

### EJERCICIO 3.1

Minimizar  $z = 3x_1 + 5x_2$

s. a  $\rightarrow 6x_1 + 9x_2 \geq 18$

$4x_1 - 7x_2 \geq 28$

$x_1, x_2 \geq 0$

DUAL

$z = 18y_1 + 28y_2$

Maximizar

$6y_1 + 4y_2 \leq 3$

$9y_1 - 7y_2 \leq 5$

$x_1, x_2 \geq 0$

$z - 18y_1 - 28y_2 = 0$

$6y_1 + 4y_2 + s_1 = 3$

$9y_1 - 7y_2 + s_2 = 5$

|       | $z$ | $y_1$ | $y_2$ | $s_1$ | $s_2$ | $R$ |
|-------|-----|-------|-------|-------|-------|-----|
| $z$   | 1   | -18   | -28   | 0     | 0     | 0   |
| $s_1$ | 0   | 6     | 4     | 1     | 0     | 3   |
| $s_2$ | 0   | 9     | -7    | 0     | 1     | 5   |

$\Rightarrow \frac{3}{4} = 0.75$

$\Rightarrow \frac{5}{-7} = -0.7142$

$s_1/4$ ;  $z + 28s_1$ ;  $s_2 + 7s_1$

|             | $z$ | $y_1$ | $y_2$ | $s_1$ | $s_2$ | $R$    |
|-------------|-----|-------|-------|-------|-------|--------|
| $z$         | 1   | 24    | 0     | 7     | 0     | 21     |
| $(y_2) s_1$ | 0   | $3/2$ | 1     | $1/4$ | 0     | $3/4$  |
| $s_2$       | 0   | 51    | 0     | $7/4$ | 1     | $41/4$ |

Sei invariante  $y_1$ :

$$y_1 = 0 ; y_2 = 2/3 ; z = 100/3$$

$$6x_1 + 9x_2 \geq 18$$

$$6x_1 + 9x_2 = 18$$

$$6x_1 + 9x_2 - 18 = 0$$

$$(6x_1 + 9x_2 - 18)(y_1) = 0$$

$$(6x_1 + 9x_2 - 18)(0) = 0$$

$$x_2 = 0$$

$$4x_1 - 7x_2 \geq 28$$

$$4x_1 - 7x_2 = 28$$

$$4x_1 - 7x_2 - 28 = 0$$

$$(4x_1 - 7x_2 - 28)(y_2) = 0$$

$$\frac{8}{3}x_1 - \frac{14}{3}x_2 - \frac{56}{3} = 0$$

$$x_1 = 7$$

$$\text{Min } z = 3(7) + 5(0)$$

$$z = 21$$

$$x_1 = 7$$

$$x_2 = 0$$

$$z = 21$$