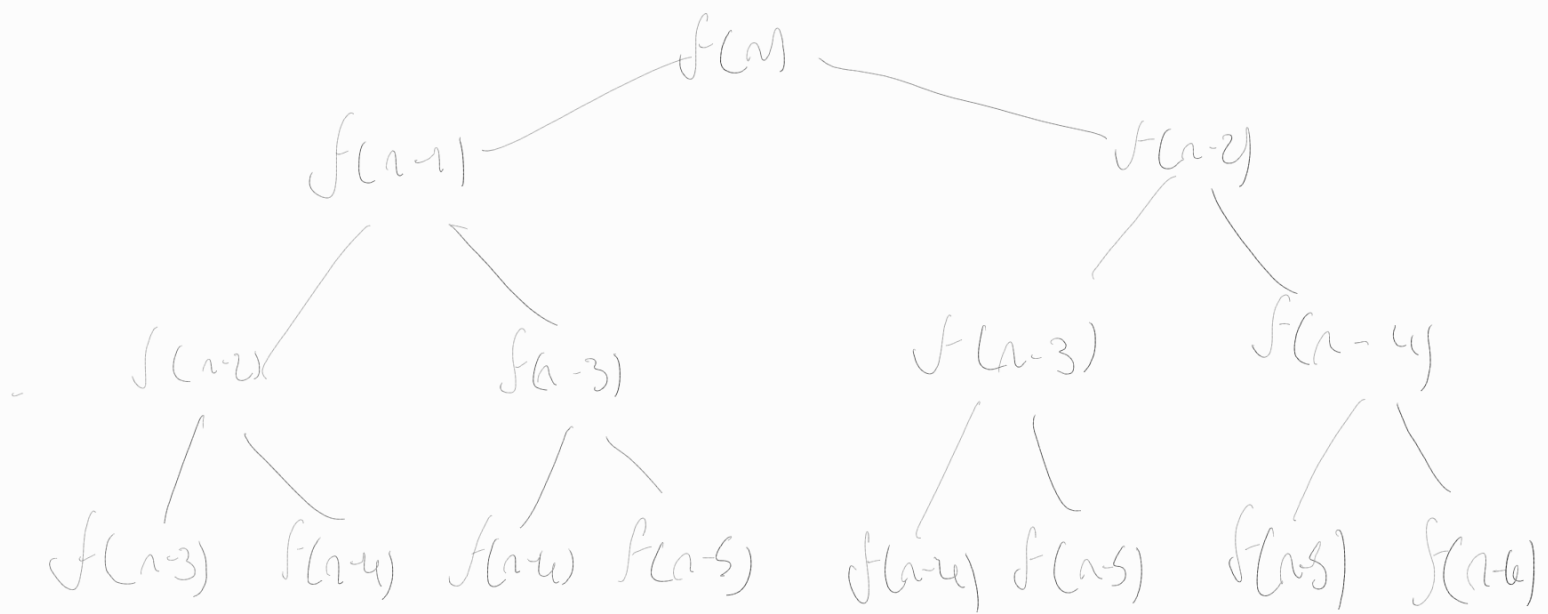
$$(2) \quad O(T(n)) = O((2^0, 2^1, 2^2, \dots, 2^{n-1}) 3 + 2^{n+1})$$

Règle de somme

$$\begin{aligned} &= \max(O(3(2^0)), O(3(2^1)), O(3(2^2)), \dots, O(3(2^{n-1})), O(2^{n+1})) \\ &= O(2^{n+1}) \end{aligned}$$

- Constantes

$$O(T(n)) = O(n) = 2^4$$



int fibonacci (int n) {

③ int fib (int n, int d1)

④ if (n == 0) {
 return 0; // und
 // ret1

else if (n == 1) { // und2

 n1 = 0 // asug

 return 1; // ret2

} else { // und3
 int n2 = 0 // asug2

 n1 = fib(n-1, n-2)

 return n1 + n2; // ret3

$$T(n) \begin{cases} n=0 = T(\text{und}_1) + T(\text{ret}_1) = t + t = 2t \\ n=2 = T(\text{und}_1) + T(\text{und}_2) + T(\text{asug}_1) + T(\text{ret}_2) = 4t \\ n>1: T(\text{und}_1) + T(\text{und}_2) + T(\text{asug}_2) + T(n-1) + T(\text{ret}_3) = 4t + T(n-1) \end{cases}$$

Expansion

$$T(n) = 4t + T(n-1)$$

$$= 4t + [4t + T(n-2)] = 2(4t) + T(n-2)$$

$$= 4t + [4t + T(n-3)] = (3)(4t) + T(n-3)$$

$$= 3(4t) + [4t + T(n-4)] = (4)(4t) + T(n-4)$$

K-esimre expansion

$$T(n) = (K)4t + T(n-k)$$

$$T(0) = 2t$$

$$T(1) = 4t \rightarrow n-k=0 \rightarrow n=k$$

$$\rightarrow T(n) = n4t + T(0) = 4nt + T(0) = 4nt + 2t$$

$$\rightarrow T(n) = 4nt + 2$$

$$O(T(n)) = O(4nt + 2) = n //$$