

✓ Data Project - Stock Market Analysis



Time Series data is a series of data points indexed in time order. Time series data is everywhere, so manipulating them is important for any data analyst or data scientist.

In this notebook, we will discover and explore data from the stock market, particularly some technology stocks (Apple, Amazon, Google, and Microsoft). We will learn how to use yfinance to get stock information, and visualize different aspects of it using Seaborn and Matplotlib. We will look at a few ways of analyzing the risk of a stock, based on its previous performance history. We will also be predicting future stock prices through a Long Short Term Memory (LSTM) method!

We'll be answering the following questions along the way:

- 1.) What was the change in price of the stock over time?
- 2.) What was the daily return of the stock on average?
- 3.) What was the moving average of the various stocks?
- 4.) What was the correlation between different stocks'?
- 5.) How much value do we put at risk by investing in a particular stock?
- 6.) How can we attempt to predict future stock behavior? (Predicting the closing price stock price of

✓ 1. What was the change in price of the stock overtime?

In this section we'll go over how to handle requesting stock information with pandas, and how to analyze basic attributes of a stock.

```
!pip install yfinance
```

```

Requirement already satisfied: yfinance in /usr/local/lib/python3.10/dist-packages (0.2.
Requirement already satisfied: pandas>=1.3.0 in /usr/local/lib/python3.10/dist-packages
Requirement already satisfied: numpy>=1.16.5 in /usr/local/lib/python3.10/dist-packages
Requirement already satisfied: requests>=2.31 in /usr/local/lib/python3.10/dist-packages
Requirement already satisfied: multitasking>=0.0.7 in /usr/local/lib/python3.10/dist-pac
Requirement already satisfied: lxml>=4.9.1 in /usr/local/lib/python3.10/dist-packages (f
Requirement already satisfied: platformdirs>=2.0.0 in /usr/local/lib/python3.10/dist-pac
Requirement already satisfied: pytz>=2022.5 in /usr/local/lib/python3.10/dist-packages (
Requirement already satisfied: frozendict>=2.3.4 in /usr/local/lib/python3.10/dist-packa
Requirement already satisfied: peewee>=3.16.2 in /usr/local/lib/python3.10/dist-packages

```

```
Requirement already satisfied: beautifulsoup4>=4.11.1 in /usr/local/lib/python3.10/dist-  
Requirement already satisfied: html5lib>=1.1 in /usr/local/lib/python3.10/dist-packages  
Requirement already satisfied: soupsieve>1.2 in /usr/local/lib/python3.10/dist-packages  
Requirement already satisfied: six>=1.9 in /usr/local/lib/python3.10/dist-packages (from  
Requirement already satisfied: webencodings in /usr/local/lib/python3.10/dist-packages (  
Requirement already satisfied: python-dateutil>=2.8.2 in /usr/local/lib/python3.10/dist-  
Requirement already satisfied: tzdata>=2022.1 in /usr/local/lib/python3.10/dist-packages  
Requirement already satisfied: charset-normalizer<4,>=2 in /usr/local/lib/python3.10/dis  
Requirement already satisfied: idna<4,>=2.5 in /usr/local/lib/python3.10/dist-packages (  
Requirement already satisfied: urllib3<3,>=1.21.1 in /usr/local/lib/python3.10/dist-pack  
Requirement already satisfied: certifi>=2017.4.17 in /usr/local/lib/python3.10/dist-pack
```

```
import pandas as pd
import numpy as np

import matplotlib.pyplot as plt
import seaborn as sns
sns.set_style('whitegrid')
plt.style.use("fivethirtyeight")
%matplotlib inline

# For reading stock data from yahoo
from pandas_datareader.data import DataReader
import yfinance as yf
from pandas_datareader import data as pdr

yf.pdr_override()

# For time stamps
from datetime import datetime

# The tech stocks we'll use for this analysis
tech_list = ['AAPL', 'GOOG', 'MSFT', 'AMZN']

# Set up End and Start times for data grab
tech_list = ['AAPL', 'GOOG', 'MSFT', 'AMZN']

end = datetime.now()
start = datetime(end.year - 1, end.month, end.day)

for stock in tech_list:
    globals()[stock] = yf.download(stock, start, end)

company_list = [AAPL, GOOG, MSFT, AMZN]
company_name = ["APPLE", "GOOGLE", "MICROSOFT", "AMAZON"]

for company, com_name in zip(company_list, company_name):
    company["company_name"] = com_name

df = pd.concat(company_list, axis=0)
df.tail(10)
```

```

yfinance: pandas_datareader support is deprecated & semi-broken so will be removed in a
[*****100%*****] 1 of 1 completed
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[*****100%*****] 1 of 1 completed
[*****100%*****] 1 of 1 completed

