CS224N Assignment 1: Exploring Word Vectors (25 Points)

Due 4:30pm, Tue Jan 14

Welcome to CS224n!

Before you start, make sure you read the README.txt in the same directory as this notebook. You will find many provided codes in the notebook. We highly encourage you to read and understand the provided codes as part of the learning:-)

```
In [3]: # All Import Statements Defined Here
         # Note: Do not add to this list.
         # -----
         import sys
         assert sys.version info[0]==3
         assert sys.version_info[1] >= 5
         from gensim.models import KeyedVectors
         from gensim.test.utils import datapath
         import pprint
         import matplotlib.pyplot as plt
         plt.rcParams['figure.figsize'] = [10, 5]
         import nltk
         nltk.download('reuters')
         from nltk.corpus import reuters
         import numpy as np
         import random
         import scipy as sp
         from sklearn.decomposition import TruncatedSVD
         from sklearn.decomposition import PCA
         START_TOKEN = '<START>'
         END TOKEN = '<END>'
         np.random.seed(0)
         random.seed(0)
```

```
[nltk_data] Downloading package reuters to
[nltk_data] /Users/jayakumar/nltk_data...
[nltk_data] Package reuters is already up-to-date!
```

Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from *co-occurrence matrices*, and those derived via *GloVe*.

Assignment Notes: Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

Note on Terminology: The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (Firth, J. R. 1957:11)

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, *co-occurrence matrices* (for more information, see here or here).

Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word w_i occurring in the document, we consider the *context window* surrounding w_i . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document, i.e. words $w_{i-n} \ldots w_{i-1}$ and $w_{i+1} \ldots w_{i+n}$. We build a co-occurrence matrix M, which is a symmetric word-by-word matrix in which M_{ij} is the number of times w_i appears inside w_i 's window among all documents.

Example: Co-Occurrence with Fixed Window of n=1:

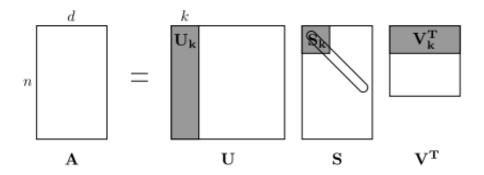
Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

| <start></start> | 0 | 2 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|-----------------|---|---|---|---|---|---|---|---|---|---|
| all | 2 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| that | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 0 |
| glitters | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| is | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 0 |
| not | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 |
| gold | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 |
| well | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 1 |
| ends | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| <end></end> | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 |

Note: In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In thise case we imagine <START> and <END> tokens encapsulating each document, e.g., " <START> All that glitters is not gold <END> ", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run dimensionality reduction. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in U_k .



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. *doctor* and *hospital* will be closer than *doctor* and *dog*.

Notes: If you can barely remember what an eigenvalue is, here's a slow, friendly introduction to SVD. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures 7, 8, and 9 of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing preprogrammed implementations of these algorithms from the numpy, scipy, or sklearn

python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k — known as Truncated SVD — then there are reasonably scalable techniques to compute those iteratively.

Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html. We provide a read_corpus function below that pulls out only articles from the "crude" (i.e. news articles about oil, gas, etc.) category. The function also adds <START> and <END> tokens to each of the documents, and lowercases words. You do **not** have to perform any other kind of preprocessing.

Let's have a look what these documents are like....

```
reuters_corpus = read_corpus()
In [5]:
         pprint.pprint(reuters_corpus[:3], compact=True, width=100)
         [['<START>', 'japan', 'to', 'revise', 'long', '-', 'term', 'energy', 'deman
         d', 'downwards', 'the',
           'ministry', 'of', 'international', 'trade', 'and', 'industry', '(', 'miti
           ')', 'will', 'revise',
           'its', 'long', '-', 'term', 'energy', 'supply', '/', 'demand', 'outlook', by', 'august', 'to',
         'by', 'august',
           'meet', 'a', 'forecast', 'downtrend', 'in', 'japanese', 'energy', 'demand
          , ',', 'ministry',
           'officials', 'said', '.', 'miti', 'is', 'expected', 'to', 'lower', 'the', projection', 'for',
         'projection', 'for',
'primary', 'energy', 'supplies', 'in', 'the', 'year', '2000', 'to', '550'
           'mln', 'kilolitres',
           '(', 'kl', ')', 'from', '600', 'mln', ',', 'they', 'said', '.', 'the', 'd
         ecision', 'follows',
           'the', 'emergence', 'of', 'structural', 'changes', 'in', 'japanese', 'ind
         ustry', 'following',
   'the', 'rise', 'in', 'the', 'value', 'of', 'the', 'yen', 'and', 'a', 'dec
         line', 'in', 'domestic',
           'electric', 'power', 'demand', '.', 'miti', 'is', 'planning', 'to', 'work
           'out', 'a', 'revised',
           'energy', 'supply', '/', 'demand', 'outlook', 'through', 'deliberations',
         'of', 'committee',
           'meetings', 'of', 'the', 'agency', 'of', 'natural', 'resources', 'and', '
         energy', ',', 'the',
           'officials', 'said', '.', 'they', 'said', 'miti', 'will', 'also', 'review
```

