Sorting → Ordering

Ascending
(Non-decreasing)

Descending
(Non-increasing)

A → 1 2 3 4 8 12

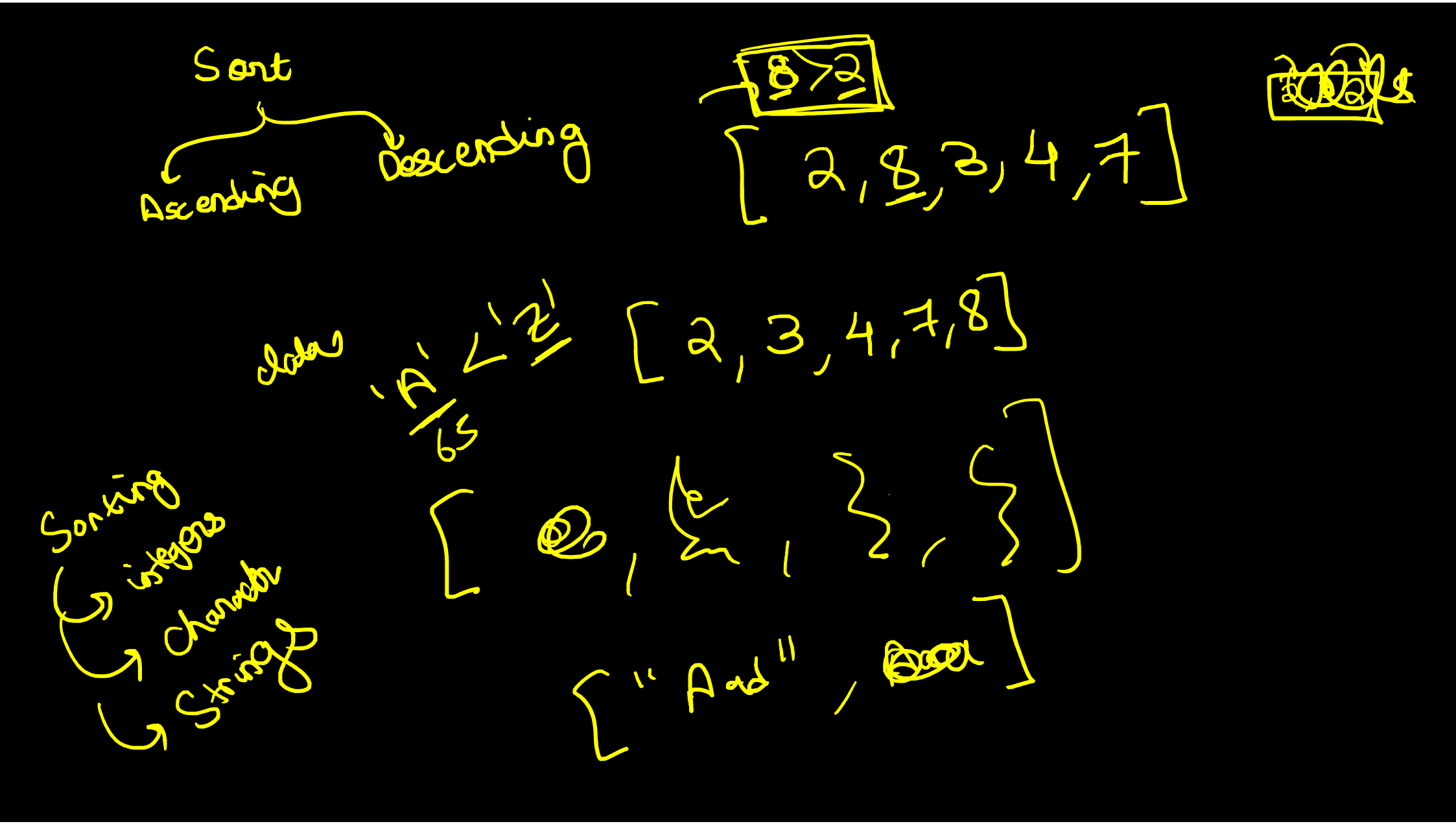
B → 1 2 2 3 4 8 12

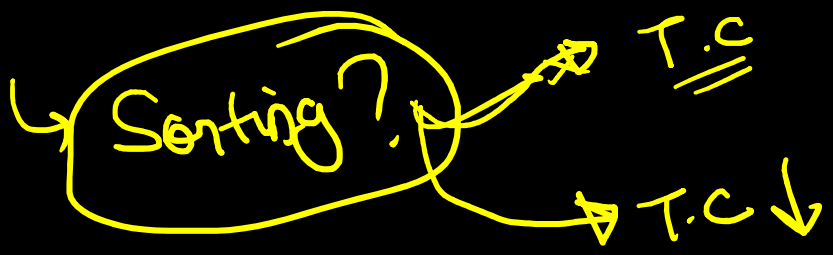
✓ Strictly increasing

Strictly decreasing 7 6 4 3 3 2

arr[::] = → 7 6 4 6

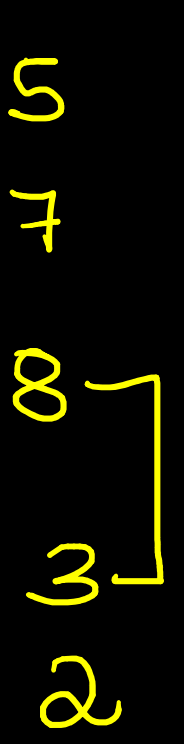
1 4

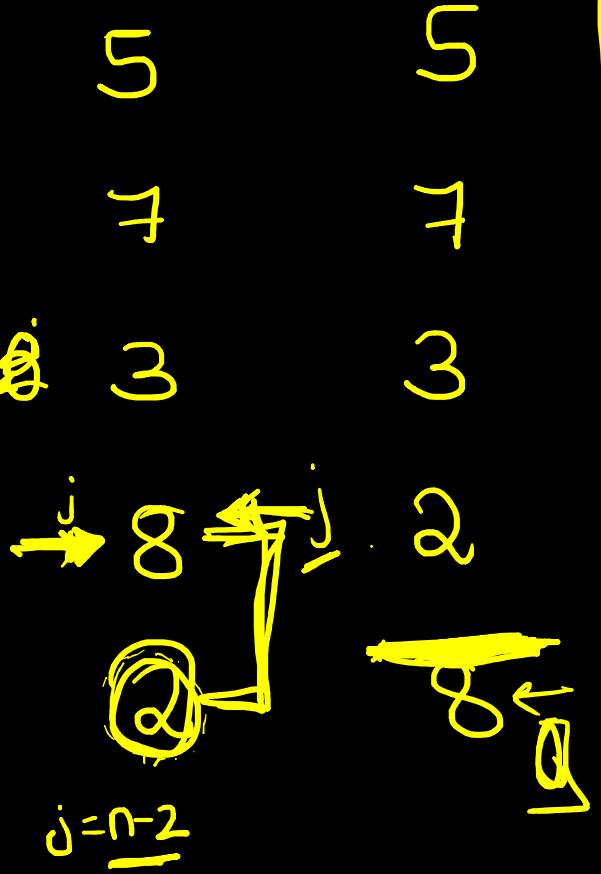

Sort
Ascending
Descending
8 > 2
[2, 8, 3, 4, 7]
Order
'A' < 'Z'
65
[2, 3, 4, 7, 8]
Sorting
integers
Characters
Strings
["Add" ,]

