# Jpeg Compression Pictures, Images and Waves

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■ Joint Photographic Experts Group

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- Lossy compression

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  - Smaller file size

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  - Smaller file size
  - Maintain image quality
  - Human perception is limited

Lossy vs Lossless

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  - Compression ratio of  $\frac{20}{10} = 2$
- Many other methods
- JPEG specific to images

#### Mathematical Basis

Discrete Cosine Transform

$$D_m^M(u) = c_m \sqrt{\frac{2}{M}} \cos\left(\frac{\pi m(2u+1)}{2M}\right) \qquad m = 0 \dots M - 1$$

$$G(m,n) = \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} g(u,v) D_m^M(u) D_n^N(u)$$

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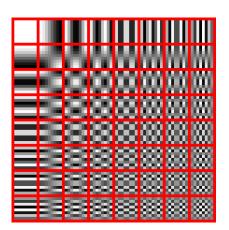
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## Conceptual Basis

- Based on waves
- Split image into "waves"
  - Vertical
  - Horizontal

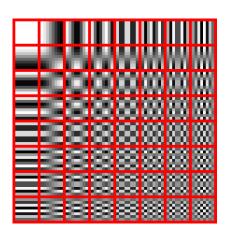
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  - Horizontal
- Want to choose the waves that we remove so that they won't be missed.

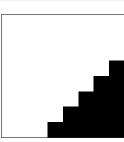


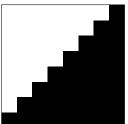
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- Arrange waves according to frequency
  - Highest frequency top left
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## Original Image



- 236 KB
- Uncompressed GIF image

### Results

#### A bit more information about this





## Compressed Image



- 41.1 KB
- Compressed JPEG image