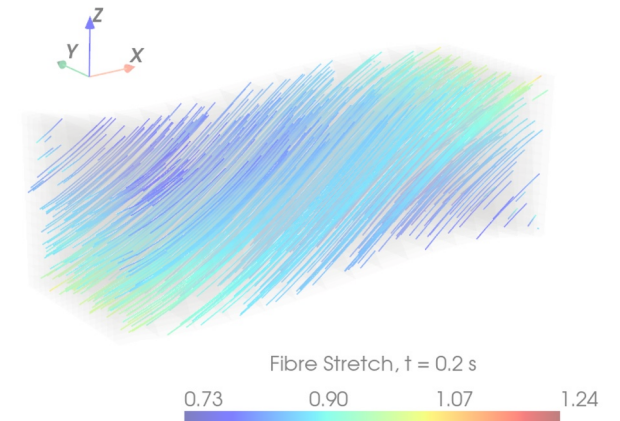
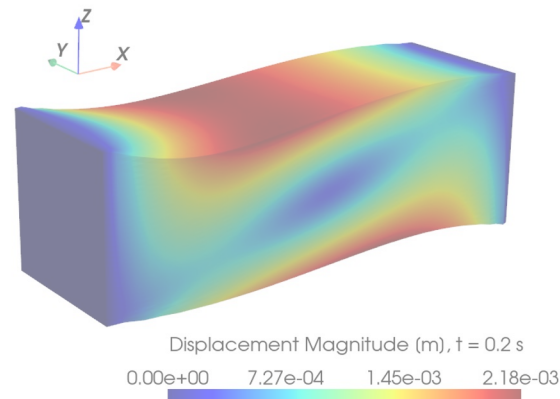


# Tutorial 1: Introduction to the Flexodeal Framework

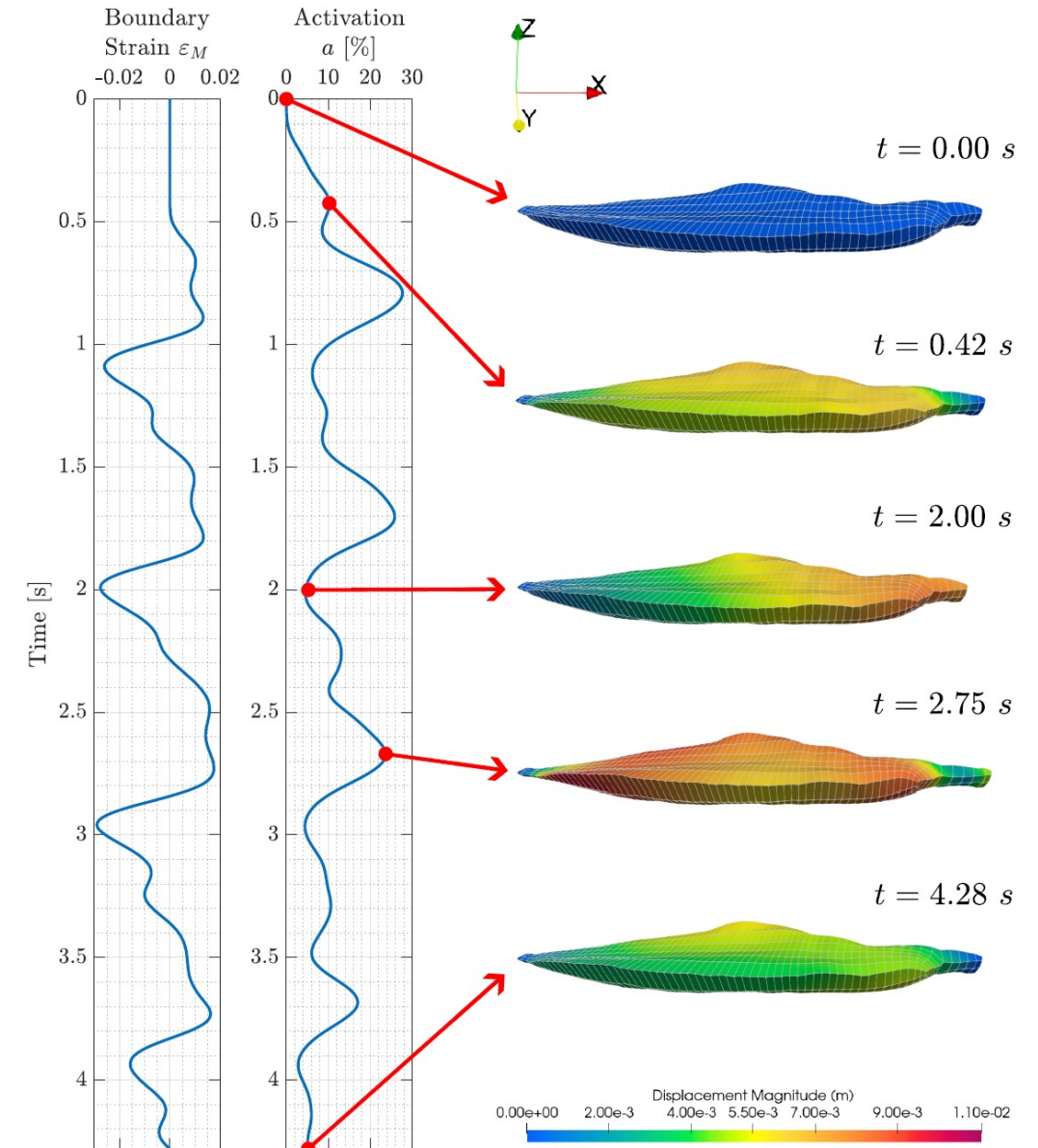
Javier Almonacid  
Research Assistant @ NML