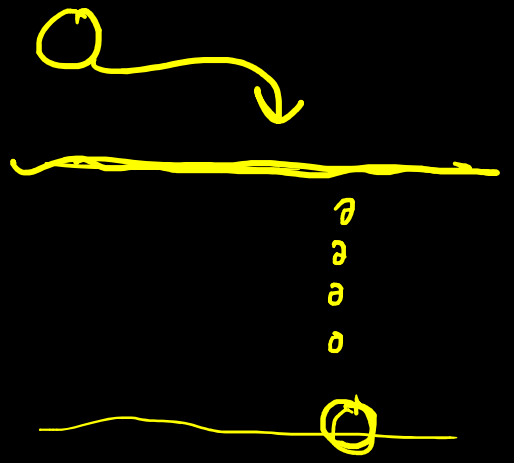

Sorting ?
T.C
T.C

Bubble Sort (Ascending)

8	5	7	3	2







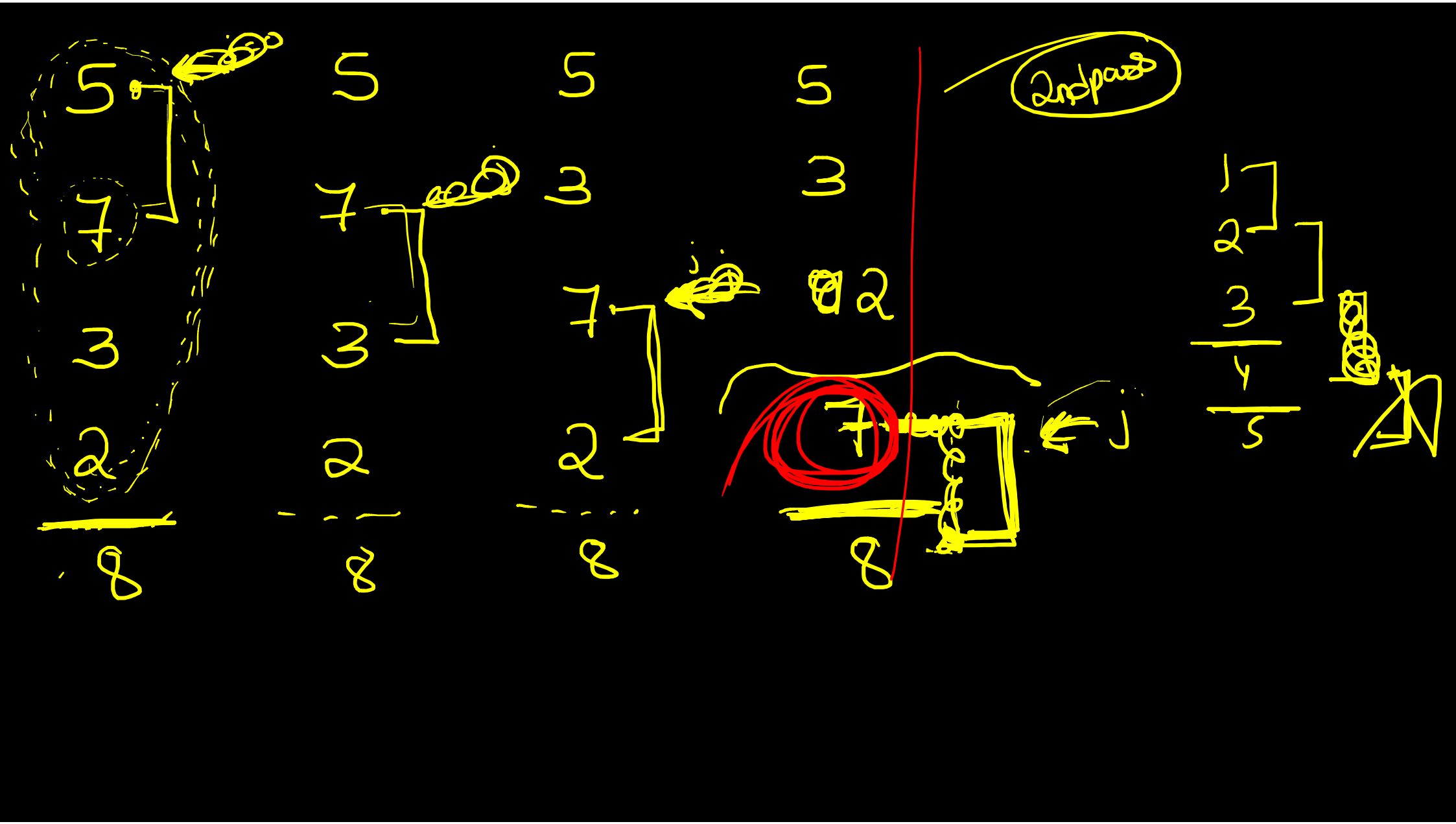
(n-1)

