

SeismicAirgun User Guide

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I. INTRODUCTION

SeismicAirgun computes airgun/bubble dynamics following a similar treatment to the seminal work of Ziolkowski (1970). A lumped parameter model is used where the internal properties of the airgun and bubbles are assumed to be spatially uniform. **SeismicAirgun** is written in MATLAB and runs efficiently on a standard desktop/laptop computer. For more details and examples of the application of **SeismicAirgun** see:

- Chelminski, S., Watson, L. M., and Ronen, S. (2019) Low-frequency pneumatic seismic sources, *Geophysical Prospecting*, <https://doi.org/10.1111/1365-2478.12774>.
- Watson, L. M., Jennings, J., and Ronen, S. (2017) Source designature of ocean-bottom node data using deterministic airgun modeling, *SEG Technical Program Expanded Abstracts 2017*, 121-126, <https://doi.org/10.1190/segam2017-17750879.1>.
- Watson, L. M., Dunham, E. M., and Ronen, S. (2016) Numerical modeling of seismic airguns and low-pressure sources, *SEG Technical Program Expanded Abstracts*, <https://doi.org/10.1190/segam2016-13846118.1>.

II. DIRECTORY

- **source** - function files associated with numerical implementation.
- **doc** - documentation including user guide and license file.
- **references** - publications that are associated with this code.

SeismicAirgun is freely available online at <https://github.com/leighton-watson/SeismicAirgun> and is distributed under the MIT license (see `license.txt` for details).

III. MODEL DESCRIPTION

Here, I describe the mathematical model of **SeismicAirgun**, which is a lumped parameter model where the internal properties of the airgun and bubble are assumed to be spatially uniform. The model can be divided into three components; i.) bubble, ii.) airgun, and iii.) acoustic radiation. For more details see Chelminski et al. (2019) and Watson et al. (2016) and the references therein.

i. Bubble

The motion of the bubble wall is governed by the modified Herring equation (Herring, 1941; Cole, 1948; Vokurka, 1986):

$$R\ddot{R} + \frac{3}{2}\dot{R}^2 = \frac{p_b - p_\infty}{\rho_\infty} + \frac{R}{\rho_\infty c_\infty} \dot{p}_b - \alpha \dot{R}, \quad (1)$$

where R , $\dot{R} = dR/dt$, and $\ddot{R} = d^2R/dt^2$ are the radius, velocity, and acceleration of the bubble wall, respectively, p_b is the pressure inside the bubble, $\dot{p}_b = dp_b/dt$, and p_∞ , ρ_∞ and c_∞ are the pressure, density, and speed of sound, respectively, in the water infinitely far from the bubble. The ambient pressure at the depth of the airgun, z , is given by $p_\infty = p_{\text{atm}} = \rho_\infty g z$, where p_{atm} is the atmospheric pressure and g is the gravitational acceleration. Mechanical energy dissipation mechanisms, which are challenging to model directly, are parameterized into an extra damping term of the form of $\alpha \dot{R}$, where α is an empirically determined constant Langhammer and Landrø (1996); Watson et al. (2017).

The bubble is initialized with a finite initial volume equal to the volume of the airgun. This is because the modified Herring equation (equation 1) becomes singular when $R \rightarrow 0$. The bubble wall velocity is initially zero and the bubble air is at the same temperature and pressure as the ambient water. The mass can then be calculated from equation 8. For more discussion on the bubble initial conditions see Watson et al. (2019).

Mass is ejected from the airgun into the water forming a bubble if three conditions are met:

1. $t < t_{\text{fire}}$. This parameter can be used to imposed a finite discharge duration.
2. $p_a(t) > p_b(t)$. The airgun only discharges if the pressure inside the source is larger than the pressure outside.
3. $m_a(t) > F m_{a0}$ where $m_a(t)$ is the mass in the airgun, $F \in [0, 1]$ is a tunable parameter that controls the fraction of mass ejected from the airgun, and m_{a0} is the initial mass in the airgun.

