

Hypothesis Testing with α Significance Level

Remember that a hypothesis test consists of five main steps:

- (1) Figure out the hypothesis: H_0 and H_A (the equal option always goes into H_0).
- (2) Compute test statistic: $z_{\text{test}} = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$

Here, μ_0 is the value that shows up in H_0

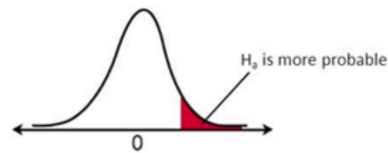
- (3) Find p-value (we look at the sign in the alternative H_A):

If $H_A: \mu > a \Rightarrow \text{p-value} = P(Z > z_{\text{test}})$

If $H_A: \mu < a \Rightarrow \text{p-value} = P(Z < z_{\text{test}})$

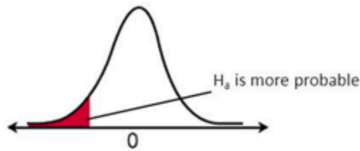
If $H_A: \mu \neq a \Rightarrow \text{p-value} = P(Z < -|z_{\text{test}}|) + P(Z > |z_{\text{test}}|)$

Types of Hypothesis Tests



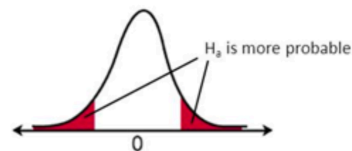
Right-tail test

$H_a: \mu > \text{value}$



Left-tail test

$H_a: \mu < \text{value}$



Two-tail test

$H_a: \mu \neq \text{value}$

(4) Decision

- If $\text{p-value} < \alpha$ we say that there is enough evidence to reject H_0 . In other words, we reject H_0
- If $\text{p-value} \geq \alpha$ we say that there is not enough evidence to reject H_0 . In other words, we can't reject H_0

5) Conclusion: write the decision from (4) in words using the context offered by the problem.