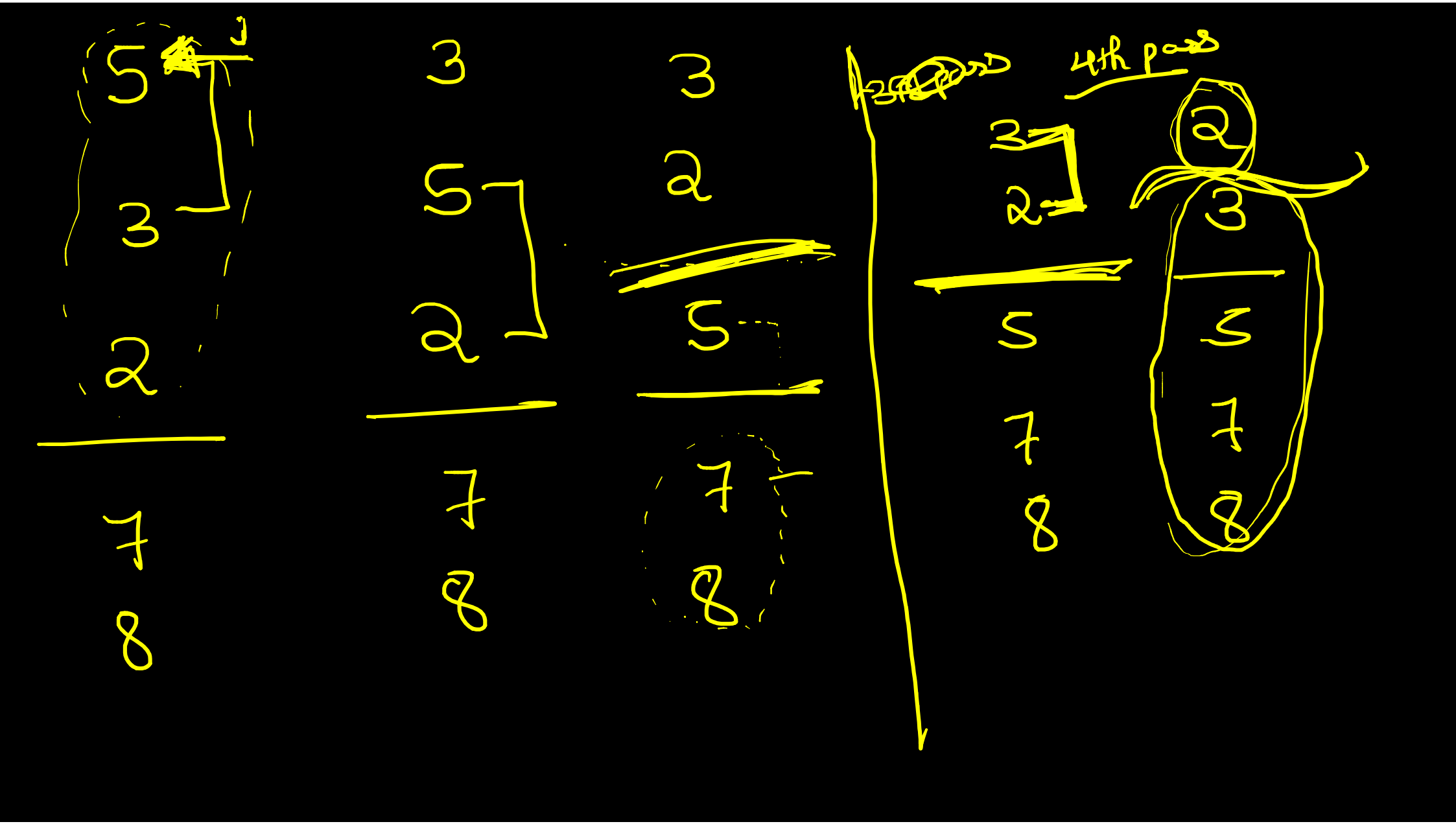
(n-2)

(n-3)

⋮

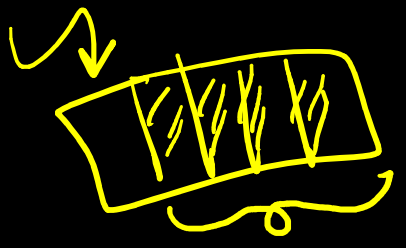
1


5
7
3
2
8
5
7
3
2
8
5
3
2
7
2
8
7
J
2nd pass
1
2
3
4
5


5
3
2
7
8
3
5
2
7
8
5
7
8
4th pass
3
2
5
7
8
2
3
5
7
8

✓ ✓ ✓ ✓ ✓

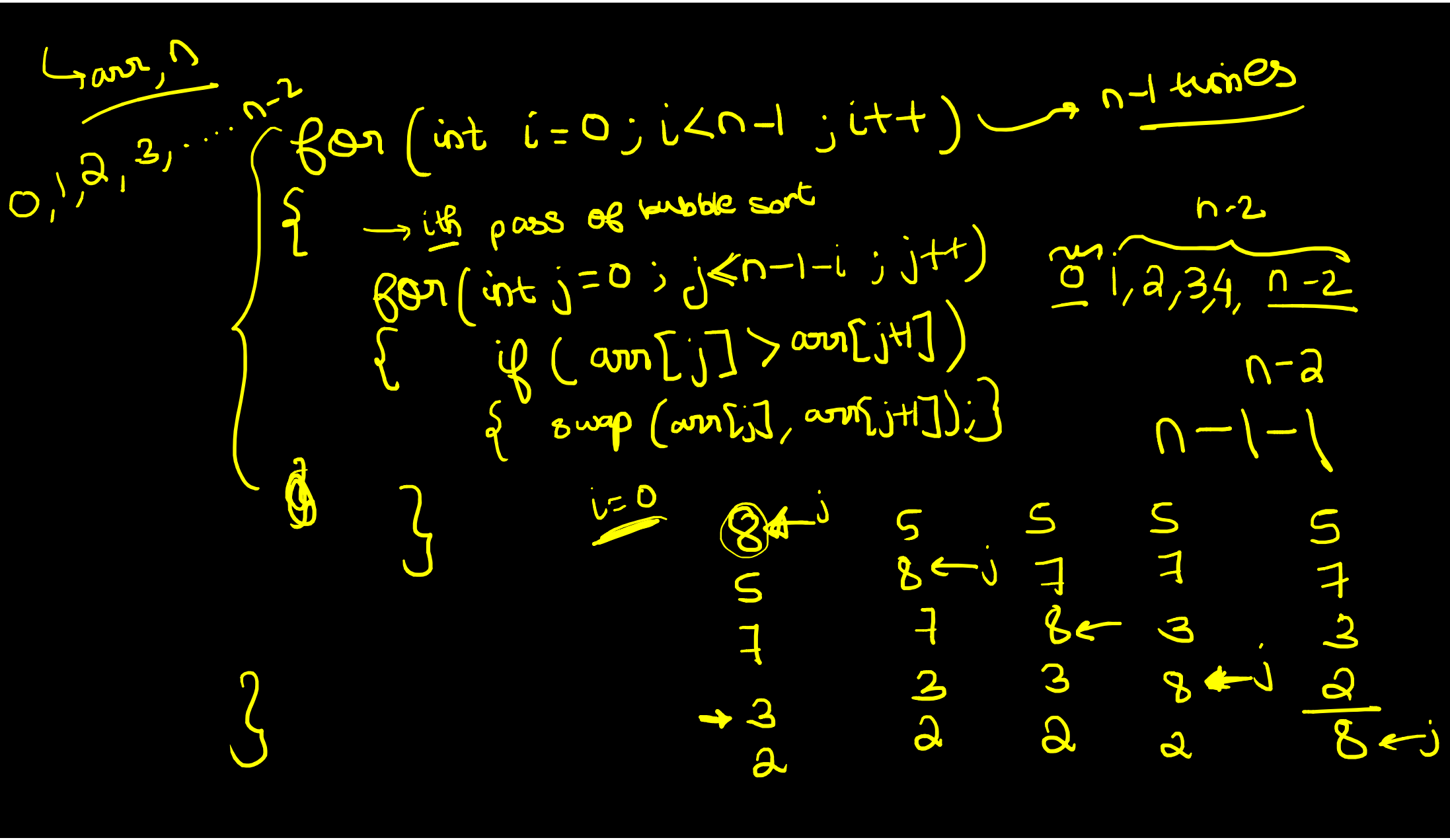
$n \longrightarrow (n-1)$ passes of Bubble sort

