Regresores cualitativos

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1 Regresores cualitativos con dos niveles

El archivo *Credit Approval Decisions.csv* contiene información acerca de la aceptación o rechazo de un crédito. Se dispone también de información acerca de otras variables adicionales. El objetivo es analizar la variable *Decision* en función del resto de variables.

```
d = read.csv("datos/Credit Approval Decisions.csv")
str(d)
## 'data.frame':
                    50 obs. of 6 variables:
                                  "Y" "Y" "Y" "N" ...
   $ Homeowner
                           : chr
  $ Credit_Score
                           : int 725 573 677 625 527 795 733 620 591 660 ...
  $ Years_Credit_History : int
                                  20 9 11 15 12 22 7 5 17 24 ...
   $ Revolving Balance
                           : num
                                  11320 7200 20000 12800 5700 ...
   $ Revolving_Utilization: num
                                  0.25 0.7 0.55 0.65 0.75 0.12 0.2 0.62 0.5 0.35 ...
   $ Decision
                           : chr
                                  "Approve" "Reject" "Approve" "Reject" ...
Convertimos las variables cualitativas a factor:
```

```
d$Homeowner = factor(d$Homeowner)
d$Decision = factor(d$Decision)
str(d)
```

1.1 Variables auxiliares

Se crean variables auxiliares con valores cero - uno. Por ejemplo

- Homeowner Y = 1 si Homeowner Y''
- Homeowner Y = 0 si Homeowner = "N"

```
HomeownerY = ifelse(d$Homeowner == "Y", 1, 0)
```

El modelo que se estima es:

$$P(Decision_i = 1) = \frac{exp(\beta_0 + \beta_1 Homeowner Y_i)}{1 + exp(\beta_0 + \beta_1 Homeowner Y_i)}$$

Al final estamos trabajando con dos modelos:

• HomeownerY = 0:

$$P(Decision_i = 1) = \frac{exp(\beta_0)}{1 + exp(\beta_0)}$$

• HomeownerY = 1:

$$P(Decision_i = 1) = \frac{exp(\beta_0 + \beta_1)}{1 + exp(\beta_0 + \beta_1)}$$

Por tanto, si $\beta_1 = 0$, entonces P(Decision = 1 | Homeowner = Y) = P(Decision = 1 | Homeowner = N). Si $\beta_1 > 0$, entonces:

$$\beta_0 < \beta_0 + \beta_1 - \beta_0 > -\beta_0 - \beta_1 exp(-\beta_0) > exp(-\beta_0 - \beta_1) 1 + exp(-\beta_0) > 1 + exp(-\beta_0 - \beta_1) \frac{1}{1 + exp(-\beta_0)} < \frac{1}{1 + exp(-\beta_0 - \beta_1)} < \frac{1}{1 + exp(-\beta_0 -$$

Multiplicando numerador y denominador por el mismo número la desigualdad no cambia:

$$\frac{exp(\beta_0)}{1 + exp(\beta_0)} < \frac{exp(\beta_0 + \beta_1)}{1 + exp(\beta_0 + \beta_1)} P(Decision = 1 | Homeowner = N) < P(Decision = 1 | Homeowner = Y)$$

Estimamos el modelo. Recordemos que la variable respuesta toma valores 0 y 1. Por tanto si definimos:

```
Decision1 = ifelse(d$Decision == "Approve", 1, 0)
```

el modelo que estamos estimando es P(Y = 1) = P(Decision1 = 1) = P(Decision = "Approve").

```
m1 = glm(Decision1 ~ HomeownerY, family = binomial)
summary(m1)
```

```
##
##
  glm(formula = Decision1 ~ HomeownerY, family = binomial)
##
## Deviance Residuals:
                 10
                     Median
                                  3Q
                                          Max
## -1.7344 -0.4265 -0.4265
                              0.7090
                                        2.2101
##
  Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                           0.7400 -3.177 0.00149 **
## (Intercept) -2.3514
## HomeownerY
                3.6041
                           0.8729
                                    4.129 3.64e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
## ## (Dispersion parameter for binomial family taken to be 1) ## ## Null deviance: 68.994 on 49 degrees of freedom ## Residual deviance: 42.194 on 48 degrees of freedom ## AIC: 46.194 ## ## Number of Fisher Scoring iterations: 5 \operatorname{Como} \beta_1 > 0 \text{ quiere decir que P(Approve}|\operatorname{Homeowner} = \operatorname{N}) < \operatorname{P(Approve}|\operatorname{Homeowner} = \operatorname{Y}).
```