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', 'the', 'breakdown',
  'of', 'energy', 'supply', 'sources', ',', 'including', 'oil', ',', 'nucle
ar', ',', 'coal', 'and',
  'natural', 'gas', '.', 'nuclear', 'energy', 'provided', 'the', 'bulk', 'o
f', 'japan', "'", 's',
   electric', 'power', 'in', 'the', 'fiscal', 'year', 'ended', 'march', '31
', ',', 'supplying',
  'an', 'estimated', '27', 'pct', 'on', 'a', 'kilowatt', '/', 'hour', 'basi
s', ',', 'followed',
   'by', 'oil', '(', '23', 'pct', ')', 'and', 'liquefied', 'natural', 'gas',
'(', '21', 'pct', '),',
   'they', 'noted', '.', '<END>'],
 ['<START>', 'energy', '/', 'u', '.', 's', '.', 'petrochemical', 'industry'
  'cheap', 'oil',
  'feedstocks', ',', 'the', 'weakened', 'u', '.', 's', '.', 'dollar', 'and'
  'a', 'plant',
  'utilization', 'rate', 'approaching', '90', 'pct', 'will', 'propel', 'the
   'streamlined', 'u',
  '.', 's', '.', 'petrochemical', 'industry', 'to', 'record', 'profits', 't
his', 'year', '
  'with', 'growth', 'expected', 'through', 'at', 'least', '1990', ',', 'maj
or', 'company',
  'executives', 'predicted', '.', 'this', 'bullish', 'outlook', 'for', 'che
mical', 'manufacturing',
   'and', 'an', 'industrywide', 'move', 'to', 'shed', 'unrelated', 'business
es', 'has', 'prompted',
'gaf', 'corp', '&', 'lt', ';', 'gaf', '>,', 'privately', '-', 'held', 'ca in', 'chemical', 'inc',
  ',', 'and', 'other', 'firms', 'to', 'aggressively', 'seek', 'acquisitions
   'of', 'petrochemical',
'plants', '.', 'oil', 'companies', 'such', 'as', 'ashland', 'oil', 'inc', '&', 'lt', ';', 'ash', '>,', 'the', 'kentucky', '-', 'based', 'oil', 'refiner', 'and', 'marketer', ',', 'are', 'also',
  'shopping', 'for', 'money', '-', 'making', 'petrochemical', 'businesses', o', 'buy', '.', '"',
'to', 'buy', '.', '"',
    'i', 'see', 'us', 'poised', 'at', 'the', 'threshold', 'of', 'a', 'golden'
, 'period', ',"', 'said',

  'paul', 'oreffice
, '&', 'lt', ';',
            'oreffice', ',', 'chairman', 'of', 'giant', 'dow', 'chemical', 'c
0', '&',
  'dow', '>,', 'adding', ',', '"', 'there', "'", 's', 'no', 'major', 'plant 'capacity', 'being',
  'added', 'around', 'the', 'world', 'now', '.', 'the', 'whole', 'game', 'i
s', 'bringing', 'out',
  'new', 'products', 'and', 'improving', 'the', 'old', 'ones', '."', 'analy
sts', 'say', 'the',
  'chemical', 'industry', "'", 's', 'biggest', 'customers', ',', 'automobil
e', 'manufacturers',
'and', 'home', 'builders', 'that', 'use', 'a', 'lot', 'of', 'paints', 'and', 'plastics', ',',
  'are', 'expected', 'to', 'buy', 'quantities', 'this', 'year', '.', 'u', '
.', 's', '.',
  'petrochemical', 'plants', 'are', 'currently', 'operating', 'at', 'about'
, '90', 'pct',
  'capacity', ',', 'reflecting', 'tighter', 'supply', 'that', 'could', 'hik
e', 'product', 'prices',
  ''capacity', 'this' 'vear', 's', 'said', 'john', 'dosh
  'by', '30', 'to', '40', 'pct', 'this', 'year', ',', 'said', 'john', 'dosh
er', ',', 'managing',
  'director', 'of', 'pace', 'consultants', 'inc', 'of', 'houston', '.', 'de
mand', 'for', 'some'
  'products', 'such', 'as', 'styrene', 'could', 'push', 'profit', 'margins'
  'up', 'by', 'as',
  'much', 'as', '300', 'pct', ',', 'he', 'said', '.', 'oreffice', ',', 'spe
aking', 'at', 'a',
  'meeting', 'of', 'chemical', 'engineers', 'in', 'houston', ',', 'said', '
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dow', 'would', 'easily',
  'top', 'the', '741', 'mln', 'dlrs', 'it', 'earned', 'last', 'year', 'and'
  'predicted', 'it',
'would', 'have', 'the', 'best', 'year', 'in', 'its', 'history', '.', 'in'
  '1985', ',', 'when',
  'oil', 'prices', 'were', 'still', 'above', '25', 'dlrs', 'a', 'barrel', '
and', 'chemical',
  'exports', 'were', 'adversely', 'affected', 'by', 'the', 'strong', 'u', '
 ', 's', '.', 'dollar',
',', 'dow', 'had', 'profits', 'of', '58', 'mln', 'dlrs', '.', '"', 'i', '
believe', 'the',
  'entire', 'chemical', 'industry', 'is', 'headed', 'for', 'a', 'record', '
year', 'or', 'close',
   'to', 'it', ',"', 'oreffice', 'said', '.', 'gaf', 'chairman', 'samuel', '
heyman', 'estimated',
  'that', 'the', 'u', '.', 's', '.', 'chemical', 'industry', 'would', 'repo
rt', 'a', '20', 'pct'
   gain', 'in', 'profits', 'during', '1987', '.', 'last', 'year', ',', 'the
   'domestic',
  'industry', 'earned', 'a', 'total', 'of', '13', 'billion', 'dlrs', ',', '
a', '54', 'pct', 'leap',
  'from', '1985', '.', 'the', 'turn', 'in', 'the', 'fortunes', 'of', 'the',
'once', '-', 'sickly',
  'chemical', 'industry', 'has', 'been', 'brought', 'about', 'by', 'a', 'co
mbination', 'of', 'luck',
  'and', 'planning', ',', 'said', 'pace', "'", 's', 'john', 'dosher', '.',
'dosher', 'said', 'last',
   'year', "'", 's', 'fall', 'in', 'oil', 'prices', 'made', 'feedstocks', 'd
ramatically', 'cheaper',
  'and', 'at', 'the', 'same', 'time', 'the', 'american', 'dollar', 'was', '
weakening', 'against',
  'foreign', 'currencies', '.', 'that', 'helped', 'boost', 'u', '.', 's', '
.', 'chemical', 'exports', '.', 'also', 'helping', 'to', 'bring', 'supply', 'and', 'deman
d', 'into', 'balance',
  'has', 'been', 'the', 'gradual', 'market', 'absorption', 'of', 'the', 'ex
tra', 'chemical',
  'manufacturing', 'capacity', 'created', 'by', 'middle', 'eastern', 'oil',
'producers', 'in',