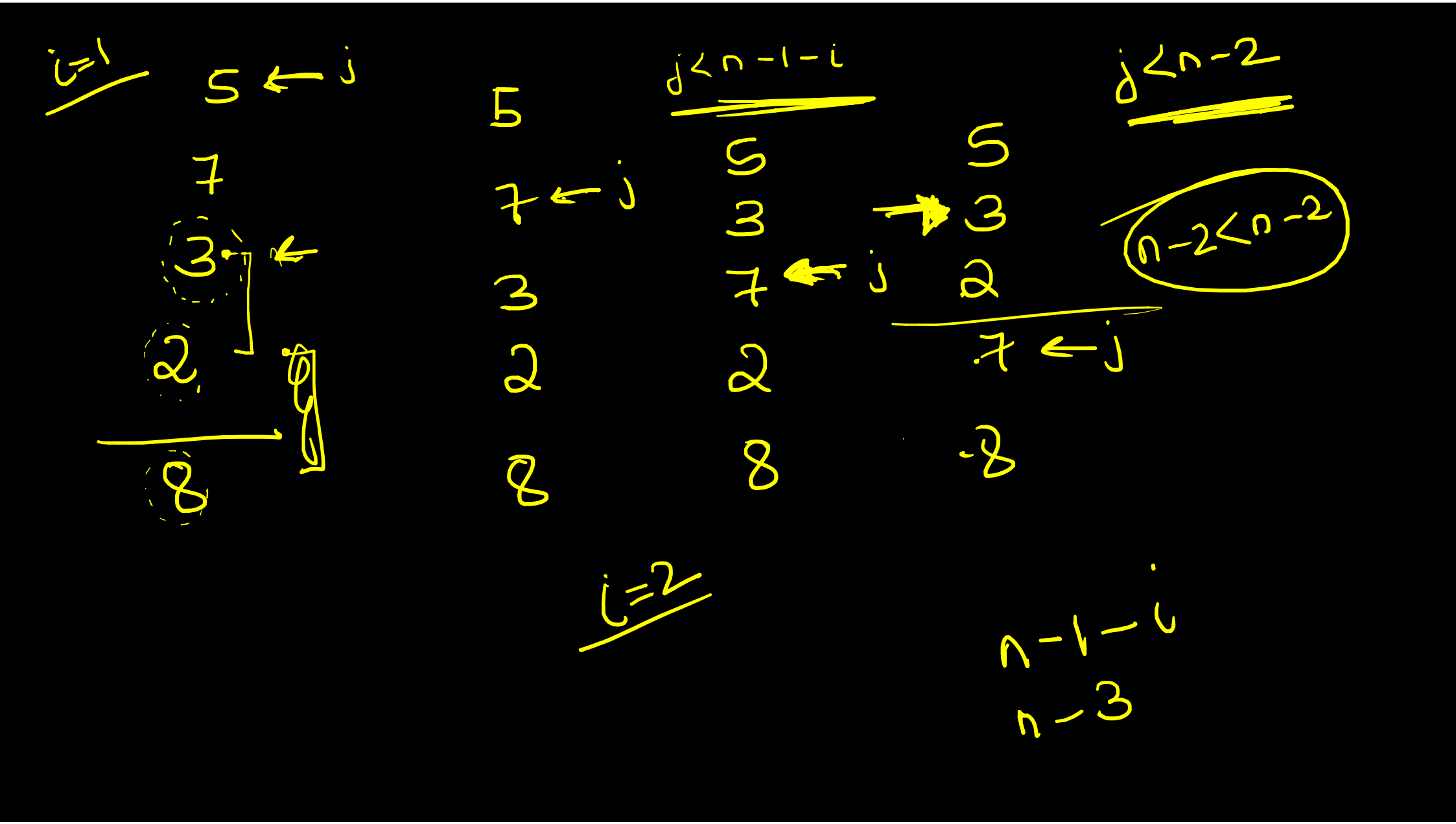


4 passes

$1+2+3 \cdots (n-1)$

$= \frac{n(n-1)}{2}$


arr, n
0, 1, 2, 3, ... n-2
for (int i = 0 ; i < n-1 ; i++) → n-1 times
{
→ ith pass of bubble sort
for (int j = 0 ; j <= n-1-i ; j++)
{
if (arr[j] > arr[j+1])
{ swap (arr[j], arr[j+1]); }
}
}
n-2
0 1, 2, 3, 4, n-2
n-2
n-1-1
i=0
8 ← j
5
7
3
2
5
8 ← j
7
3
2
5
7
8 ←
3
2
5
7
3
8 ← j
2
5
7
3
2
8 ← j


i=1
5 ← j
7
3
2
8
5
7 ← j
3
2
8
j<n-1-i
5
3
7 ← j
2
8
j<n-2
5
3
2
7 ← j
8
n-2<n-2
i=2
n-1-i
n-3

```
for ( int i = 1; i <= n-1 ; i++)
{
    // ith pass of bubble sort
    for (int j=0; j < n-i ; j++)
    {

    }
}
```