1.2 Variables auxiliares 1

```
HomeownerN = ifelse(d$Homeowner == "N", 1, 0)
m2 = glm(Decision1 ~ HomeownerN, family = binomial)
summary(m2)
##
## Call:
## glm(formula = Decision1 ~ HomeownerN, family = binomial)
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
## -1.7344 -0.4265 -0.4265
                              0.7090
                                       2.2101
##
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 1.2528
                           0.4629
                                    2.706 0.0068 **
## HomeownerN -3.6041
                           0.8729 -4.129 3.64e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 68.994 on 49 degrees of freedom
## Residual deviance: 42.194 on 48 degrees of freedom
## AIC: 46.194
## Number of Fisher Scoring iterations: 5
```

1.3 Factores

Es importante utilizar bien los niveles de las variables:

```
levels(d$Decision)
```

```
## [1] "Approve" "Reject"
levels(d$Homeowner)
## [1] "N" "Y"
Por tanto, si estimamos el modelo:
m3 = glm(Decision ~ Homeowner, data = d, family = binomial)
summary(m3)
```

```
##
## Call:
  glm(formula = Decision ~ Homeowner, family = binomial, data = d)
##
## Deviance Residuals:
                     Median
##
      Min
                 1Q
                                   3Q
                                           Max
   -2.2101 -0.7090
                     0.4265
                               0.4265
                                        1.7344
##
## Coefficients:
##
               Estimate Std. Error z value Pr(>|z|)
                 2.3514
                            0.7400
                                     3.177 0.00149 **
  (Intercept)
                -3.6041
                            0.8729 -4.129 3.64e-05 ***
## HomeownerY
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 68.994 on 49 degrees of freedom
## Residual deviance: 42.194 on 48 degrees of freedom
## AIC: 46.194
##
## Number of Fisher Scoring iterations: 5
```

En el fondo estamos estimando P(Reject|Homeowner = "Y"), ya que

- la variable respuesta tiene que tomar valores 1 y 0. R asigna el cero al nivel de referencia. Por lo tanto, P(Decision = 1) = P(Decision = Reject).
- para el regresor de tipo factor, R crea una variable auxiliar que vale 1 y 0, y asigna el cero al nivel de referencia. Por tanto crea HomeownerY, donde HomownerY = 1 cuando Homeowner = "Yes".

Si queremos estimar el modelo m1 anterior tenemos que hacer:

```
d$Decision = relevel(d$Decision, ref = "Reject")
m4 = glm(Decision ~ Homeowner, data = d, family = binomial)
summary(m4)
##
## Call:
## glm(formula = Decision ~ Homeowner, family = binomial, data = d)
## Deviance Residuals:
##
      Min
                 1Q
                     Median
                                   30
                                           Max
## -1.7344 -0.4265 -0.4265
                               0.7090
                                        2.2101
##
  Coefficients:
##
##
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -2.3514
                            0.7400 -3.177 0.00149 **
## HomeownerY
                 3.6041
                            0.8729
                                     4.129 3.64e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 68.994 on 49 degrees of freedom
## Residual deviance: 42.194 on 48 degrees of freedom
## AIC: 46.194
```

```
##
## Number of Fisher Scoring iterations: 5
```

2 Variables cualitativas y cuantitativas

El funcionamiento es idéntico que el modelo de regresión lineal:

```
d$Decision = relevel(d$Decision, ref = "Approve")
m4 = glm(Decision ~ Homeowner + Credit_Score + Years_Credit_History, data = d, family = binomial)
summary(m4)
##
## Call:
  glm(formula = Decision ~ Homeowner + Credit Score + Years Credit History,
      family = binomial, data = d)
##
## Deviance Residuals:
##
       Min
                   10
                         Median
                                       3Q
                                                Max
## -2.49762 -0.07724
                        0.00330
                                  0.12979
                                            1.31515
## Coefficients:
##
                        Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                        38.05066
                                   14.85133
                                              2.562
                                                      0.0104 *
## HomeownerY
                        -3.13441
                                    1.73873
                                            -1.803
                                                      0.0714 .
## Credit_Score
                        -0.04946
                                    0.01933
                                            -2.559
                                                      0.0105 *
## Years_Credit_History -0.31716
                                    0.21846 - 1.452
                                                      0.1466
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 68.994 on 49
                                     degrees of freedom
## Residual deviance: 15.208 on 46 degrees of freedom
## AIC: 23.208
## Number of Fisher Scoring iterations: 8
```

3 Variables cualitativas con más de dos niveles

Igual que en regresión lineal, se tienen que crear tantas variables auxiliares como niveles del factor menos una.