

Jpeg Compression

Pictures, Images, Waves and

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JPEG Image Compression

- Joint Photographic Experts Group

JPEG Image Compression

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- Lossy compression

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 - Smaller file size

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JPEG Image Compression

- Joint Photographic Experts Group
- Lossy compression
 - Smaller file size
 - Maintain image quality
 - Human perception is limited

Compression

Lossy vs Lossless

- Simplest compression

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 - `aaa,ttttt,pppp,hh,sssss` - 20 "bits"

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 - *becomes*
 - `3a5t4p2h6s` - 10 "bits"

Compression

Lossy vs Lossless

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 - Compression ratio of $\frac{20}{10} = 2$

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Lossy vs Lossless

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 - *becomes*
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 - Compression ratio of $\frac{20}{10} = 2$
- Many other methods
- JPEG specific to images

Mathematical Basis

■ Discrete Cosine Transform

$$D_m^M(u) = c_m \sqrt{\frac{2}{M}} \cos\left(\frac{\pi m(2u+1)}{2M}\right) \quad m = 0 \dots M-1$$

$$G(m, n) = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} g(u, v) D_m^M(u) D_n^N(v)$$

Mathematical Basis

■ Discrete Cosine Transform

$$D_m^M(u) = c_m \sqrt{\frac{2}{M}} \underbrace{\cos\left(\frac{\pi m(2u+1)}{2M}\right)}_{\text{Cosine Waves}} \quad m = 0 \dots M-1$$

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Mathematical Basis

■ Discrete Cosine Transform

$$D_m^M(u) = c_m \underbrace{\sqrt{\frac{2}{M}} \cos \left(\overbrace{\frac{\pi m(2u+1)}{2M}}^{\text{Different coefficients}} \right)}_{\text{Cosine Waves}} \quad m = 0 \dots M-1$$

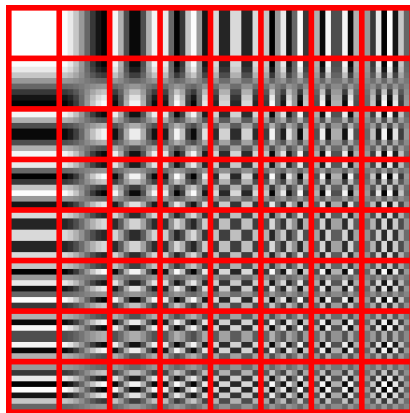
$$G(m, n) = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} g(u, v) D_m^M(u) D_n^N(v)$$

Conceptual Basis

- Based on waves
- Split image into "waves"
 - Vertical
 - Horizontal

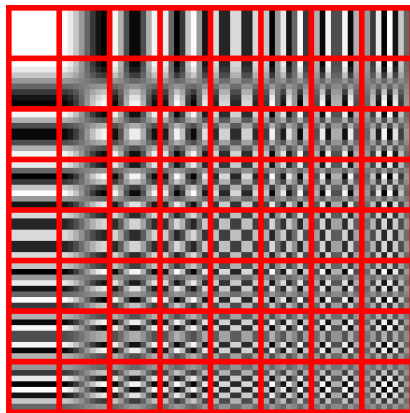
Conceptual Basis

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Conceptual Basis

- Based on waves
- Split image into "waves"
 - Vertical
 - Horizontal
- Want to choose the waves that we remove so that they won't be missed.



Step by Step

- Decompose image into "waves"

Step by Step

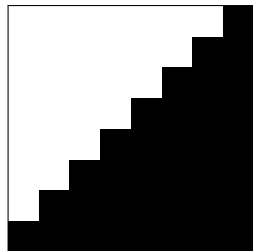
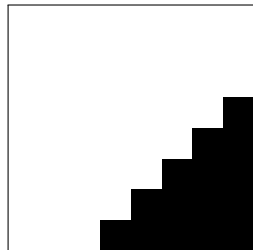
- Decompose image into "waves"
- Arrange waves according to frequency
 - Highest frequency - top left
 - Lowest frequency - bottom right

Step by Step

- Decompose image into "waves"
- Arrange waves according to frequency
 - Highest frequency - top left
 - Lowest frequency - bottom right
- Erase bottom right corner
- Recompile image

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- Decompose image into "waves"
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Original Image



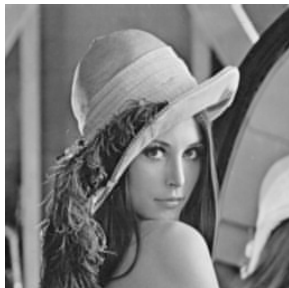
- 236 KB
- Uncompressed GIF image

Results

A bit more information about this



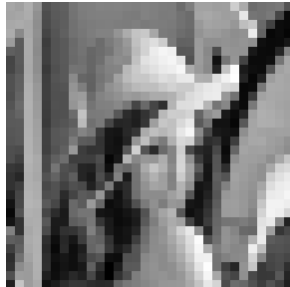
41.4 KB



25.4 KB

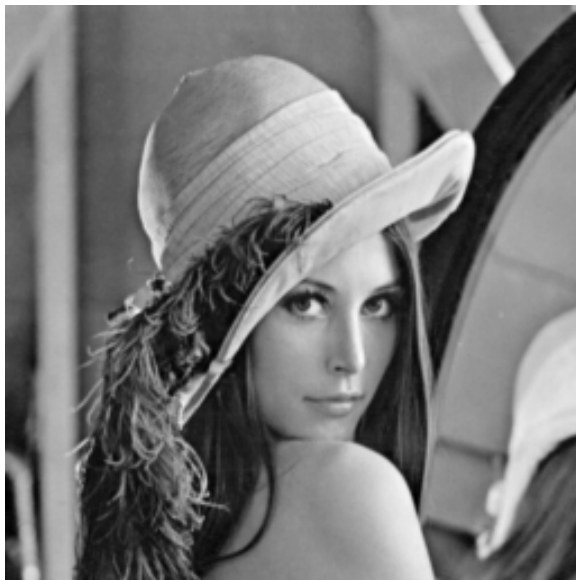


36.9 KB



2.5 KB

Compressed Image



- 41.1 KB
- Compressed JPEG image