j = 0 → n-2

← n

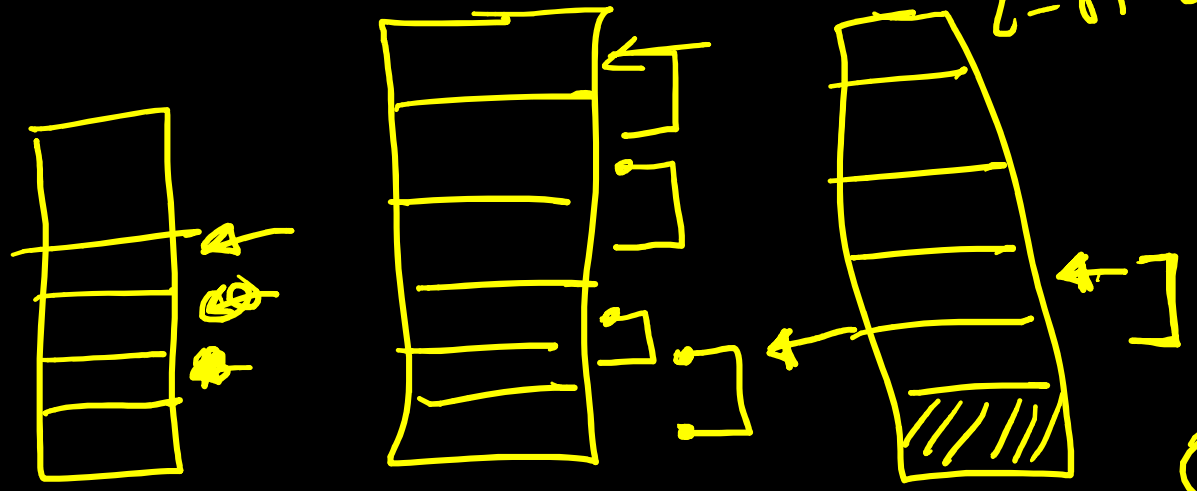
```
for (i=0 ; i<n-1 ; i++)
{  for( int j=0 ; j<n-1-i ; j++ )
   { }
}
```

$i=0 \rightarrow n-1$ times

$i=1 \rightarrow n-2$ times

$i=2 \rightarrow n-3$

$i=n-2 \rightarrow 1$ times



$$\frac{n(n-1)}{2}$$

$$O(n^2)$$

$O(n^2)$

$O(1)$

$\frac{n(n-1)}{2}$

① Find 2 long

② Find k th largest $arr[n-k]$

Stable

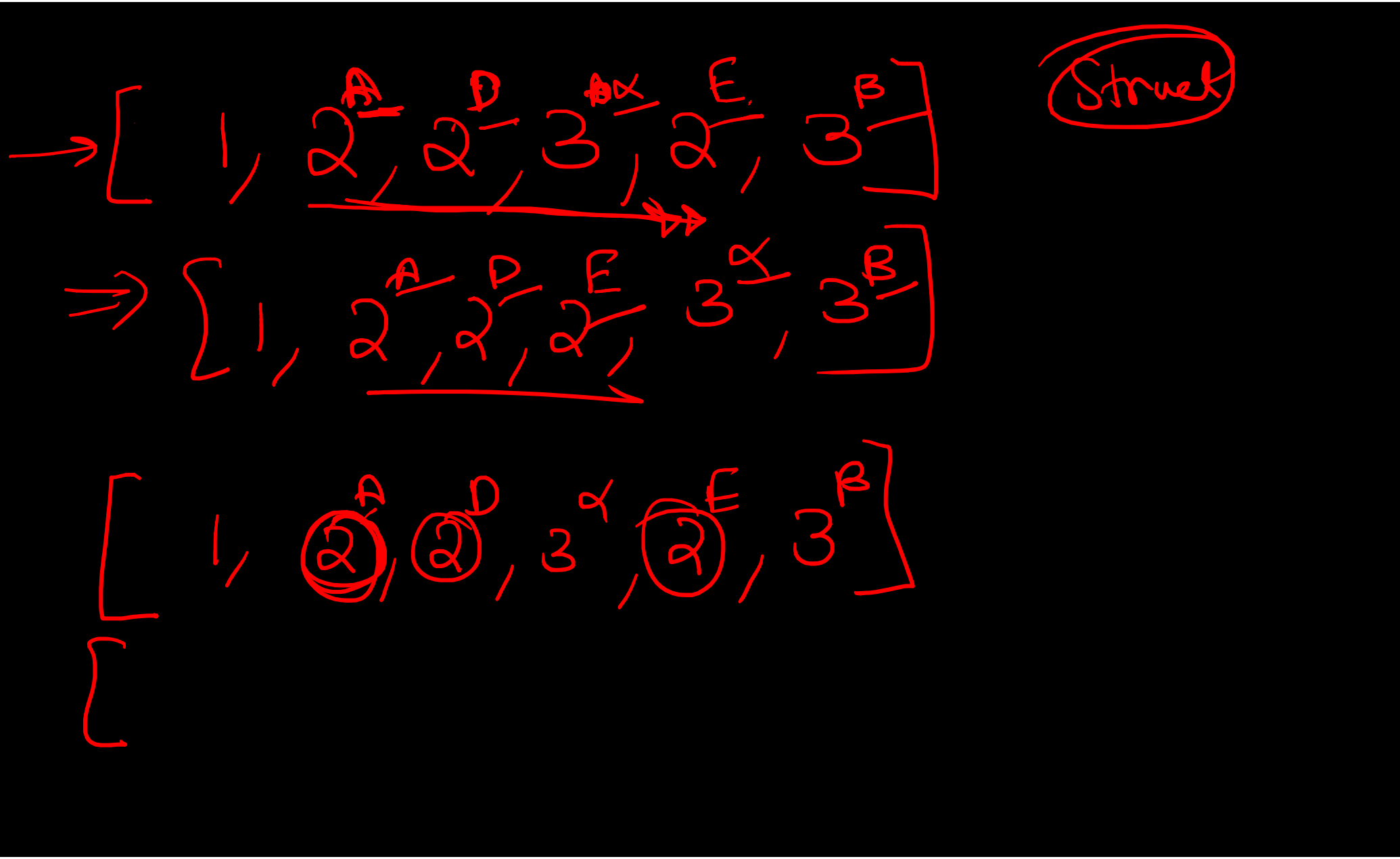
[1, 2, 8*, 7, 8B]