```

	Open	High	Low	Close	Adj Close	Volume	company_name
Date							
2024-05-28	179.929993	182.240005	179.490005	182.149994	182.149994	29927000	AMAZON
2024-05-29	181.699997	184.080002	181.550003	182.020004	182.020004	32009300	AMAZON
2024-05-30	181.309998	181.339996	178.360001	179.320007	179.320007	29249200	AMAZON
2024-05-31	178.300003	179.210007	173.869995	176.440002	176.440002	58903900	AMAZON
2024-06-03	177.699997	178.699997	175.919998	178.339996	178.339996	30786600	AMAZON
2024-06-04	177.639999	179.820007	176.440002	179.339996	179.339996	27198400	AMAZON

Import Libraries: Import necessary libraries. Set Styles: Set styles for plotting. Read Stock Data: Set up the stock symbols and download their data from Yahoo Finance. Add Company Names: Add a column to each DataFrame indicating the company name. Concatenate Data: Combine all individual DataFrames into one.

Quick note: Using `globals()` is a sloppy way of setting the DataFrame names, but it's simple. Now we have our data, let's perform some basic data analysis and check our data.

✓ Descriptive Statistics about the Data

`.describe()` generates descriptive statistics. Descriptive statistics include those that summarize the central tendency, dispersion, and shape of a dataset's distribution, excluding NaN values.

Analyzes both numeric and object series, as well as DataFrame column sets of mixed data types. The output will vary depending on what is provided. Refer to the notes below for more detail.

```
# Summary Stats
AAPL.describe()
```



	Open	High	Low	Close	Adj Close	Volume
count	251.000000	251.000000	251.000000	251.000000	251.000000	2.510000e+02
mean	182.746534	184.211999	181.367410	182.821753	182.296098	5.750452e+07
std	8.738375	8.552274	8.749900	8.690825	8.641298	1.844647e+07
min	165.350006	166.399994	164.080002	165.000000	164.776505	1.421504e+07
25%	175.244995	177.025002	173.660004	175.280006	174.800789	4.657160e+07
50%	183.419998	184.899994	181.809998	183.630005	182.988205	5.302030e+07
75%	190.239998	191.540001	189.189995	190.139999	189.854996	6.438910e+07
max	198.020004	199.619995	197.000000	198.110001	197.589523	1.632241e+08



We have only 255 records in one year because weekends are not included in the data.

✓ Information About the Data

.info() method prints information about a DataFrame including the index dtype and columns, non-null values, and memory usage.

```
# General info
AAPL.info()
```



```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 251 entries, 2023-06-12 to 2024-06-10
Data columns (total 7 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Open            251 non-null   float64
1   High            251 non-null   float64
2   Low             251 non-null   float64
3   Close           251 non-null   float64
4   Adj Close       251 non-null   float64
5   Volume          251 non-null   int64
6   company_name    251 non-null   object
dtypes: float64(5), int64(1), object(1)
memory usage: 15.7+ KB
```