'the', 'early', '1980s', '.', 'finally', ',', 'virtually', 'all', 'major'
  'chemical', 'manufacturers', 'have', 'embarked', 'on', 'an', 'extensive',
'corporate',
  'restructuring', 'program', 'to', 'mothball', 'inefficient', 'plants', ',
  'trim', 'the',
  'payroll', 'and', 'eliminate', 'unrelated', 'businesses', '.', 'the', 're
structuring', 'touched',
  'off', 'a', 'flurry', 'of', 'friendly', 'and', 'hostile', 'takeover', 'at
tempts', '.', 'gaf', ',',
  'which', 'made', 'an', 'unsuccessful', 'attempt', 'in', '1985', 'to', 'ac
quire', 'union',
  'carbide', 'corp', '&', 'lt', ';', 'uk', '>,', 'recently', 'offered', 'th
ree', 'billion', 'dlrs',
  'for', 'borg', 'warner', 'corp', '&', 'lt', ';', 'bor', '>,', 'a', 'chica
go', 'manufacturer',
                     'and', 'chemicals', '.', 'another', 'industry', 'powerh
  'of', 'plastics',
ouse', ', ', 'w', '.', 'r', 'grace', '&', 'lt', ';', 'gra', '>', 'has', 'divested', 'its',
'retailing', ',
  'restaurant',
                 'and', 'fertilizer', 'businesses', 'to', 'raise', 'cash', '
for', 'chemical'
  'acquisitions', '.', 'but', 'some', 'experts', 'worry', 'that', 'the', 'c
hemical', 'industry',
  'may', 'be', 'headed', 'for', 'trouble', 'if', 'companies', 'continue', '
turning', 'their',
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'back', 'on', 'the', 'manufacturing', 'of', 'staple', 'petrochemical', 'c
ommodities', ',', 'such',
  'as', 'ethylene', ',', 'in', 'favor', 'of', 'more', 'profitable', 'specia
lty', 'chemicals',
    'that', 'are', 'custom', '-', 'designed', 'for', 'a', 'small', 'group', '
    of', 'buyers', '.', '"',
    'companies', 'like', 'dupont', '&', 'lt', ';', 'dd', '>', 'and', 'monsant
    o', 'co', '&', 'lt', ';',
    'mtc', '>', 'spent', 'the', 'past', 'two', 'or', 'three', 'years', 'tryin
    ''s' 'got' 'out'
g', 'to', 'get', 'out',

'of', 'the', 'commodity', 'chemical', 'business', 'in', 'reaction', 'to',

'how', 'badly', 'the',
   'market', 'had', 'deteriorated', ',"', 'dosher', 'said', '.', '"', 'but',
'i', 'think', 'they',
  'will', 'eventually', 'kill', 'the', 'margins', 'on', 'the', 'profitable'
  'chemicals', 'in',
  'the', 'niche', 'market', '."', 'some', 'top', 'chemical', 'executives',
'share', 'the',