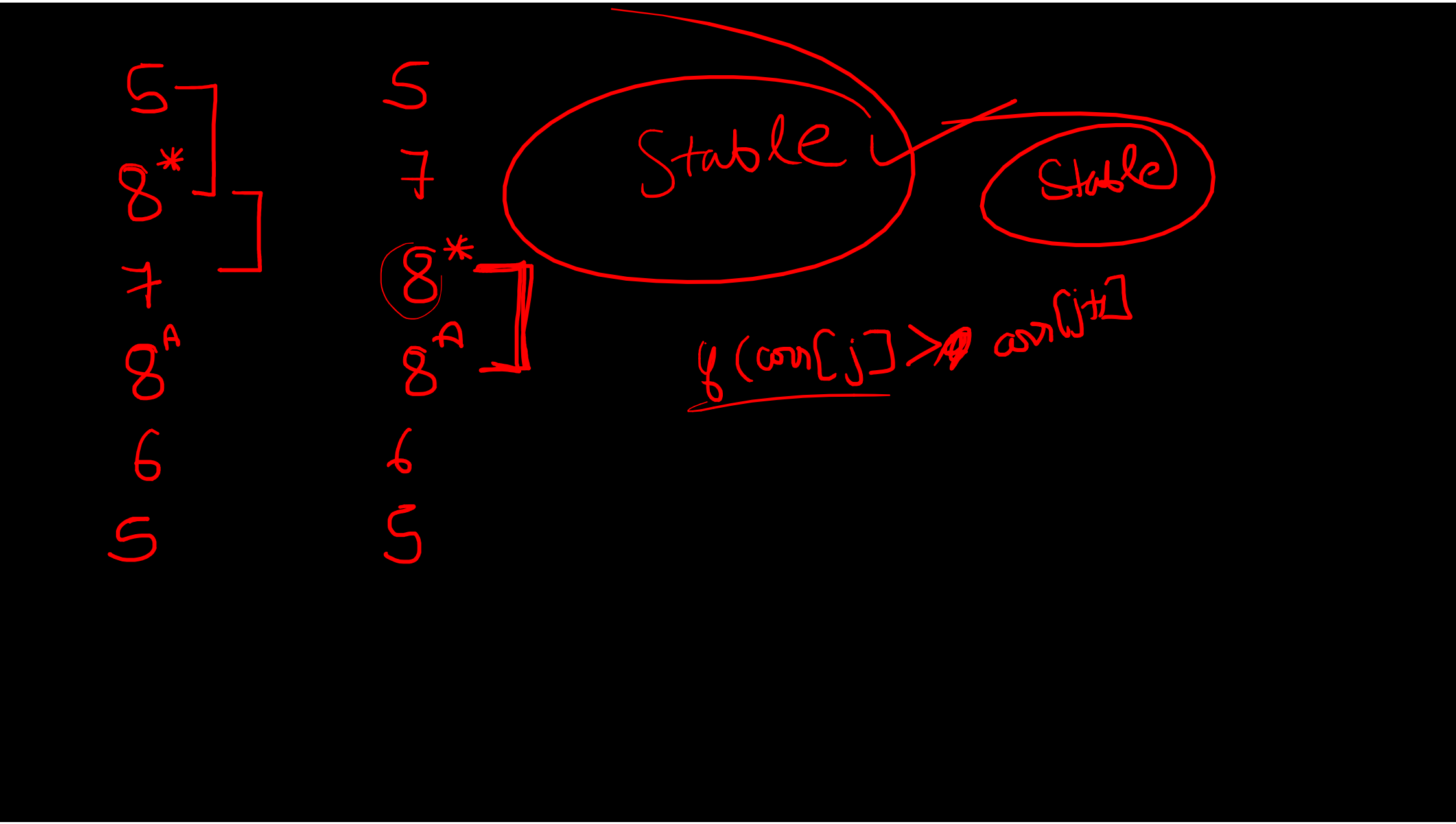
A, B

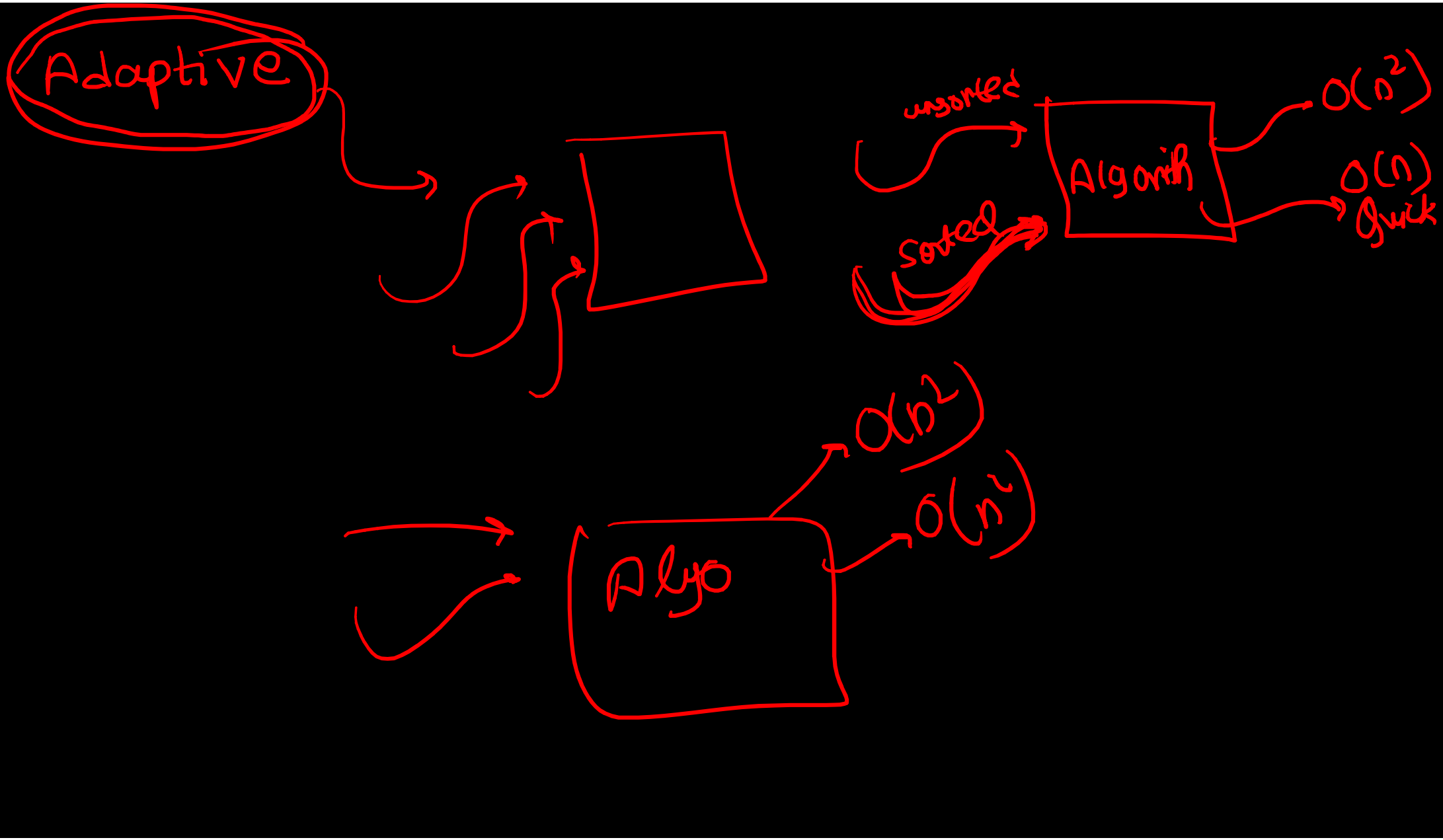
[B, A]