Mass flow from the airgun to the bubble is given by:

$$\frac{dm_b}{dt} = \begin{cases} p_a A \left(\frac{\gamma}{Q T_a} \right)^{1/2} \left(\frac{2}{\gamma-1} \right)^{1/2} \left[\left(\frac{p_a}{p_b} \right)^{(\gamma-1)/\gamma} - 1 \right] & \text{if flow is unchoked} \\ p_a A \left(\frac{\gamma}{Q T_a} \right)^{1/2} & \text{if flow is choked} \end{cases} \quad (2)$$

where m_b is the mass of the bubble, A is the airgun port area, Q is the specific gas constant, and p_a and T_a are the airgun pressure and temperature, respectively. Flow through the port is choked (choked flow is when the flow through a nozzle has a velocity equal to the sound speed, the maximum possible velocity for fluid flow through a nozzle) if (Babu, 2014)

$$\frac{p_a}{p_b} \geq \left(\frac{\gamma+1}{2} \right)^{\gamma/(\gamma-1)}, \quad (3)$$

where γ is the ratio of heat capacities. If the pressure ratio is less than this critical value then flow through the port will be unchoked.

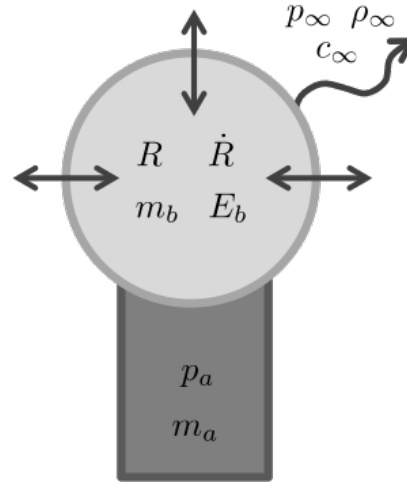
The internal energy of the bubble, E_b , changes according to the first law of thermodynamics for an open system:

$$\frac{dE_b}{dt} = c_p T_a \frac{dm_b}{dt} - 4\pi M \kappa R^2 (T_b - T_\infty) - p_b \frac{dV_b}{dt}, \quad (4)$$

where c_p is the heat capacity at constant volume, κ is the heat transfer coefficient, M is a constant that accounts for the increased effective surface area over which heat transfer can occur as a result of turbulence at the bubble walls (Laws et al., 1990), and $V_b = (4/3)\pi R^3$ is the volume of the bubble, which is assumed to be spherical.

The bubble of air is less dense than the surrounding water and hence moves buoyantly upwards in the water column. The vertical velocity of the bubble is given by Herring (1941); Taylor (1942);

Figure 1: Model schematic. The airgun and bubble are treated as lumped parameter objects. The internal properties are assumed to be spatially uniform and described by a single value that evolves in time.



Langhammer and Landrø (1996)

$$\frac{dz(t)}{dt} = \frac{-2g\beta}{R(t)^3} \int_0^t R(\tau)^3 d\tau, \quad (5)$$

where β is a tunable parameter.

ii. Airgun

The airgun and bubble are coupled by conservation of mass:

$$\frac{dm_a}{dt} = -\frac{dm_b}{dt}, \quad (6)$$

where m_a is the mass of air inside the airgun, and conservation of energy:

$$\frac{dE_a}{dt} = -c_p T_a \frac{dm_b}{dt}, \quad (7)$$

where E_a is the internal energy of the airgun.

The airgun and bubble governing equations are closed with the ideal gas equation of state:

$$p = \frac{mQT}{V}, \quad (8)$$

and the relationship between the internal energy and temperature:

$$E = c_v mT, \quad (9)$$

where c_v is the heat capacity at constant volume.

iii. Acoustic Radiation

The pressure perturbation in the water is related to the bubble dynamics by (Keller and Kolodner, 1956)

$$\Delta p(r, t) = \rho_\infty \left[\frac{\ddot{V}(t - r/c_\infty)}{4\pi r} - \frac{\dot{V}(t - r/c_\infty)^2}{32\pi^2 r^4} \right], \quad (10)$$

where Δp is the pressure perturbation in the water, r is the distance from the center of the bubble to the receiver, and V is the volume of the bubble. The second term on the right side is a near-field term that decays rapidly with distance. In addition to the direct arrival there is a ghost arrival, which is the initially upgoing wave that is reflected with negative polarity from the sea surface. For a receiver directly below the source the observed pressure perturbation is

$$\Delta p_{\text{obs}}(r, t) = \Delta p_D(r, t) - \Delta p_G(r + 2D, t), \quad (11)$$

where Δp_D is the direct signal and Δp_G is the ghost arrival, which is assumed to have -1 reflection coefficient from the sea surface. D is the depth of the seismic airgun (Figure 2).