'concern', '.', '"', 'the', 'challenge', 'for', 'our', 'industry', 'is',

''dean' 'from'.
'to', 'keep', 'from',
   'getting', 'carried', 'away', 'and', 'repeating', 'past', 'mistakes', ',"
  'heyman', 'cautioned', '.', '"', 'the', 'shift', 'from', 'commodity', 'ch
emicals', 'may', 'be',
  'ill', '-', 'advised', '.', 'specialty', 'businesses', 'do', 'not', 'stay
   'special', 'long'
  '."', 'houston', '-', 'based', 'cain', 'chemical', ',', 'created', 'this'
, 'month', 'by', 'the',
  'sterling', 'investment', 'banking', 'group', ',', 'believes', 'it', 'can
 , 'generate', '700',
  'mln', 'dlrs', 'in', 'annual', 'sales', 'by', 'bucking', 'the', 'industry
   'trend', '.'
  'chairman', 'gordon', 'cain', ',', 'who', 'previously', 'led', 'a', 'leve
raged', 'buyout', 'of',
   'dupont', "'", 's', 'conoco', 'inc', "'", 's', 'chemical', 'business', ',
 , 'has', 'spent', '1',
'.', '1', 'billion', 'dlrs', 'since', 'january', 'to', 'buy', 'seven', 'p
etrochemical', 'plants',
   'along', 'the', 'texas', 'gulf', 'coast', '.', 'the', 'plants', 'produce'
  'only', 'basic',
  'commodity', 'petrochemicals', 'that', 'are', 'the', 'building', 'blocks'
  'of', 'specialty',
  'products', '.', '"', 'this', 'kind', 'of', 'commodity', 'chemical', 'bus
iness', 'will', 'never',
   'be', 'a', 'glamorous', ',', 'high', '-', 'margin', 'business', ',"', 'ca
in', 'said', ',',
  'adding', 'that', 'demand', 'is', 'expected', 'to', 'grow', 'by', 'about' 'three', 'pct',
                     'garo', 'armen', ',', 'an', 'analyst', 'with', 'dean', '
   'annually', '.',
witter', 'reynolds', ',',
   'said', 'chemical', 'makers', 'have', 'also', 'benefitted', 'by', 'increa
sing', 'demand', 'for',
   'plastics', 'as', 'prices', 'become', 'more', 'competitive', 'with', 'alu
minum', ',', 'wood',
  'and', 'steel', 'products', '.', 'armen', 'estimated', 'the', 'upturn', '
in', 'the', 'chemical',
  'business', 'could', 'last', 'as', 'long', 'as', 'four', 'or', 'five', 'y
ears', ',', 'provided',
  'the', 'u', '.', 's', '.', 'economy', 'continues', 'its', 'modest', 'rate
   'of', 'growth', '.'
  '<END>'],
 ['<START>', 'turkey', 'calls', 'for', 'dialogue', 'to', 'solve', 'dispute'
, 'turkey', 'said',
  'today', 'its', 'disputes', 'with', 'greece', ',', 'including', 'rights',
'on', 'the',
```

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'continental', 'shelf', 'in', 'the', 'aegean', 'sea', ',', 'should', 'be'
, 'solved', 'through',
  'negotiations', '.', 'a', 'foreign', 'ministry', 'statement', 'said', 'th
e', 'latest', 'crisis',
   'between', 'the', 'two', 'nato', 'members', 'stemmed', 'from', 'the', 'co
ntinental', 'shelf',

'dispute', 'and', 'an', 'agreement', 'on', 'this', 'issue', 'would', 'eff
ect', 'the', 'security',

',', 'economy', 'and', 'other', 'rights', 'of', 'both', 'countries', '.',

'"', 'as', 'the',

'issue', 'is', 'basicly', 'political', ',', 'a', 'solution', 'can', 'only
', 'be', 'found', 'by',

'bilateral' 'negotiations', '."', 'the', 'statement', 'said', '.', 'gree
  'bilateral', 'negotiations', ',"', 'the', 'statement', 'said', '.', 'gree
ce', 'has', 'repeatedly',
  'said', 'the', 'issue', 'was', 'legal', 'and', 'could', 'be', 'solved', '
at', 'the',
   'international', 'court', 'of', 'justice', '.', 'the', 'two', 'countries'
   'approached', 'armed',
   'confrontation', 'last', 'month', 'after', 'greece', 'announced', 'it', '
planned', 'oil',
  'exploration', 'work', 'in', 'the', 'aegean', 'and', 'turkey', 'said', 'i
t', 'would', 'also',
   'search', 'for', 'oil', '.', 'a', 'face', '-', 'off', 'was', 'averted', '
when', 'turkey',
   'confined', 'its', 'research', 'to', 'territorrial', 'waters', '.', '"',
'the', 'latest',
   'crises', 'created', 'an', 'historic', 'opportunity', 'to', 'solve', 'the
   'disputes', 'between',
  'the', 'two', 'countries', ',"', 'the', 'foreign', 'ministry', 'statement
  , 'said', '.', 'turkey',
"'", 's', 'ambassador', 'in', 'athens', ',', 'nazmi', 'akiman', ',', 'was
 , 'due', 'to', 'meet',
  'prime', 'minister', 'andreas', 'papandreou', 'today', 'for', 'the', 'gre
ek', 'reply', 'to', 'a', 'message', 'sent', 'last', 'week', 'by', 'turkish', 'prime', 'minister',
'turgut', 'ozal', '.',
   'the', 'contents', 'of', 'the', 'message', 'were', 'not', 'disclosed', '.
', '<END>']]
```

Question 1.1: Implement distinct_words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus. You can do this with for loops, but it's more efficient to do it with Python list comprehensions. In particular, this may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information.

You may find it useful to use Python sets to remove duplicate words.

```
In [7]:
        # -----
        # Run this sanity check
        # Note that this not an exhaustive check for correctness.
         # -----
        # Define toy corpus
        test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, ENI
        test_corpus_words, num_corpus_words = distinct_words(test_corpus)
        # Correct answers
        ans test corpus words = sorted([START TOKEN, "All", "ends", "that", "gold",
        ans_num_corpus_words = len(ans_test_corpus_words)
        # Test correct number of words
        assert(num_corpus_words == ans_num_corpus_words), "Incorrect number of dist
        # Test correct words
        assert (test corpus words == ans test corpus words), "Incorrect corpus word
        # Print Success
        print ("-" * 80)
        print("Passed All Tests!")
        print ("-" * 80)
```

----Passed All Tests!