February 27, 2026



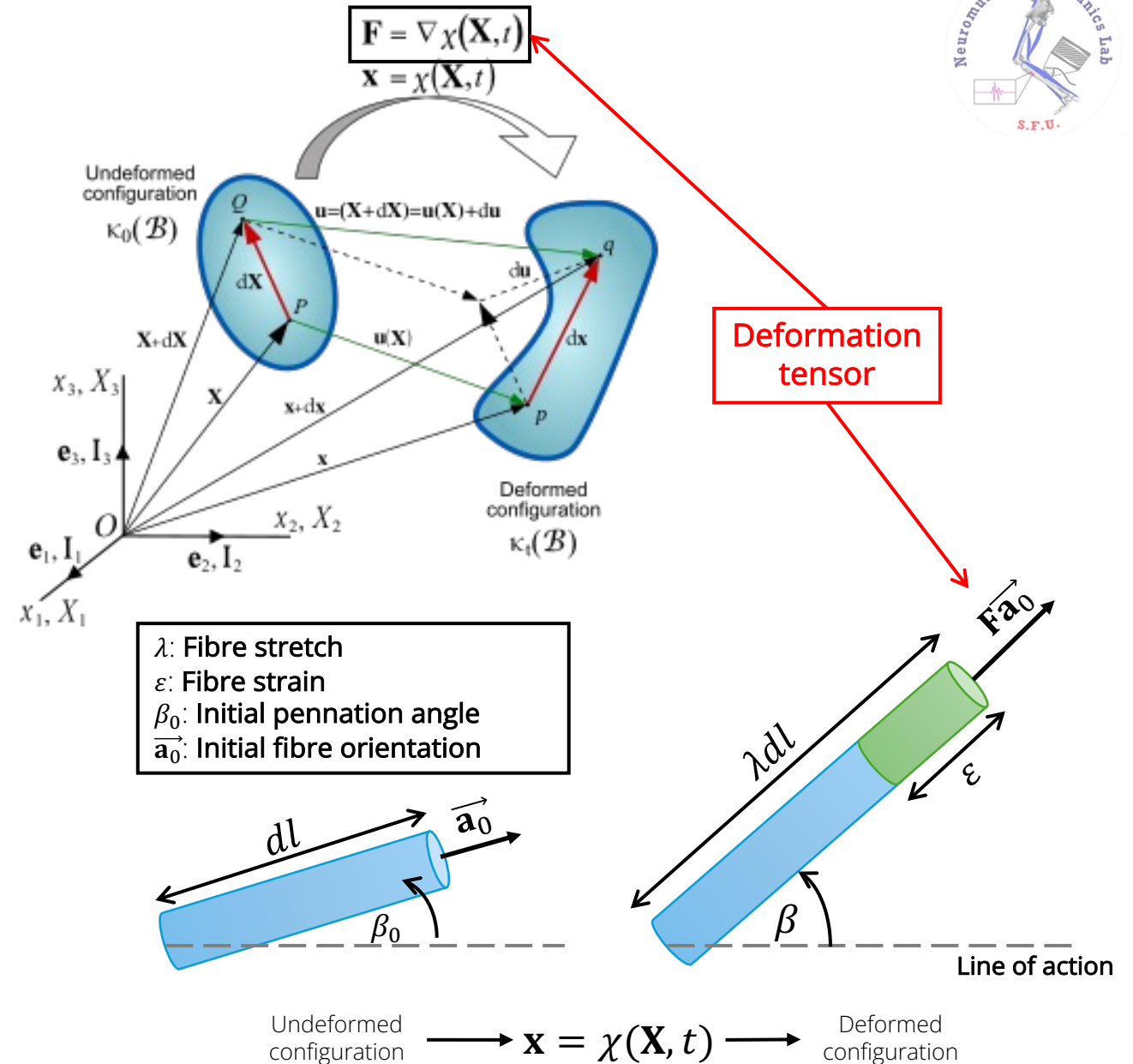
# What is Flexodeal?