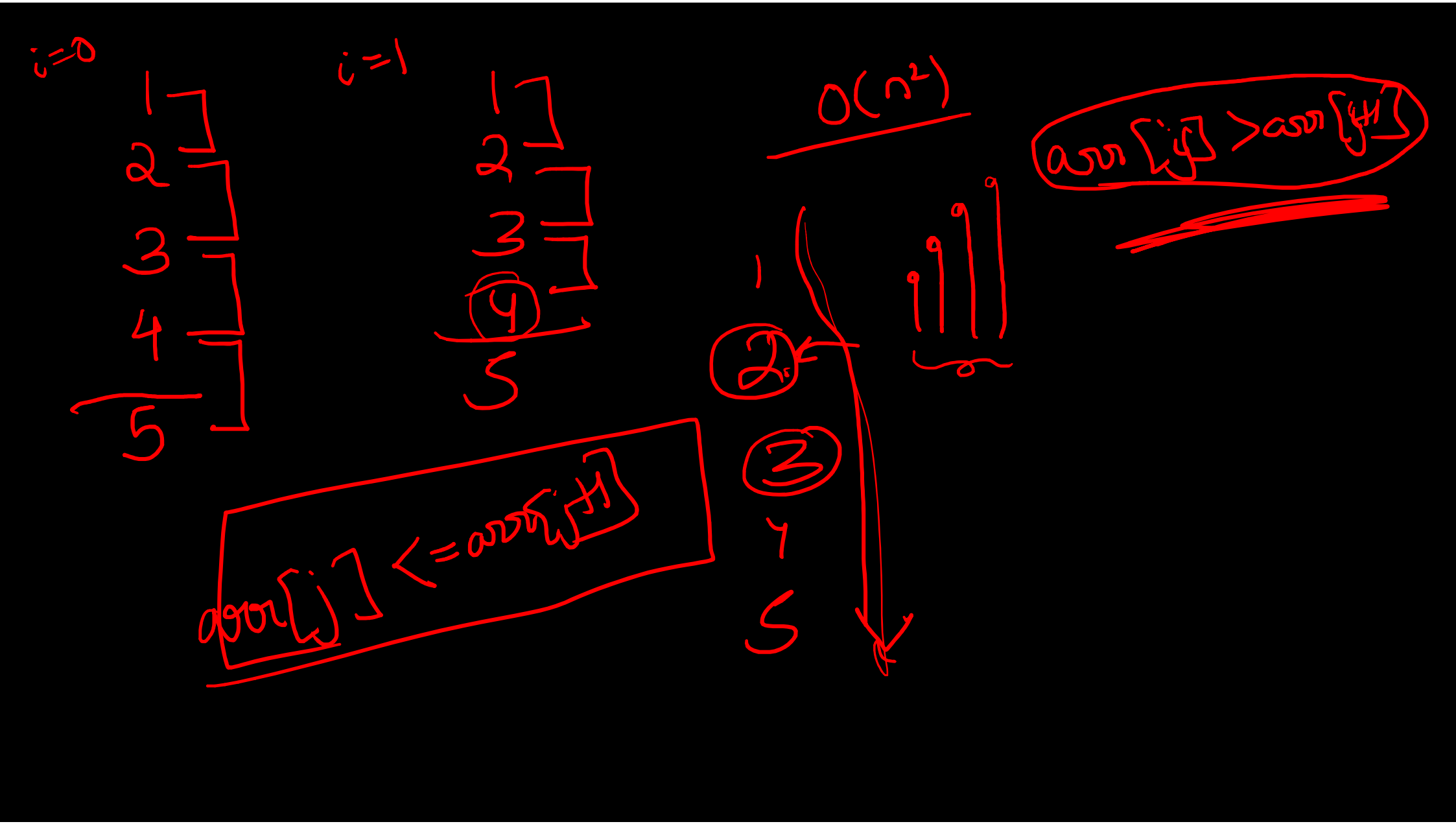
[1, 2, 7, 8B, 8A]