Question 1.2: Implement compute_co_occurrence_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n Python NumPy tutorial.

```
def compute co occurrence matrix(corpus, window size=4):
In [8]:
             """ Compute co-occurrence matrix for the given corpus and window_size
                 Note: Each word in a document should be at the center of a window.
                       number of co-occurring words.
                       For example, if we take the document "<START> All that glitte
                       "All" will co-occur with "<START>", "that", "glitters", "is",
                 Params:
                     corpus (list of list of strings): corpus of documents
                     window size (int): size of context window
                 Return:
                     M (a symmetric numpy matrix of shape (number of unique words in
                         Co-occurence matrix of word counts.
                         The ordering of the words in the rows/columns should be the
                     word2Ind (dict): dictionary that maps word to index (i.e. row/c
             words, num_words = distinct_words(corpus)
             M = None
             word2Ind = {}
             # -----
             # Write your implementation here.
             for index, word in enumerate(words):
                 word2Ind[word] = index
             M = np.zeros((num words, num words))
             for d, doc in enumerate(corpus):
                 for t, token in enumerate(doc):
                     j = max(0, t - window_size)
                     while j <= min(t + window_size, len(doc) - 1):</pre>
                         if j != t:
                             M[word2Ind[doc[t]]][word2Ind[doc[j]]] = M[word2Ind[doc|
                         j = j + 1
              _____
             return M, word2Ind
```

```
In [9]:
         # Run this sanity check
         # Note that this is not an exhaustive check for correctness.
         # ______
         # Define toy corpus and get student's co-occurrence matrix
         test corpus = ["{} All that glitters isn't gold {}".format(START TOKEN, ENI
         M_test, word2Ind_test = compute_co_occurrence_matrix(test_corpus, window_si
         # Correct M and word2Ind
         M_test_ans = np.array(
             [[0., 0., 0., 0., 0., 1., 0., 0., 1.,],
              [0., 0., 1., 1., 0., 0., 0., 0., 0., 0., ],
              [0., 1., 0., 0., 0., 0., 0., 1., 0.,],
              [0., 1., 0., 0., 0., 0., 0., 0., 1.,],
              [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
              [0., 0., 0., 0., 0., 0., 1., 1., 0.,],
              [1., 0., 0., 0., 0., 0., 1., 0., 0., ],
              [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
              [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.,],
              [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
         ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold",
         word2Ind_ans = dict(zip(ans_test_corpus_words, range(len(ans_test_corpus_words))
         # Test correct word2Ind
         assert (word2Ind ans == word2Ind test), "Your word2Ind is incorrect:\nCorre
         # Test correct M shape
         assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.\r'
         # Test correct M values
         for w1 in word2Ind ans.keys():
             idx1 = word2Ind ans[w1]
             for w2 in word2Ind_ans.keys():
                 idx2 = word2Ind_ans[w2]
                 student = M_test[idx1, idx2]
                 correct = M_test_ans[idx1, idx2]
                 if student != correct:
                     print("Correct M:")
                     print(M test ans)
                     print("Your M: ")
                     print(M test)
                     raise AssertionError("Incorrect count at index ({}, {})=({}, {]
         # Print Success
         print ("-" * 80)
         print("Passed All Tests!")
         print ("-" * 80)
```

Passed All Tests!

Question 1.3: Implement reduce_to_k_dim [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

Note: All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD.

```
In [10]:
         def reduce_to_k_dim(M, k=2):
              """ Reduce a co-occurence count matrix of dimensionality (num_corpus_wo
                 to a matrix of dimensionality (num corpus words, k) using the following
                      - http://scikit-learn.org/stable/modules/generated/sklearn.deco
                 Params:
                     M (numpy matrix of shape (number of unique words in the corpus
                     k (int): embedding size of each word after dimension reduction
                 Return:
                     M_reduced (numpy matrix of shape (number of corpus words, k)):
                             In terms of the SVD from math class, this actually retu
              0.00
                              # Use this parameter in your call to `TruncatedSVD`
             n_iters = 10
             M reduced = None
             print("Running Truncated SVD over %i words..." % (M.shape[0]))
                  # -----
                 # Write your implementation here.
              svd = TruncatedSVD(n components=k, n iter=n iters)
             M_reduced = svd.fit_transform(M)
                  # -----
             print("Done.")
             return M_reduced
```

```
In [11]: | # -----
         # Run this sanity check
         # Note that this is not an exhaustive check for correctness
         # In fact we only check that your M_reduced has the right dimensions.
         # -----
         # Define toy corpus and run student code
         test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN, ENI
         M_test, word2Ind_test = compute_co_occurrence_matrix(test_corpus, window_si
         M_test_reduced = reduce_to_k_dim(M_test, k=2)
         # Test proper dimensions
         assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have
         assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should ha
         # Print Success
         print ("-" * 80)
         print("Passed All Tests!")
         print ("-" * 80)
```

```
Running Truncated SVD over 10 words...

Done.

-----
Passed All Tests!
```

Question 1.4: Implement plot_embeddings [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code. In the future, a good way to make a plot is to look at the Matplotlib gallery, find a plot that looks somewhat like what you want, and adapt the code they give.