- It is a **computational framework** developed by the NML to simulate the **dynamic** deformation of **active** muscle tissue in **3D** based on commonly-accepted **physiological principles**.
- Written in C++, powered by **deal.II**.
- Discretization based on **finite elements**.
- Geometries are meshed using **hexahedral** elements (voxels).



# Main Features

- Local minimization of the total energy leads to a system of nonlinear PDEs in a **three-field formulation** (Simo et al. 1985).
- Stress modelled as the additive response of:
  - An **along-fibre** component (Hill's model),
  - Base material,
  - Intramuscular fat,
  - Tendon,
  - Aponeurosis.

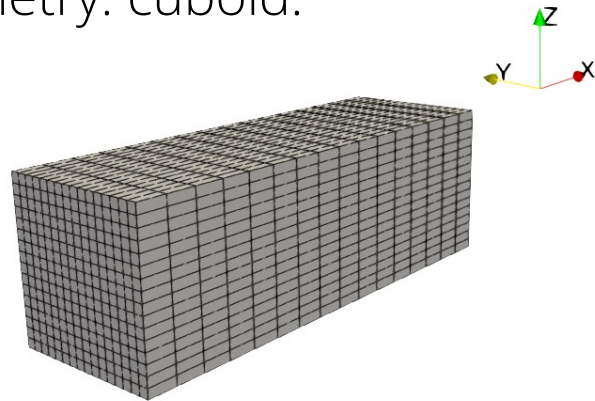


# Available in two versions

## Flexodeal Lite (Tutorial 1)

[github.com/sfu-nml/flexodeal-lite](https://github.com/sfu-nml/flexodeal-lite)

- A simpler code suitable for **numerical developments** or **simple experiments**.
- Supports muscle tissue only (no tendon or aponeurosis).
- Fat-free muscle (by default).
- Default geometry: cuboid.

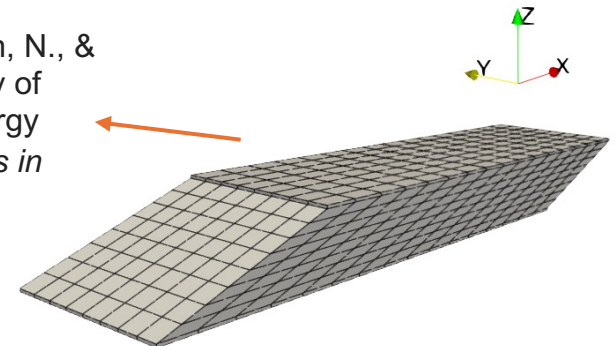


## Flexodeal (Tutorial 2)

[github.com/sfu-nml/flexodeal](https://github.com/sfu-nml/flexodeal)

- A more complex code suitable for **realistic experiments** of the muscle-tendon unit.
- Support muscle tissue, tendon, and aponeurosis.
- Spatially-variable intramuscular fat.
- Spatially-variable initial fibre orientations.
- Default geometry: idealized MG.

