

Regresores cualitativos

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1 Regresores cualitativos con dos niveles

El archivo *Credit Approval Decisions.csv* contiene información acerca de la aceptación o rechazo de un crédito. Se dispone también de información acerca de otras variables adicionales. El objetivo es analizar la variable *Decision* en función del resto de variables.

```
d = read.csv("datos/Credit Approval Decisions.csv")
str(d)
```

```
## 'data.frame': 50 obs. of 6 variables:
## $ Homeowner : chr "Y" "Y" "Y" "N" ...
## $ Credit_Score : int 725 573 677 625 527 795 733 620 591 660 ...
## $ Years_Credit_History : int 20 9 11 15 12 22 7 5 17 24 ...
## $ Revolving_Balance : num 11320 7200 20000 12800 5700 ...
## $ Revolving_Utilization: num 0.25 0.7 0.55 0.65 0.75 0.12 0.2 0.62 0.5 0.35 ...
## $ Decision : chr "Approve" "Reject" "Approve" "Reject" ...
```

Convertimos las variables cualitativas a factor:

```
d$Homeowner = factor(d$Homeowner)
d$Decision = factor(d$Decision)
str(d)
```

```
## 'data.frame': 50 obs. of 6 variables:
## $ Homeowner : Factor w/ 2 levels "N","Y": 2 2 2 1 1 2 1 1 2 2 ...
## $ Credit_Score : int 725 573 677 625 527 795 733 620 591 660 ...
## $ Years_Credit_History : int 20 9 11 15 12 22 7 5 17 24 ...
## $ Revolving_Balance : num 11320 7200 20000 12800 5700 ...
## $ Revolving_Utilization: num 0.25 0.7 0.55 0.65 0.75 0.12 0.2 0.62 0.5 0.35 ...
## $ Decision : Factor w/ 2 levels "Approve","Reject": 1 2 1 2 2 1 1 2 2 1 ...
```

1.1 Variables auxiliares

Se crean variables auxiliares con valores cero - uno. Por ejemplo

- HomeownerY = 1 si Homeowner = "Y"
- HomeownerY = 0 si Homeowner = "N"

```
HomeownerY = ifelse(d$Homeowner == "Y", 1, 0)
```

Estimamos por tanto el modelo

$$P(Decision_i = 1) = \frac{\exp(\beta_0 + \beta_1 HomeownerY_i)}{1 + \exp(\beta_0 + \beta_1 HomeownerY_i)}$$

Al final estamos trabajando con dos modelos:

- HomeownerY = 0:

$$P(Decision_i = 1) = \frac{\exp(\beta_0)}{1 + \exp(\beta_0)}$$

- HomeownerY = 1:

$$P(Decision_i = 1) = \frac{\exp(\beta_0 + \beta_1)}{1 + \exp(\beta_0 + \beta_1)}$$

Por tanto, si $\beta_1 = 0$, entonces $P(\text{Decision} = 1 \mid \text{Homeowner} = Y) = P(\text{Decision} = 1 \mid \text{Homeowner} = N)$. Si $\beta_1 > 0$, entonces:

$$\beta_0 < \beta_0 + \beta_1 - \beta_0 > -\beta_0 - \beta_1 \exp(-\beta_0) > \exp(-\beta_0 - \beta_1) 1 + \exp(-\beta_0) > 1 + \exp(-\beta_0 - \beta_1) \frac{1}{1 + \exp(-\beta_0)} < \frac{1}{1 + \exp(-\beta_0 - \beta_1)} \frac{e}{1 + e}$$

Estimamos el modelo. Recordemos que la variable respuesta toma valores 0 y 1. Por tanto si definimos:

```
Decision1 = ifelse(d$Decision == "Approve", 1, 0)
```

el modelo que estamos estimando es $P(Y = 1) = P(\text{Decision1} = 1) = P(\text{Decision} = \text{"Approve"})$.

```
m1 = glm(Decision1 ~ HomeownerY, family = binomial)
summary(m1)
```

```
##
## Call:
## glm(formula = Decision1 ~ HomeownerY, family = binomial)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.7344  -0.4265  -0.4265   0.7090   2.2101
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  -2.3514     0.7400  -3.177  0.00149 **
## HomeownerY     3.6041     0.8729   4.129 3.64e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 68.994  on 49  degrees of freedom
## Residual deviance: 42.194  on 48  degrees of freedom
## AIC: 46.194
```

```
##
## Number of Fisher Scoring iterations: 5
```

Como $\beta_1 > 0$ quiere decir que $P(\text{Approve}|\text{Homeowner} = N) < P(\text{Approve}|\text{Homeowner} = Y)$.