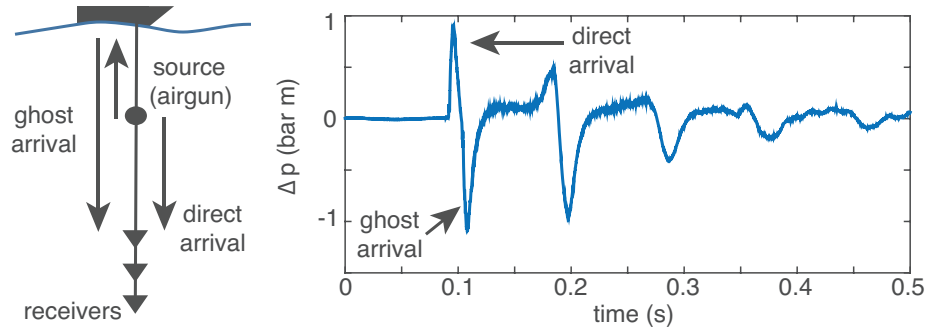


Figure 2: Schematic showing direct and ghost arrivals along with example source signature from Watson et al. (2016).

IV. NUMERICAL IMPLEMENTATION

SeismicAirgun solves a system of eight ordinary differential equations using MATLAB's built-in solver, `ode45`, which is explicit Runge-Kutta (4,5) method. The variables that are evolved are (1) R , bubble radius, (2) \dot{R} , bubble wall velocity, (3) m_b , the mass of bubble, (4) T_b , temperature of bubble, (5) p_a , pressure inside the airgun, (6) m_a , mass of air inside the airgun, (7) z , depth of the bubble, and (8) the integrand in equation 5.

V. USING SeismicAirgun

Several example script files are include that demonstrate how to specific source properties, run the code, save and display the outputs, and compare the simulation results to *Nucleus* signatures. The three example script files provided are:

- `example_main.m`: shows how to specify source properties, run the code, display basic outputs, and save the simulation result.
- `example_dispOutputs.m`: demonstrates how to plot other outputs from the simulation.
- `example_compareNucleus.m`: compares the simulation results with *Nucleus* data (contained in `nuc.csv` and `nucProperties.csv`).