Ross, S. A., Domínguez, S., Nigam, N., & Wakeling, J. M. (2021). The energy of muscle contraction. III. Kinetic energy during cyclic contractions. *Frontiers in physiology*, 12, 628819



# Downloading and compiling Flexodeal Lite

Description	UNIX Command
Download the latest release of Flexodeal Lite from: <a href="https://github.com/sfu-nml/flexodeal-lite/releases">https://github.com/sfu-nml/flexodeal-lite/releases</a>	<code>wget https://github.com/sfu-nml/flexodeal-lite/archive/refs/tags/v1.6.1.zip</code>
Unzip the downloaded file	<code>unzip v1.6.1.zip</code>
Navigate to the flexodeal-lite-1.6.1 folder	<code>cd flexodeal-lite-1.6.1</code>
Compile the software	<code>cmake . -DCMAKE_BUILD_TYPE=Release -DDEAL_II_DIR=&lt;path/to/deal.II&gt;</code>
Call "make"	<code>make</code>
If "make" was successful, you should now have an executable called "flexodeal-lite".	<code>./flexodeal-lite</code>

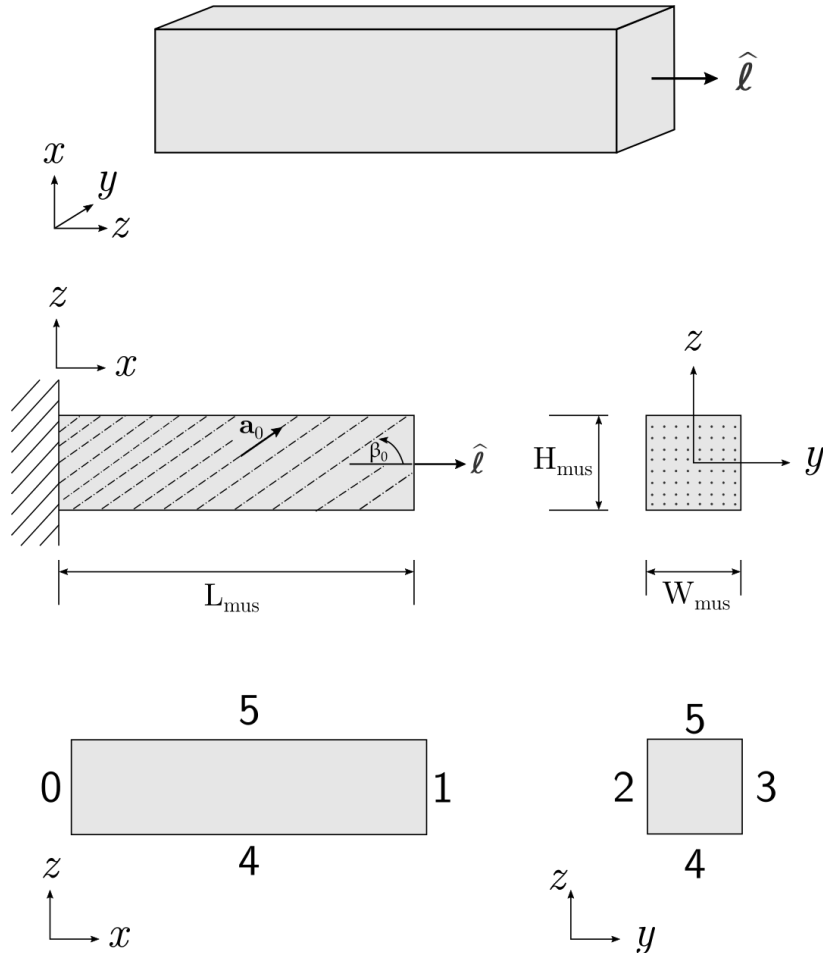
# The default experiment

# How to set up a computational experiment?

- In the Flexodeal framework, we follow the principles of computational mechanics.
- To set an experiment, you will need:
  1. A **mesh** of your geometry (computational domain).
  2. Model and simulation (numerical) **parameters**.
  3. A time-dependent **boundary strain** -> this controls the length of the muscle.
  4. A time-dependent **activation** profile.
- We will go over the details of the default experiment in Flexodeal Lite, i.e. the one you obtain when simply running in your terminal:

**`./flexodeal-lite.`**

# Geometry (computational domain)



3D view. Geometry contains **muscle tissue only** (no aponeurosis or tendon).