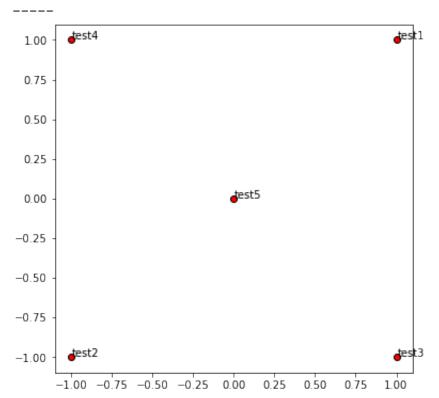
""" Plot in a scatterplot the embeddings of the words specified in the

def plot embeddings(M reduced, word2Ind, words):

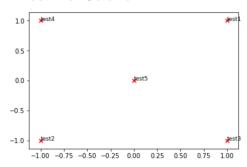
In [12]:

```
NOTE: do not plot all the words listed in M_reduced / word2Ind.
                  Include a label next to each point.
                  Params:
                     M reduced (numpy matrix of shape (number of unique words in the
                     word2Ind (dict): dictionary that maps word to indices for matri
                     words (list of strings): words whose embeddings we want to visi
              0.00
              # -----
              # Write your implementation here.
              word vectors = np.array([M reduced[word2Ind[w]] for w in words])
              plt.figure(figsize=(6,6))
              plt.scatter(word_vectors[:,0], word_vectors[:,1], edgecolors='k', c='r
              for word, (x, y) in zip(words, word_vectors):
                  plt.text(x+0.005, y+0.005, word)
         # -----
In [13]:
          # Run this sanity check
          # Note that this is not an exhaustive check for correctness.
          # The plot produced should look like the "test solution plot" depicted bel
          print ("-" * 80)
          print ("Outputted Plot:")
          M_{reduced_plot_test} = np.array([[1, 1], [-1, -1], [1, -1], [-1, 1], [0, 0])
          word2Ind_plot_test = {'test1': 0, 'test2': 1, 'test3': 2, 'test4': 3, 'test
          words = ['test1', 'test2', 'test3', 'test4', 'test5']
          plot_embeddings(M_reduced_plot_test, word2Ind_plot_test, words)
          print ("-" * 80)
```

Outputted Plot:



Test Plot Solution

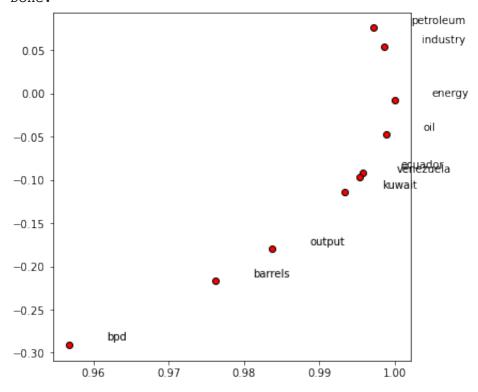


Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

Now we will put together all the parts you have written! We will compute the cooccurrence matrix with fixed window of 4 (the default window size), over the Reuters
"crude" (oil) corpus. Then we will use TruncatedSVD to compute 2-dimensional
embeddings of each word. TruncatedSVD returns U*S, so we need to normalize the
returned vectors, so that all the vectors will appear around the unit circle (therefore
closeness is directional closeness). **Note**: The line of code below that does the
normalizing uses the NumPy concept of *broadcasting*. If you don't know about
broadcasting, check out Computation on Arrays: Broadcasting by Jake VanderPlas.

Run the below cell to produce the plot. It'll probably take a few seconds to run. What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? **Note:** "bpd" stands for "barrels per day" and is a commonly used abbreviation in crude oil topic articles.

Running Truncated SVD over 8185 words... Done.



ANSWER

- * countries 'ecuador', 'kuwait' and 'venezuela' cluster together
- \ast 'petroleum' and 'industry' are quite nearby though not together with 'energy' and 'oil'
- * 'output', 'barrels' and 'bpd' do not cluster together (as one might have expected)

Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading GloVe's original paper.

Then run the following cells to load the GloVe vectors into memory. **Note**: If this is your first time to run these cells, i.e. download the embedding model, it will take about 15 minutes to run. If you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

Loaded vocab size 400000

Note: If you are receiving reset by peer error, rerun the cell to restart the download.

Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

1. Put 10000 Glove vectors into a matrix M

Note: This will take several minutes
----wv from bin = load embedding model()