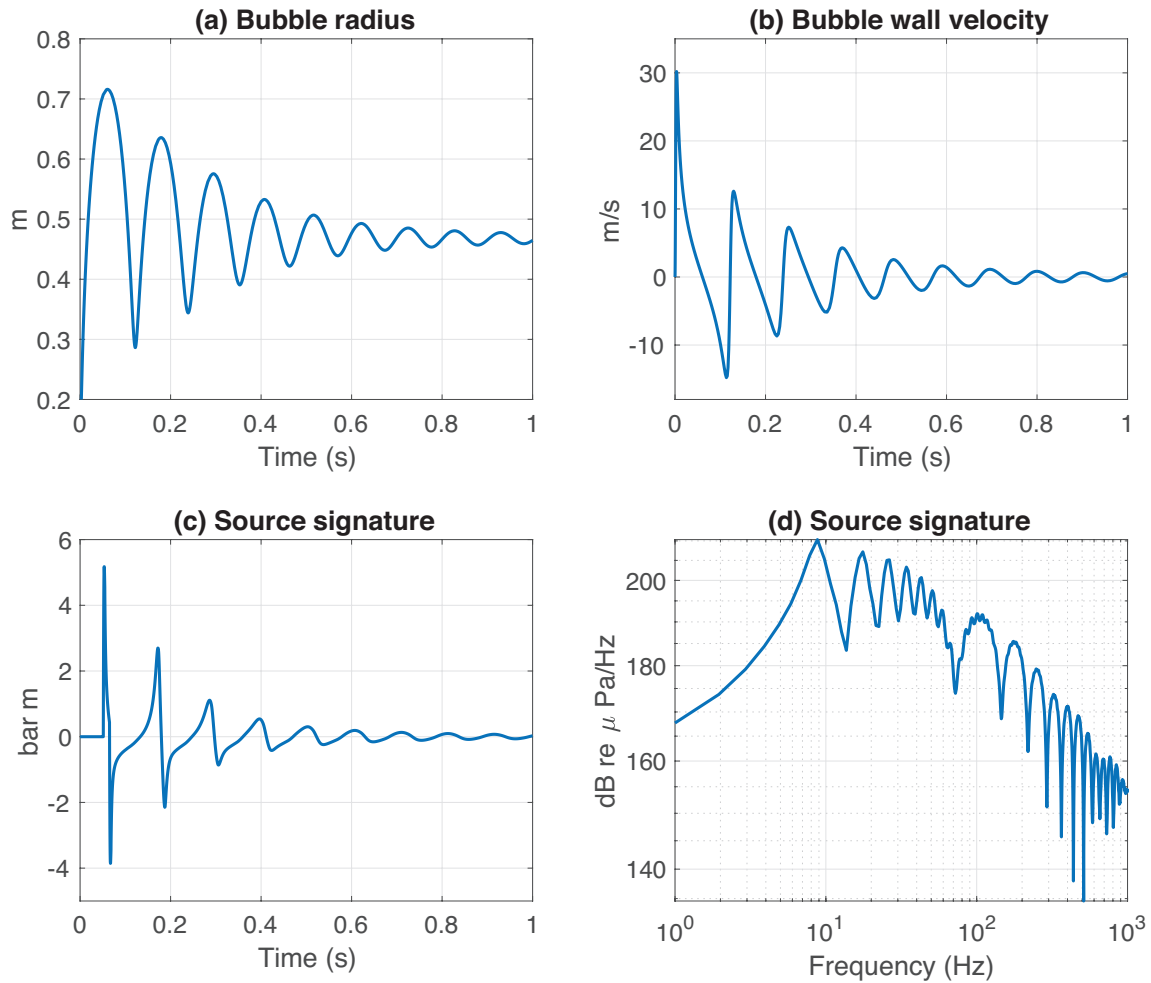


Figure 3: Example model outputs for a 1000 in³ airgun pressurized to 1600 psi with a port area of 16 in² fired at a depth of 10 m showing (a) bubble radius, (b) bubble wall velocity, and source signature (acoustic pressure perturbation in the water) in the (c) time and (d) frequency domains. The source signature in the time domain is displayed in bar m, which enables comparison between observations at different source-receiver distances.

i. `example_main.m`

The source contained is contained in the directory `source`. Therefore, the first thing to do is to point to this directory:

```
addpath source/
```

The source firing properties are specified:

```
% Source Firing Configuration
src_pressure = 1000; % source pressure [psi]
src_volume = 10000; % source volume [in^3]
src_area = 80; % port area of source [in^2]
src_depth = 10; % depth of source [m]
% pressure (psi), volume (in^3), port/throat area (in^2)
src_props = [src_pressure, src_volume, src_area];
```

Logical flags are used to determine if the user wants to direct arrival (no ghost) to be plotted (in time and frequency domains) and saved (in ascii and binary formats).

```
% save direct arrival
save_outputs = false; % false = do not save outputs, true = save outputs
% plot direct arrival
plot_outputs = false; % false = do not plot outputs, true = plot outputs
```

There are several physical (distance from source to receiver, total simulation time, sampling interval) and tuning parameters (α in equation 1 and β in equation 5) that need to be specified. Parameters are saved to the structure `physConst` using the function file `physical_constants`. The mass fraction ejected from the airgun, F , is directly specified in `physical_constants`.

```
% Physical and Tuning Parameters
r = 100; % distance from source to receiver.
time = [0 2]; % time [s]
alpha = 0.8; % tuning parameter - decay of amplitude of pressure perturbation
beta = 0; % tuning parameter - rate of ascent of bubble
physConst = physical_constants(src_depth, r, time, alpha, beta); % physical constant
dt = 1.25e-5; % sampling interval
```

The solver is run by calling `SeismicAirgun`:

```
output = SeismicAirgun(src_props, physConst, dt, plot_outputs);
```

Outputs can be saved in a variety of formats: ascii, binary and (work in progress) SEG-Y.