Main parameters (can be modified in **parameters file**):

- $L_{\text{mus}}$ : muscle length
- $H_{\text{mus}}$ : muscle height
- $W_{\text{mus}}$ : muscle width
- $\mathbf{a}_0 = \langle \cos(\beta_0), 0, \sin(\beta_0) \rangle$ : fibre orientation
- $\hat{\ell}$ : line of action

Boundary IDs:

- 0: Fixed (no displacement)
- 1: Moving boundary (**prescribed strain**)
- 2-5: Traction free.



# Parameters file

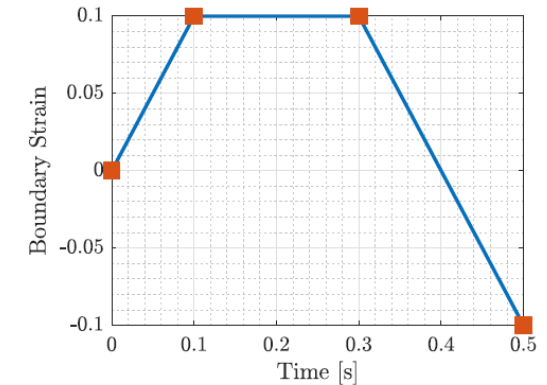
- A file with extension **.prm** containing several **model** and **simulation** parameters.
- Some important parameters in this file are:
  - Type of simulation (dynamic or quasi-static),
  - Simulation time and time step size,
  - Muscle block dimensions,
  - Fibre orientations,
  - Markers (to track selected point displacements),
  - Solver type ("Direct" for coarse meshes, "CG" for finer meshes),
  - Error tolerances.
- Open the **parameters.prm** file to see the complete list of parameters.

# Boundary strain and activation files

- They provide the **time-dependent prescribed boundary strain** (on boundary ID 1 for the default experiment) and the **time-dependent activation profile** to the simulation.
- Each file is a table of coordinate pairs.
- Flexodeal uses linear interpolation to evaluate these functions between control points.

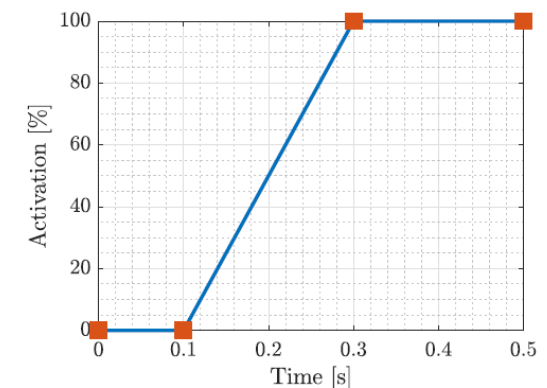
Strain  
(e.g., 0.1 = 10% strain =  
lengthen muscle to  $1.1L_{mus}$ )

control_points_strain.dat	
0.0	0.0
0.1	0.1
0.3	0.1
0.5	-0.1



Time  
(in seconds)