2. Run reduce_to_k_dim (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```
def get_matrix_of_vectors(wv_from_bin, required_words=['barrels', 'bpd', 'e
In [17]:
             """ Put the GloVe vectors into a matrix M.
                Param:
                    wv from bin: KeyedVectors object; the 400000 GloVe vectors load
                Return:
                    M: numpy matrix shape (num words, 200) containing the vectors
                    word2Ind: dictionary mapping each word to its row number in M
             import random
             words = list(wv_from_bin.vocab.keys())
             print("Shuffling words ...")
             random.seed(224)
             random.shuffle(words)
             words = words[:10000]
             print("Putting %i words into word2Ind and matrix M..." % len(words))
             word2Ind = {}
             M = []
             curInd = 0
             for w in words:
                try:
                    M.append(wv_from_bin.word_vec(w))
                    word2Ind[w] = curInd
                    curInd += 1
                except KeyError:
                    continue
             for w in required_words:
                if w in words:
                    continue
                try:
                    M.append(wv_from_bin.word_vec(w))
                    word2Ind[w] = curInd
                    curInd += 1
                except KeyError:
                    continue
             M = np.stack(M)
             print("Done.")
             return M, word2Ind
         # -----
In [18]:
         # Run Cell to Reduce 200-Dimensional Word Embeddings to k Dimensions
         # Note: This should be quick to run
         # -----
         M, word2Ind = get matrix of vectors(wv from bin)
         M_reduced = reduce_to_k_dim(M, k=2)
         # Rescale (normalize) the rows to make them each of unit-length
         M_lengths = np.linalg.norm(M_reduced, axis=1)
```

M_reduced normalized = M_reduced / M_lengths[:, np.newaxis] # broadcasting

Putting 10000 words into word2Ind and matrix M...

Running Truncated SVD over 10010 words...

Shuffling words ...

Done.

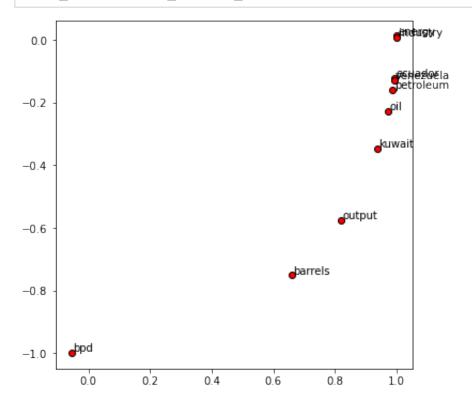
Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please follow the Piazza instructions, as how to run remotely on Stanford Farmshare machines.

Question 2.1: GloVe Plot Analysis [written] (4 points)

Run the cell below to plot the 2D GloVe embeddings for ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil', 'output', 'petroleum', 'venezuela'].

What clusters together in 2-dimensional embedding space? What doesn't cluster together that you might think should have? How is the plot different from the one generated earlier from the co-occurrence matrix? What is a possible reason for causing the difference?

```
In [19]: words = ['barrels', 'bpd', 'ecuador', 'energy', 'industry', 'kuwait', 'oil
    plot_embeddings(M_reduced_normalized, word2Ind, words)
```



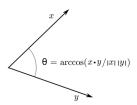
ANSWER

- * 'energy' and 'industry' clusters together and so does countries: 'ecuador', 'venezula'.
- * 'kuwait' however does not cluster together (as one would have been expected).
- * 'bpd', 'barrels' and 'output' also do not cluster together.
- * Compared to co-occurrence matrix, GloVe embeddings seem more 'indicative'/'decisive' related words are much closer, unrelated words are much farther. This could be because GloVe is more denser representation than co-occurrence matrix.

Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:



Instead of computing the actual angle, we can leave the similarity in terms of $similarity = cos(\Theta)$. Formally the Cosine Similarity s between two vectors p and q is defined as:

$$s = \frac{p \cdot q}{||p||||q||}, \text{ where } s \in [-1, 1]$$

Question 2.2: Words with Multiple Meanings (2 points) [code + written]

Polysemes and homonyms are words that have more than one meaning (see this wiki page to learn more about the difference between polysemes and homonyms). Find a word with at least 2 different meanings such that the top-10 most similar words (according to cosine similarity) contain related words from both meanings. For example, "leaves" has both "vanishes" and "stalks" in the top 10, and "scoop" has both "handed_waffle_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one. Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain one of the meanings of the words)?

Note: You should use the wv_from_bin.most_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance please check the **GenSim documentation**.

ANSWER

* 'sweet' has multiple meanings: it is a 'flavor', it can mean being 'lovely', it is a 'taste', it can also be a savory.

Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words (w1,w2,w3) where w1 and w2 are synonyms and w1 and w3 are antonyms, but Cosine Distance(w1,w3) < Cosine Distance(w1,w2). For example, w1="happy" is closer to w3="sad" than to w2="cheerful".

Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv_from_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the **GenSim** documentation for further assistance.

ANSWER

Out[72]: -0.03175687789916992

```
* w1='sweet', w2='savory', w3='spicy'.
* Possible explanation: 'sweet' and 'spicy' may have been
used in same context more often than 'sweet' and 'savory'
esp. since 'savory' is a rarer word.
```

Solving Analogies with Word Vectors

Word vectors have been shown to sometimes exhibit the ability to solve analogies.

As an example, for the analogy "man: king:: woman: x" (read: man is to king as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x. The most_similar function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list. The answer to the analogy will be the word ranked most similar (largest numerical value).

Note: Further Documentation on the most_similar function can be found within the **GenSim documentation**.

```
In [20]: # Run this cell to answer the analogy -- man : king :: woman : x
pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'king'], negative
```

```
[('queen', 0.6978678703308105),
  ('princess', 0.6081745028495789),
  ('monarch', 0.5889754891395569),
  ('throne', 0.5775108933448792),
  ('prince', 0.5750998258590698),
  ('elizabeth', 0.5463595986366272),
  ('daughter', 0.5399125814437866),
  ('kingdom', 0.5318052172660828),
  ('mother', 0.5168544054031372),
  ('crown', 0.5164473056793213)]
```

Question 2.4: Finding Analogies [code + written] (2 Points)

Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y :: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

Note: You may have to try many analogies to find one that works!

