Matlab problem 1

You know (Maxwell's devil told you) that the value of bilirubin in the blood of a healthy person is a Gaussian random variable with mean μ_0 and variance σ_0^2 ; a person with pancreas tumor has the value of bilirubin in the blood which is again Gaussian with mean μ_1 and variance σ_1^2 . You decide that the bilirubin test is positive if the measured bilirubin value is above threshold T.

Write the formulas of your test specificity and sensitivity. Let us say that the incidence of pancreas tumor in the population is p. Write the formulas for the probabilities $P(D_y|T_p)$ that a person really is affected by pancreas tumor given that the test is positive and $P(D_n|T_n)$ that a person really is healthy given that the test is negative.

Write a Matlab script that plots:

- 1. test sensitivity and specificity as functions of the threshold T
- 2. $P(D_y|T_p)$ as function of T and p (a surface, you can use mesh or meshc)
- 3. $P(D_n|T_n)$ as function of T and p (a surface, you can use mesh or meshc)
- 4. the superimposed contour plots of $P(D_y|T_p)$ and $P(D_n|T_n)$ at probability values 0.5, 0.9, 0.99, 0.999, 0.9999

Use initially

- $\mu_0 = 10, \, \sigma_0^2 = 4$
- $\mu_1 = 15, \, \sigma_1^2 = 8$

then, once you can plot the results for this case, change these values and comment the results.