1.2 Variables auxiliares 1

```
HomeownerN = ifelse(d$Homeowner == "N", 1, 0)

m2 = glm(Decision1 ~ HomeownerN, family = binomial)
summary(m2)

##
## Call:
## glm(formula = Decision1 ~ HomeownerN, family = binomial)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.7344  -0.4265  -0.4265   0.7090   2.2101
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   1.2528     0.4629   2.706  0.0068 **
## HomeownerN    -3.6041     0.8729  -4.129 3.64e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 68.994  on 49  degrees of freedom
## Residual deviance: 42.194  on 48  degrees of freedom
## AIC: 46.194
##
## Number of Fisher Scoring iterations: 5
```

1.3 Factores

Es importante utilizar bien los niveles de las variables:

```
levels(d$Decision)

## [1] "Approve" "Reject"

levels(d$Homeowner)

## [1] "N" "Y"
```

Por tanto, si estimamos el modelo:

```
m3 = glm(Decision ~ Homeowner, data = d, family = binomial)
summary(m3)

##
## Call:
## glm(formula = Decision ~ Homeowner, family = binomial, data = d)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -2.2101 -0.7090 0.4265 0.4265 1.7344
##
## Coefficients:
##             Estimate Std. Error z value Pr(>|z|)
## (Intercept)  2.3514      0.7400   3.177 0.00149 **
## HomeownerY   -3.6041      0.8729  -4.129 3.64e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 68.994  on 49  degrees of freedom
## Residual deviance: 42.194  on 48  degrees of freedom
## AIC: 46.194
##
## Number of Fisher Scoring iterations: 5
```

En el fondo estamos estimando $P(\text{Reject} | \text{Homeowner} = \text{"Y"})$, ya que

- la variable respuesta tiene que tomar valores 1 y 0. R asigna el cero al nivel de referencia. Por lo tanto, $P(\text{Decision} = 1) = P(\text{Decision} = \text{Reject})$.
- para el regresor de tipo factor, R crea una variable auxiliar que vale 1 y 0, y asigna el cero al nivel de referencia. Por tanto crea HomeownerY, donde HomeownerY = 1 cuando Homeowner = "Yes".

Si queremos estimar el modelo m1 anterior tenemos que hacer:

```
d$Decision = relevel(d$Decision, ref = "Approve")
m4 = glm(Decision ~ Homeowner, data = d, family = binomial)
summary(m4)
```

```
##
## Call:
## glm(formula = Decision ~ Homeowner, family = binomial, data = d)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.2101 -0.7090  0.4265  0.4265  1.7344
##
## Coefficients:
##             Estimate Std. Error z value Pr(>|z|)
## (Intercept)  2.3514      0.7400   3.177 0.00149 **
## HomeownerY   -3.6041      0.8729  -4.129 3.64e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 68.994  on 49  degrees of freedom
## Residual deviance: 42.194  on 48  degrees of freedom
## AIC: 46.194
##
## Number of Fisher Scoring iterations: 5
```

2 Variables cualitativas y cuantitativas

El funcionamiento es idéntico que el modelo de regresión lineal:

```

d$Decision = relevel(d$Decision, ref = "Approve")
m4 = glm(Decision ~ Homeowner + Credit_Score + Years_Credit_History, data = d, family = binomial)
summary(m4)

##
## Call:
## glm(formula = Decision ~ Homeowner + Credit_Score + Years_Credit_History,
##      family = binomial, data = d)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -2.49762  -0.07724   0.00330   0.12979   1.31515
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    38.05066    14.85133     2.562  0.0104 *
## HomeownerY      -3.13441     1.73873    -1.803  0.0714 .
## Credit_Score    -0.04946     0.01933    -2.559  0.0105 *
## Years_Credit_History -0.31716     0.21846    -1.452  0.1466
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 68.994  on 49  degrees of freedom
## Residual deviance: 15.208  on 46  degrees of freedom
## AIC: 23.208
##
## Number of Fisher Scoring iterations: 8

```

3 Variables cualitativas con más de dos niveles

Igual que en regresión lineal, se tienen que crear tantas variables auxiliares como niveles del factor menos una.