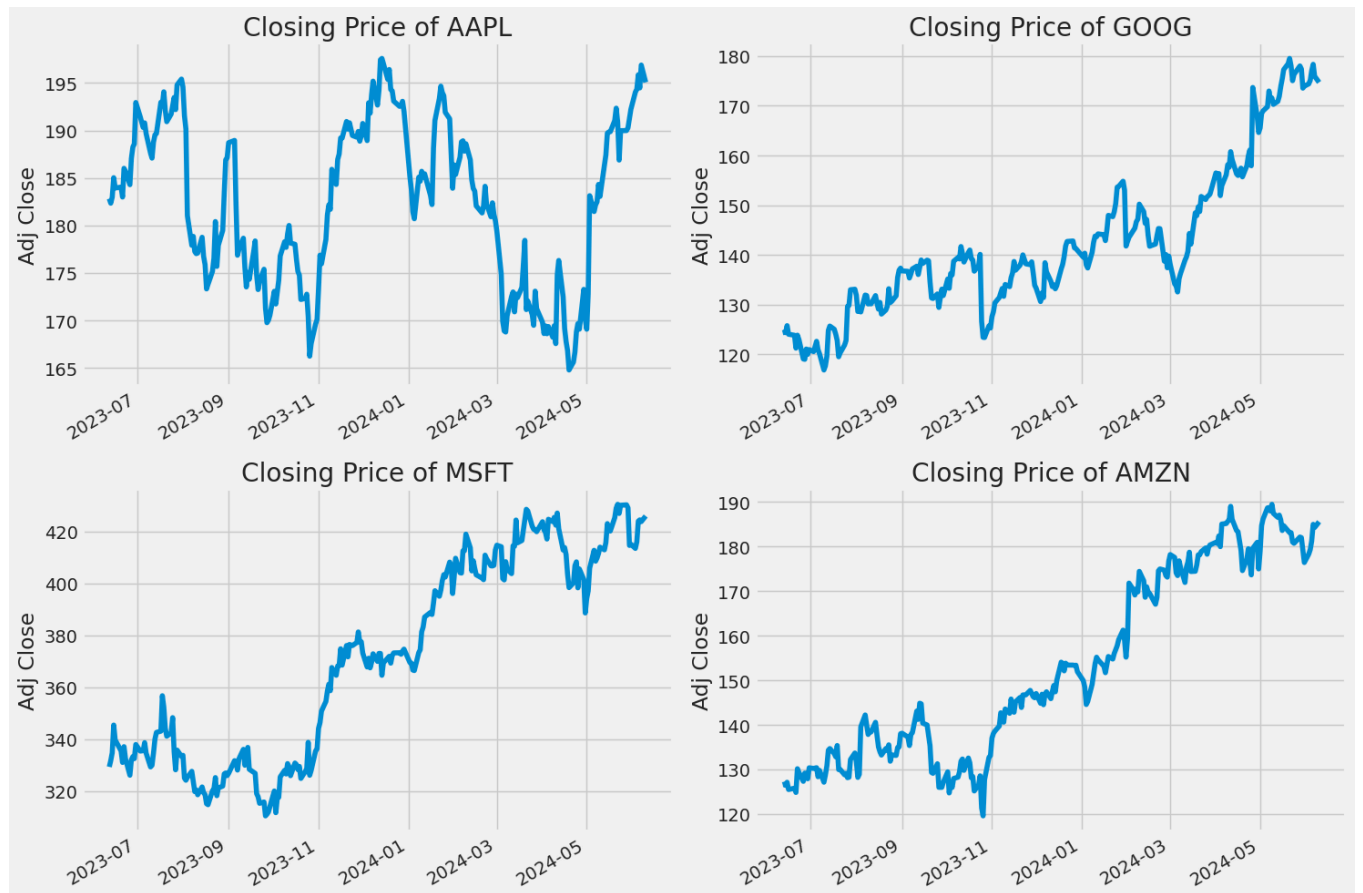
✓ Closing Price

The closing price is the last price at which the stock is traded during the regular trading day. A stock's closing price is the standard benchmark used by investors to track its performance over time.

```
# Let's see a historical view of the closing price
plt.figure(figsize=(15, 10))
plt.subplots_adjust(top=1.25, bottom=1.2)

for i, company in enumerate(company_list, 1):
    plt.subplot(2, 2, i)
    company['Adj Close'].plot()
    plt.ylabel('Adj Close')
    plt.xlabel(None)
    plt.title(f"Closing Price of {tech_list[i - 1]}")

plt.tight_layout()
```