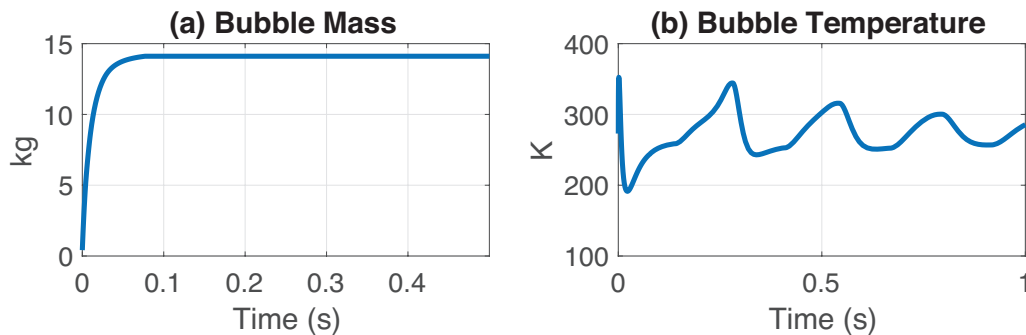


Figure 4: Example model outputs for a 10,000 in³ airgun pressurized to 1000 psi with a port area of 80 in² fired at a depth of 10 m showing (a) bubble mass and (b) temperature.

ii. `example_dispOutputs.m`

This script file is very similar to `example_main.m` with the addition of demonstrating how to plot additional outputs, such as mass and temperature of the bubble (Figure 4).

iii. `example_compareNucleus.m`

Nucleus is a commercial airgun modeling software produced by PGS. The **SeismicAirgun** git repository contains 65 example *Nucleus* signatures (containing just the direct arrival). The source properties (pressure and volume) are contained in `nucProperties.csv` while the time series data is contained in `nuc.csv`.

`example_compareNucleus.m` compares the simulated signatures using **SeismicAirgun** with the *Nucleus* signatures. A similar comparison is presented in Watson et al. (2017). The source pressure and volume are selected to match the *Nucleus* values:

```
src_pressure = nucProp(i,1); % source pressure [psi]
src_volume = nucProp(i,2); % source volume [in^3]
```

The other parameter values are the port area (16 in²), source depth (10 m), and the tuning parameters α (0.8), β , (1), and F (0.05). **SeismicAirgun** is able to provide a good match to *Nucleus*, as shown in Figure 5.

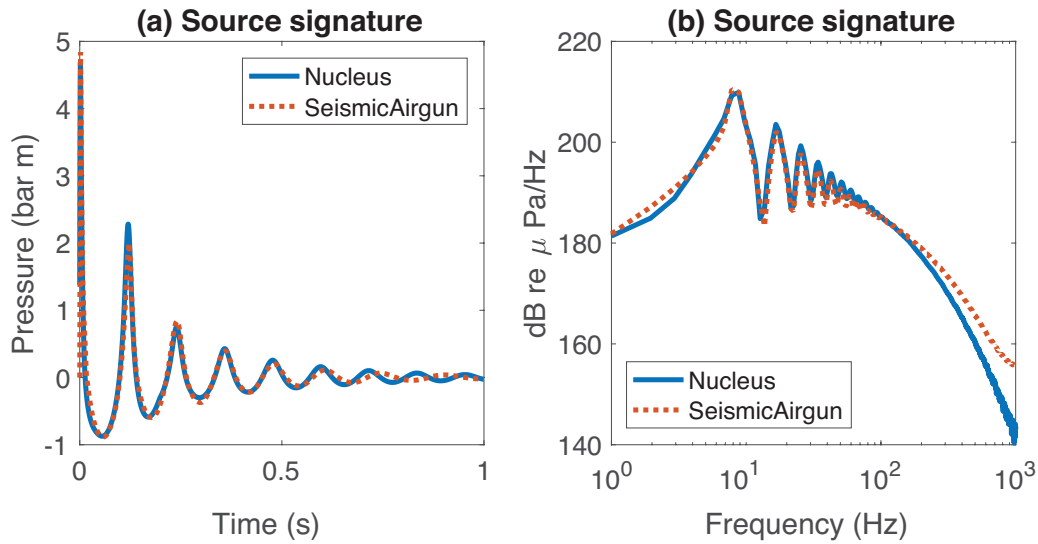


Figure 5: Example model outputs for a 400 in³ airgun pressurized to 2000 psi.

Note that **SeismicAirgun** is limited to a single source and cannot rigorously account for the complex interactions between bubbles generated by multiple sources in close proximity.

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