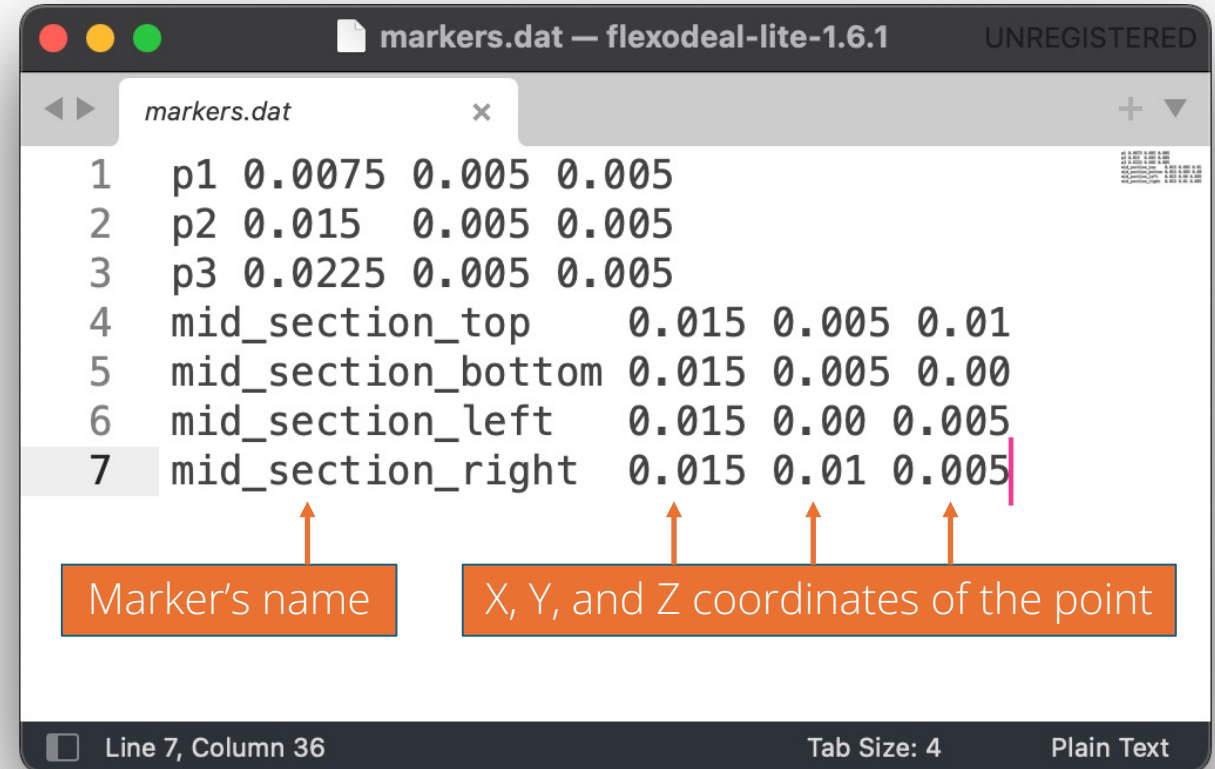
control_points_activation.dat	
0.0	0.0
0.1	0.0
0.3	1.0
0.5	1.0



Activation  
(e.g., 0.5 = 50%, 1.0 = 100%)

# Markers (displacement trackers, optional)

- Although the entire 3D displacement field is available as a VTU file, we can also track this variable at **point locations** in the mesh.
- Markers **must correspond to** mesh vertices.
- If you do not require this feature, **this file can be left empty**.



```

markers.dat
1  p1  0.0075  0.005  0.005
2  p2  0.015   0.005  0.005
3  p3  0.0225  0.005  0.005
4  mid_section_top      0.015  0.005  0.01
5  mid_section_bottom  0.015  0.005  0.00
6  mid_section_left    0.015  0.00  0.005
7  mid_section_right   0.015  0.01  0.005
  
```

Marker's name

X, Y, and Z coordinates of the point

Line 7, Column 36      Tab Size: 4      Plain Text

# Some notes

- CMake compiles a **machine-dependent** version of Flexodeal.
- Unless you modified the **flexodeal-lite.cc** file directly, **you do not need** to call **make** (or **cmake**) every time you run **./flexodeal-lite**
- The call to **./flexodeal-lite** accepts the following **command-line arguments**:

Argument	Default value	Description
-PARAMETERS	parameters.prm	Parameter file
-BDY_STRAIN	control_points_strain.dat	Boundary strain profile
-ACTIVATION	control_points_activation.dat	Activation profile
-OUTPUT_DIR	Directory name based on current time and date	Folder where the simulation results will be stored

# Output files & visualization

# CSV files



Description	File
Time series of activation and muscle length.	activation_muscle_length-3d.csv
Time series of selected point displacements (markers).	displacements-3d.csv
Time series of energies (kinetic, internal, volumetric, isochoric, ...).	energy_data-3d.csv
Time series of force at the moving end of muscle in the direction of the line of action	force_data-3d.csv
Vectorial force at each boundary ID at each time step	force_data-3d-000.csv force_data-3d-001.csv ...
Time series of velocity averages	gearing_info-3d.csv
Time series of mean stretch and mean pennation angle	mean_stretch_pennation_data-3d.csv

# ParaView files (3D fields)

Description	File
Main model unknowns: muscle displacement, pressure, dilatation.	solution-3d-000.vtu solution-3d-001.vtu ...
Muscle velocity	velocity-3d-000.vtu velocity-3d-001.vtu ...
Fibre stretch and fibre orientations	stretch-3d-000.csv stretch-3d-001.csv ...
Fibre strain rate	strain-rate-3d-000.csv strain-rate-3d-001.csv ...
Kirchhoff stress tensor	stress-3d-000.vtu stress-3d-001.vtu ...

