

Iteration - 1.

x_i y_i
7.6 157

7.1 174

Sample - 1

step 1: [7.6, 157] $\eta = 0.01$, $m = 1$, $c = -1$

$$\begin{aligned} 2: \quad \frac{\partial E}{\partial m} \Big|_{m=1} &= -(y_i^a - m x_i^a - c) (-x_i^a) \\ &= (157 - 7.6 - (-1)) (7.6) \\ &= (150.4) (7.6) \\ &= 1143.04. \end{aligned}$$

$$\begin{aligned} \frac{\partial E}{\partial c} \Big|_{c=-1} &= -(y_i^a - m x_i^a - c) \\ &= -(157 - (1) (7.6) - (-1)) \\ &= -(158 - 7.6) \\ &= -150.4 \end{aligned}$$

$$\text{step 3: } \Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01) (1143.04) = -11.430$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = -(0.01) (-150.4) = 1.504.$$

$$\text{step 4: } m = m + \Delta m = 1 + (-11.43) = -10.43$$

$$c = c + \Delta c = -1 + (1.504) = 0.504.$$

Iteration - 2

$$S_1: [7.6, 157], \eta = 0.01, m = -10.43, c = 0.504$$

$$S_2: \left. \frac{\partial E}{\partial m} \right|_{m=-10.43} = (157 - (-10.43)(7.61) - 0.504)(7.61)$$

$$= (157 + (10.43)(7.61) - 0.504)(7.61)$$

$$= (156.496 + 79.372)(7.61)$$

$$= 1794.955$$

$$\left. \frac{\partial E}{\partial c} \right|_{c=0.504} = -(157 - (-10.43)(7.61) - 0.504)$$

$$= -235.868$$

$$S_3: \Delta m = -\eta \frac{\partial E}{\partial c} = (-0.01 \times 1794.955) = -17.949$$

$$\Delta c = -\eta \frac{\partial E}{\partial c} = (-0.01)(-235.868)$$

$$= 2.358$$

$$S_4: m = m + \Delta m = -10.43 + (-17.943)$$

$$= -28.379$$

$$c = c + \Delta c = 0.504 + 2.358$$

$$= 2.862$$

Sample - 2

Iteration - 1

$$S_1: (7.1, 174) \quad \eta = 0.01, m = 1, c = -1$$

$$S_2: \left. \frac{\partial E}{\partial m} \right|_{m=1} = -(y_i^a - mx_i^a - c) - x_i^a$$

$$= (174 - (7.1) - (-1)) + 7.1$$

$$= (175 - 7.1)(7.1)$$

$$\begin{aligned}\frac{\partial E}{\partial c} \Big|_{c=1} &= -(y_i^a - mx_i^a - c) \\ &= -(174 - (7.1) - (-1)) \\ &= -167.9\end{aligned}$$

$$S_3: \Delta m = -\eta \frac{\partial E}{\partial m} = -(0.01) 1192.09 = -11.920$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} = -(0.01) (-167.9) \\ &= 1.679\end{aligned}$$

$$S_4: m = m + \Delta m = 1 + (-11.920) = -10.920$$

$$c = c + \Delta c = -1 + 1.679 = 0.679$$

Iteration - 2

$$S_1: [7.1, 174] \quad \eta = 0.01 \quad m = -10.92$$

$$c = 0.67$$

$$\begin{aligned}S_2: \frac{\partial E}{\partial m} \Big|_{m=-10.92} &= (174 - (-10.92)(7.1) - \\ &\quad 0.67(7.1)) \\ &= (173.3217 - (10.92 + 7.1)(7.3)) \\ &= 1781.056\end{aligned}$$

$$\begin{aligned}\frac{\partial E}{\partial c} \Big|_c &= 0.679 = -(174 - (-10.92)(7.1) \\ &\quad - 0.679)\end{aligned}$$

$$= -250.853$$

S₃ :

$$\Delta m = -\eta \frac{\partial E}{\partial m} = (-0.01) \times (1781.056)$$
$$= -17.810$$

$$\Delta C = -\eta \frac{\partial E}{\partial C} = -(-0.01) (-250.853)$$
$$= 2.508$$

S₄ :

$$m = m + \Delta m = -10.92 - 17.81$$
$$= -28.73$$

$$C = C + \Delta C$$

$$= 0.679 + 2.508$$

$$= 3.187.$$