# Measurement and Optimal Measurement of a Non-linear Solenoid Valve

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Final Project Presentation - EE5630



### Outline of the Presentation

- Introduction
- Background and Motivation
- Problem Formulation
- Dynamics and Cost Function
- Analysis and Simulation
- Conclusion

Introduction

### What is a Solenoid Valve?

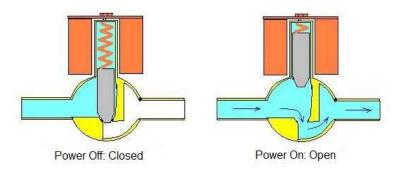


Figure: A Solenoid Valve

### **Background and Motivation**

#### Solenoid Valves: Possible Applications

- Hydraulics for actuation
- On/Off fluid flow for mixing
- Pressure application for injection molding
- Fast switching is often desirable
- Fast switching can cause a non-linear response
- Our objective is to have a fast, linear response with a minimized control input

### **Problem Formulation**

#### Methods of Acquiring Dynamics

- Data Sheet
- Analyzing the physics of the mechanisms within the system to analytically solve for the differential equations
- Opening Physically test the input and output of a system using sensors

Method 3 was used for this project

### Solenoid Valve: Modeling

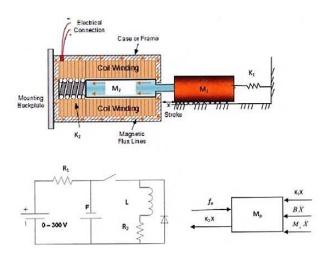
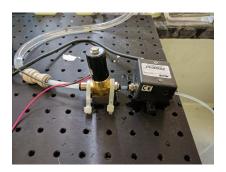
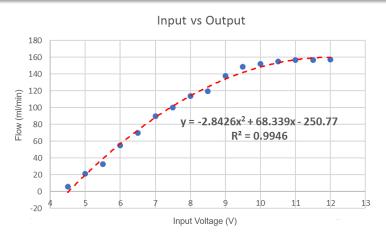


Figure: Solenoid Valve With Equivalent Circuit and Free Body Diagram

### Testbed

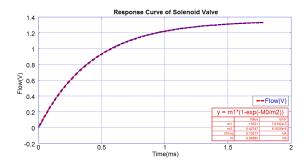
 A testbed was assembled to record the solenoid's response to a step input of 12V





- The curve is nonlinear
- Linearizing the transfer function was found to not dramatically affect the final output
- For simplicity it was assumed to be linear.

### Response Curves



 The response to a step input had the same form as a charging capacitor, a curve fit was applied using the equation of a charging capacitor

### Dynamics of the System

The derivative of equation (1), equation (2) is our first state equation

#### **Charging Capacitor Model**

$$Q = Cu(t)(1 - e^{\frac{-t}{RC}}) \tag{1}$$

$$dx = \frac{u(t)}{R} \left(e^{\frac{-t}{RC}}\right) \tag{2}$$

#### **Cost Function**

- Goal was to follow a predetermined line to linearize response and to minimize control effort
- Both a tracking function and a minimum control effort component were added to the cost function shown in Equation (3)

#### **Cost Function**

$$J = \int_{t_0}^{t_f} ||x(t) - r(t)||_Q^2 + u(t)^2 dt$$
 (3)

### Optimal Control Approach

Pontryagin's was used due to the non-linearity of our system. By definition, the control u\* causes the functional J to have a relative minimum if:

#### Pontryagin's Minimum Principle

$$J(u) - J(u*) = \Delta J \ge 0 \tag{4}$$

### Optimal Control Approach

• The Hamiltonian(5) was used to determine the state equation (7) co-state equation(8) and the necessary condition for u\*

#### **Equations**

$$H = g + p[a] \tag{5}$$

$$H = (x - .7493)^{2} + u^{2} + p(\frac{100000ue^{\frac{-100000t}{42747}}}{42747})$$
 (6)

#### **Necessary Condition Equations**

$$\frac{\partial H}{\partial p} = \dot{x} = \frac{100000ue^{\left(\frac{-100000t}{42747}\right)}}{42747} \tag{7}$$

$$\frac{\partial H}{\partial x} = \dot{p} = 2x1.5t\tag{8}$$

$$\frac{\partial H}{\partial u} = 2u + \frac{-100000pe^{\left(\frac{-100000t}{42747}\right)}}{42747} \tag{9}$$

- The necessary condition for u\* can be determined setting equation (9) equal to zero and solving for u
- The analytical solutions to these equations were cross checked in Matlab by using a symbolic solver

- Once the state and co-state equations were determined,
  MATLAB function bvp4c was used to determine x and p
- These values were then substituted back into u\* shown in equation (9)

u\*

$$u^* = \frac{-100000pe^{\left(\frac{-50000t}{42747}\right)}}{42747} \tag{10}$$

#### **Initial Simulation**

- The first simulation had zero weighting added to the cost function is equation (3)
- The minimum control effort component of the cost function seems to be dominant
- Weighting will be introduced in future trials

### **Initial Simulation Results**

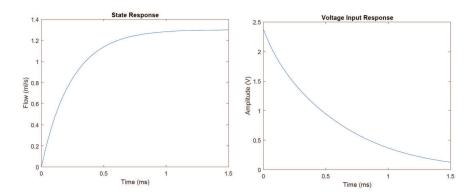


Figure: Zero Weight Response

### Weighting

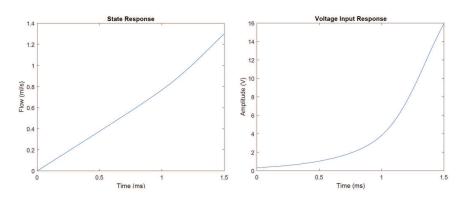


Figure: 5000 Weight Response

• A weighting factor of 5000 was added to the tracking function component, but ended up being too high

### Weighting

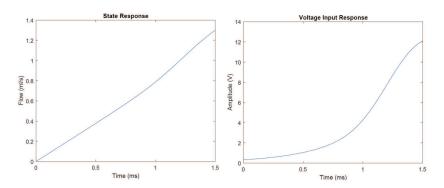


Figure: 2750 Weight Response

 After various trials a weighting factor of 2750 was used and the response was as expected

### But Wait There's More!!!



Figure: Billy Mays

### Physical Test

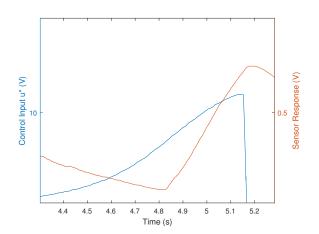


Figure: u\* input (V) and Sensor Response (V) vs. Time (s)

### Physical Test cont.

- The optimal control input u\* was applied to the actual solenoid valve
- The sensor's response was linear, confirming simulated results in real application

### Limitations of the work

- Optimal control limited by sensor speed
- Sensors response is linearized
- A faster, more accurate sensor will enhance optimal control's effects

#### Conclusions

- Physical testing was successful and confirmed the control calculated constrains the flow to a linear path
- Error of the final state was approximately 1% which is reasonable for most applications that require a linear flow response

#### Future Work

- Apply nonlinear transfer function to dynamics to eliminate error
- Integrate higher quality flow sensor for accurate data acquisition
- Calibrate pressure drop between two pressure sensors for accurate flow reading

Introduction Problem Formulation Optimal Control Solution Discussion and Conclusion

Thank you!

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## Questions?