# Visualization in ParaView

- Task: Open and explore any of the VTU files.
- Suggested: Rescale data range over all timesteps.
- Discussion of visualization techniques and presentation.



# Running simple examples

# Example 1: Isometric contraction

- Run the experiment (write everything in one line):

```
./flexodeal-lite -PARAMETERS=examples/IC_parameters.prm  
-BDY_STRAIN=examples/IC_strain.dat -ACTIVATION=examples/IC_activation.dat  
-OUTPUT_DIR=results_ic
```

- We consider a 3 x 1 x 1 cm block of parallel-fibred muscle tissue (no pennation).
- Fully activate the block over a span of 1 s.
- This is a **quasi-static experiment**. No velocity or fibre strain rate data is exported.
- This is also a **benchmark experiment**. At any of the fixed ends, when the activation reaches 100%:

$$\text{Force} = F_0 = \sigma_0 \times \text{CSA} = 200,000 \text{ Pa} \times 0.01^2 \text{ m}^2 = 20 \text{ N}$$

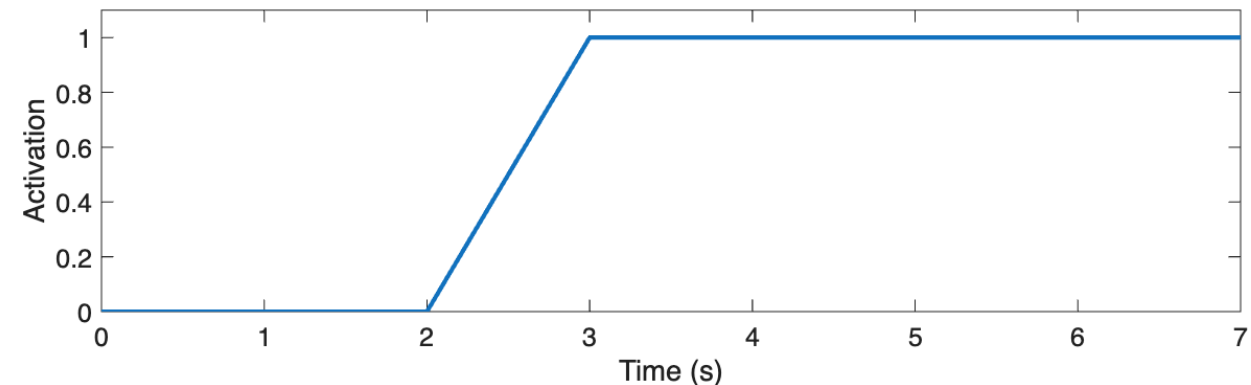
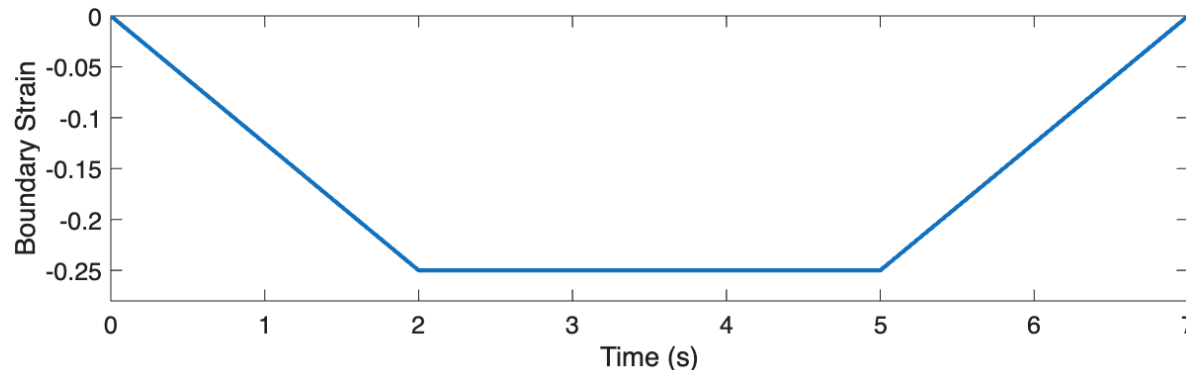
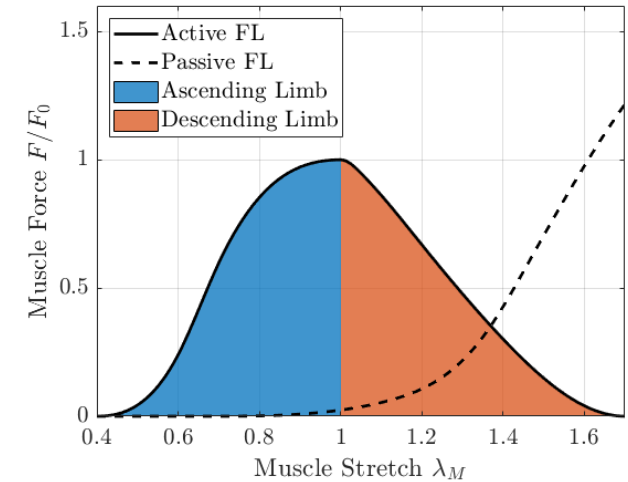
- Hence, we expect a force of ~20 N at any of the fixed ends.