```
In [73]:
               # -----
               # Write your implementation here.
          pprint.pprint(wv from bin.most similar(positive=['india', 'bradman'], negat
          pprint.pprint(wv from bin.most similar(positive=['israel', 'muslim'], negat
               # -----
          [('tendulkar', 0.5084308981895447),
           ('rahul', 0.5017741918563843),
           ('ranjitsinhji', 0.4883757531642914),
           ('sub-continent', 0.4831077456474304),
           ('sachin', 0.4825434684753418),
           ('delhi', 0.47772687673568726),
           ('kumble', 0.47549352049827576),
           ('ganguly', 0.468065083026886), ('dravid', 0.4610215425491333),
           ('maharaja', 0.45348769426345825)]
          [('jewish', 0.7402099370956421),
           ('israeli', 0.6739732027053833),
           ('israelis', 0.6715682744979858),
           ('palestinian', 0.6709890365600586), ('palestinians', 0.6703073978424072),
           ('jerusalem', 0.6596884727478027),
           ('jews', 0.6331148147583008),
           ('arab', 0.6251180171966553),
           ('arabs', 0.5814354419708252),
           ('muslims', 0.5775227546691895)]
```

ANSWER

```
* Analogy:- "australia": "bradman":: "india": "tendulkar"

* This analogy holds since "Don Bradman" is generally
regarded as the best cricket batsman of Austrlia and
similarly "Sachin Tendulkar" is generally regarded as the
best cricket batsman of India.
```

Question 2.5: Incorrect Analogy [code + written] (1 point)

Find an example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the (incorrect) value of b according to the word vectors.

ANSWER

```
* Expected Analogy:- "australia" : "kangaroo" :: "india" :
("elephant" | "tiger")
* Actual Result:- "australia" : "kangaroo" :: "india":
"kashmir"
```

Question 2.6: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "worker" and most dissimilar to "man", and (b) which terms are most similar to "man" and "worker" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
In [21]: # Run this cell
# Here `positive` indicates the list of words to be similar to and `negativ
# most dissimilar from.
pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'worker'], negative
print()
pprint.pprint(wv_from_bin.most_similar(positive=['man', 'worker'], negative
```

```
[('employee', 0.6375863552093506),
 ('workers', 0.6068919897079468),
('nurse', 0.5837947130203247),
('pregnant', 0.5363885760307312),
('mother', 0.5321309566497803),
('employer', 0.5127025842666626),
('teacher', 0.5099577307701111),
('child', 0.5096741914749146),
('homemaker', 0.5019455552101135),
('nurses', 0.4970571994781494)]
[('workers', 0.611325740814209),
('employee', 0.5983108878135681),
('working', 0.5615329742431641),
('laborer', 0.5442320108413696),
('unemployed', 0.5368517637252808),
('job', 0.5278826951980591),
('work', 0.5223963260650635),
('mechanic', 0.5088937282562256),
('worked', 0.5054520964622498),
('factory', 0.4940453767776489)]
```

ANSWER

```
* "woman" associated occupation roles are reinforcing role
biases like "nurse", "homemaker", "mother"
* "man" associated occupation roles are reinforcing role
biases like "laborer", "mechanic"
```

Question 2.7: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the most_similar function to find another case where some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
In [45]: # ------
# Write your implementation here.

pprint.pprint(wv_from_bin.most_similar(positive=['african', 'worker'], negaprint()
    pprint.pprint(wv_from_bin.most_similar(positive=['american', 'worker'], negaprint()
    pprint.pprint(wv_from_bin.most_similar(positive=['american', 'worker'], negaprint()
```

```
[('workers', 0.5144128799438477),
('mozambique', 0.5087184906005859),
('zimbabwe', 0.5028067231178284),
('zambia', 0.4929963946342468),
('migrant', 0.48975875973701477),
('africa', 0.4858377277851105),
('laborer', 0.47043585777282715),
('johannesburg', 0.4502374529838562),
('unemployed', 0.4486370086669922),
('mbeki', 0.44758090376853943)]
[('employee', 0.6299172639846802),
('workers', 0.5489532947540283),
('contractor', 0.5050545334815979),
('working', 0.5027685165405273),
('worked', 0.4873591661453247),
('employees', 0.48215365409851074),
('u.s.', 0.4752364754676819),
('employer', 0.47171080112457275),
('mechanic', 0.470342218875885),
('citizen', 0.46596723794937134)]
```

ANSWER

```
* "african" worker related terms are reinforcing negative
biases like "migrant", "unemployed", "laborer"
* "american" worker related terms are reinforcing biases like
"employee", "employer", "mechanic", "contractor"
```

Question 2.8: Thinking About Bias [written] (2 points)

What might be the causes of these biases in the word vectors? You should give least 2 explainations how bias get into the word vectors. How might you be able to investigate/test these causes?

ANSWER

* These biases are caused by underlying biases/stereotypes captured in the text over which word vectors have been trained. Since word vectors captures semantic correlation, the underlying semantic biases/stereotypes also gets captured. To be able to investigate/test these causes, we can enlist various known biases/stereotypes and do like above — by running most_similar method on the two different vectors (biased and unbiased) and the reverse and checking if they result in demonstrating biases/stereotypes.

Submission Instructions

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTex", you can also save the webpage as pdf. Make sure all your solutions especially the coding parts are displayed in the pdf, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 6. Submit your PDF on Gradescope.

| In []: |]: |
|---------|----|
| In []: |]: |