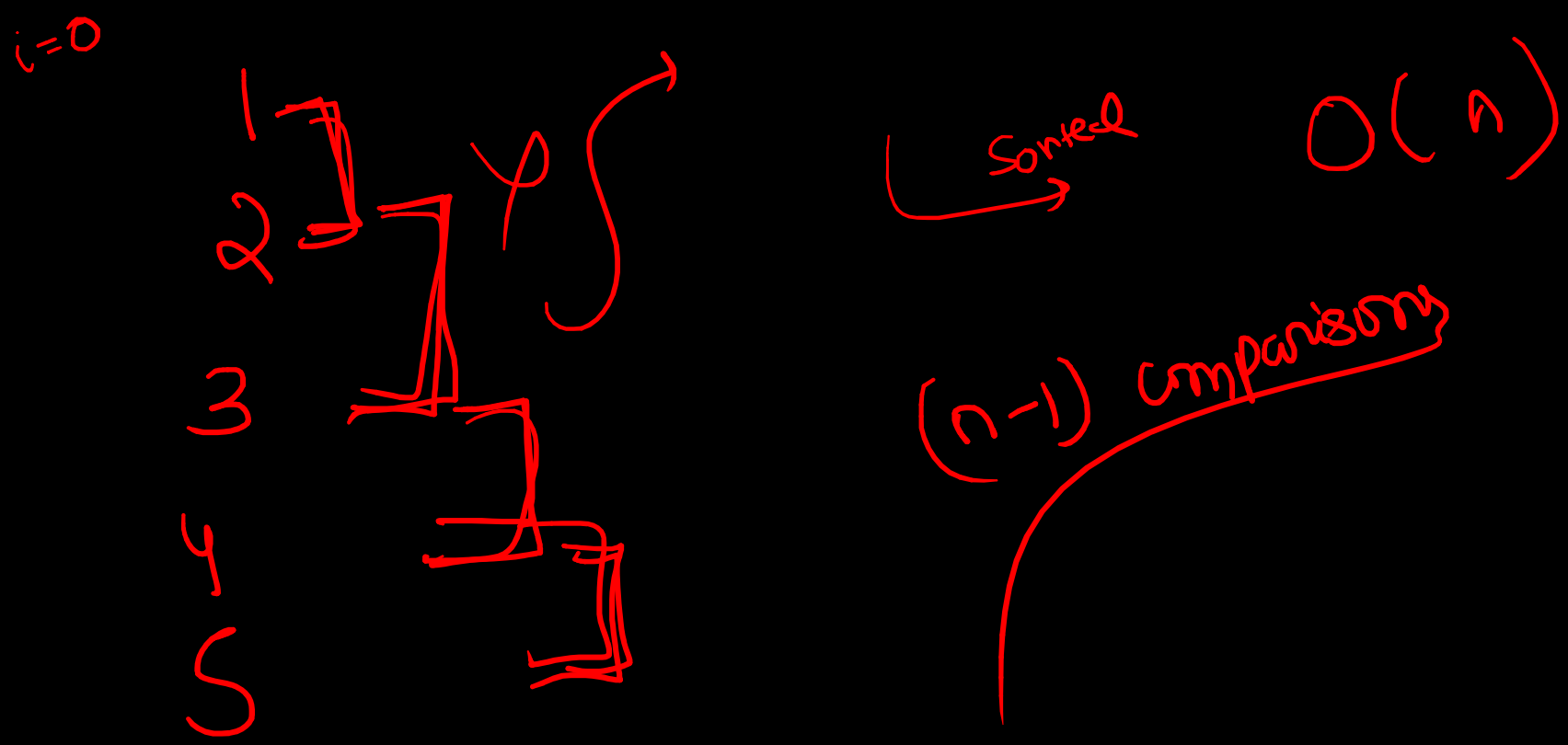
unstable

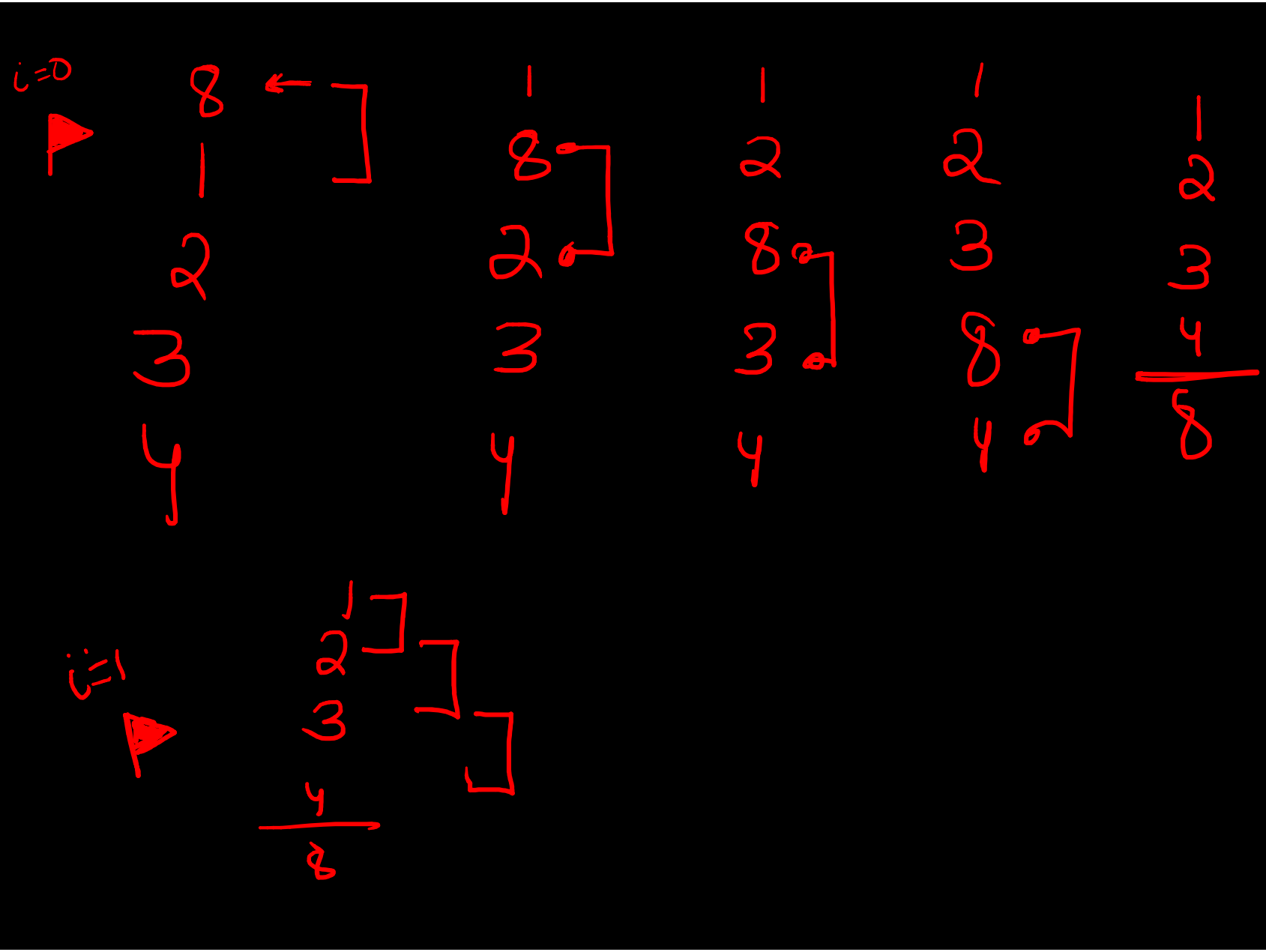

[1, 2^A, 2^D, 3^α, 2^E, 3^B]
Struct
[1, 2^A, 2^D, 2^E, 3^α, 3^B]
[1, 2^A, 2^D, 3^α, 2^E, 3^B]
[


5
8*
7
8^A
6
5
5
7
8*
8^A
6
5
Stable
Stable
if (arr[j] > arr[j+1]


Adaptive
unsorted
sorted
Algorith
O(n²)
O(n)
Quick
Algo
O(n²)
O(n)


i=0
i=1
O(n²)
arr[j] > arr[j+1]
arr[j] <= arr[j+1]


i=0
1
2
3
4
5
Sorted
O(n)
(n-1) comparisons


i=0
8
1
2
3
4
1
8
2
3
4
1
2
8
3
4
1
2
3
8
4
1
2
3
4
8
i=1
2
3
4
8