# Example 2: Ascending limb contraction

- Run the experiment (write everything in one line):

```
./flexodeal-lite -PARAMETERS=examples/AL_parameters.prm
-BDY_STRAIN=examples/AL_strain.dat
-ACTIVATION=examples/AL_activation.dat
-OUTPUT_DIR=results_al
```

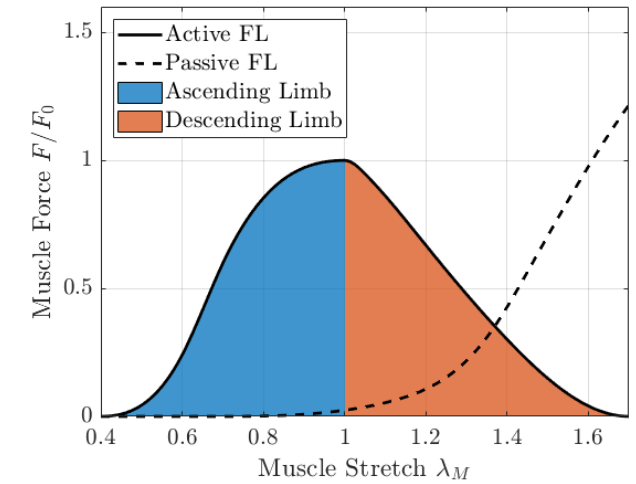
- We consider a 3 x 1 x 1 cm block of muscle-tissue, 30 deg. pennation. This is a **dynamic experiment**.
- Strain and activation profiles:



# Try it yourself!



- Set up a contraction on the **descending limb** of the force-length curve as follows:
  1. Lengthen the muscle block to 1.1 times its initial length (or +10% strain) over 2 seconds.
  2. Then, perform an isometric contraction over 1 second, activating the muscle to 50%.
  3. Shorten the muscle back to its initial length over 2 seconds.
- You can assume the same geometry and muscle architecture as for the ascending limb contraction.



# More Resources

- Finite element simulation using deal.II:  
<https://www.dealii.org/current/doxygen/deal.II/Tutorial.html>
- Mathematical details of Flexodeal:
  - Almonacid, J. A., Domínguez-Rivera, S. A., Konno, R. N., Nigam, N., Ross, S. A., Tam, C., & Wakeling, J. M. (2024). A three-dimensional model of skeletal muscle tissues. *SIAM journal on applied mathematics*, 84(3), S538-S566.
  - Almonacid Paredes, J. A. (2025). On the nonlinear elastodynamics of skeletal muscle (Chapters 5 and 6). PhD Thesis, Simon Fraser University (available at [www.sfu.ca/~javier](http://www.sfu.ca/~javier)).
- ParaView documentation:  
<https://docs.paraview.org/en/v5.13.1/UsersGuide/introduction.html>



[www.github.com/sfu-nml](https://www.github.com/sfu-nml)



[www.linkedin.com/company/sfu-nml](https://www.linkedin.com/company/sfu-nml)



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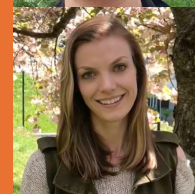
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