

## CS 111 Practice Quiz 2

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**Problem 1:** You need to show all your work (write the solutions step-by-step) in order to receive credit for the following questions.

- (a) Compute  $8^9 \pmod{5}$  by squaring.
- (b) Compute  $6^{-1} \pmod{13}$  using the method of linear combinations (listing multiples).
- (c) Compute  $5^{-1} \pmod{11}$  using Fermat's Little Theorem.
- (d) Solve:  $5x \equiv 7 \pmod{11}$ .

**Problem 2:**

(a) In the RSA, Bob is considering the following choices for the values of  $p, q$  and  $e$ :

- $p = 13, q = 5, e = 3$
- $p = 11, q = 11, e = 3$
- $p = 3, q = 31, e = 5$

For each choice determine whether it's correct or not, and justify your answer.

(b) After thinking a little bit more, Bob chooses  $p = 5, q = 11$  and  $e = 7$ .

- (i) Determine the values of  $n$  and  $\phi(n)$ .
- (ii) Determine  $d$ . Show your work.
- (iii) Encrypt  $M = 2$ . Show your work.

**Problem 3:** For each statement tell whether it is true or false and justify your answer.

- (a) For all nonnegative integers  $n$ ,  $n^2 + 5n + 6$  is an even number.
- (b) For all positive integers  $n$ ,  $n^2 + 5n + 6$  is not a prime number.

**Academic integrity declaration.** Please provide a statement confirming that you completed this assignment all by yourself. (For example, "*Hereby I affirm that I completed this test on my own, without any unauthorized help.*") and sign it. Submissions without the signed statement will not be graded.