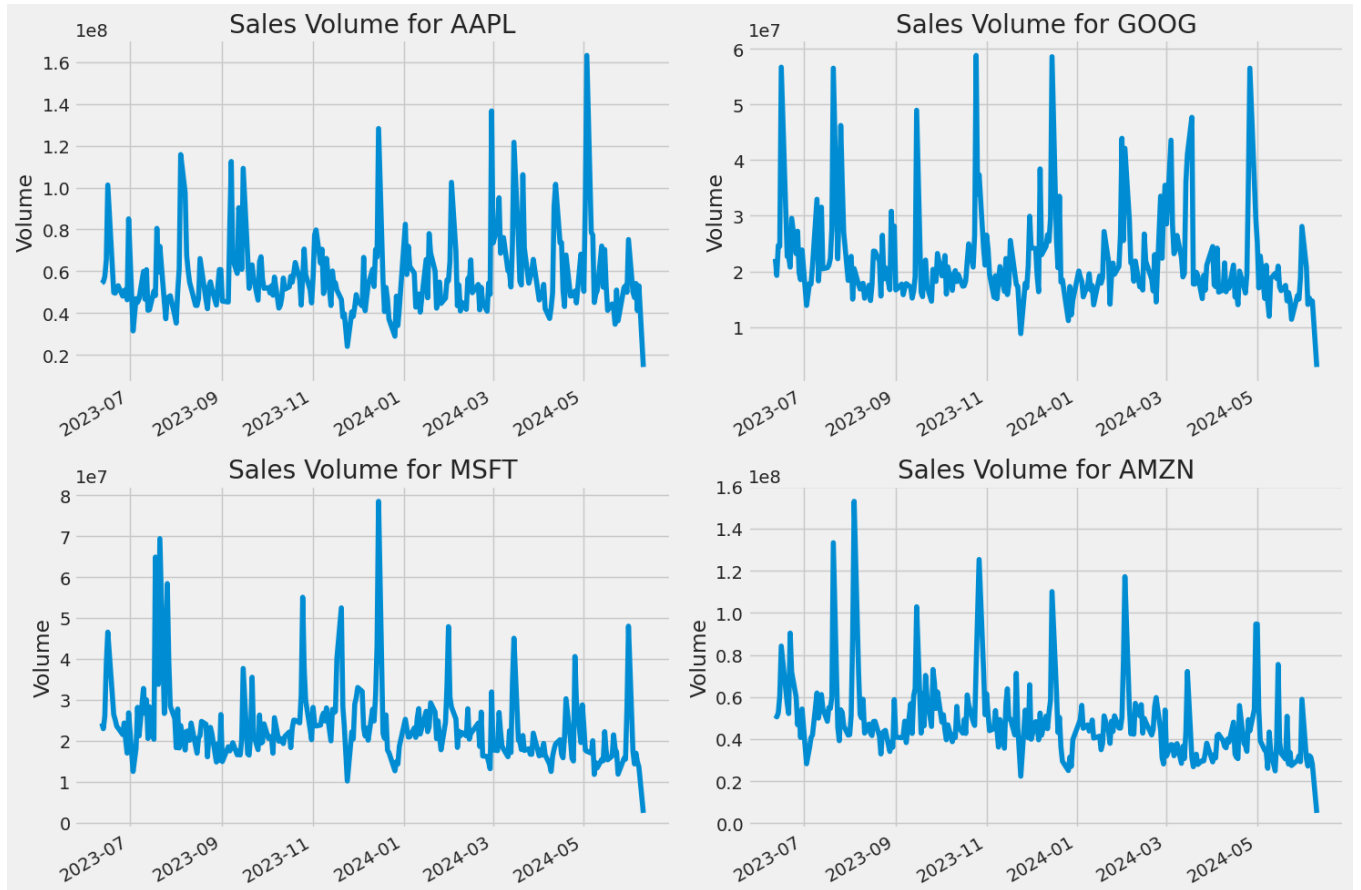
✓ Volume of Sales

Volume is the amount of an asset or security that changes hands over some period of time, often over the course of a day. For instance, the stock trading volume would refer to the number of shares of security traded between its daily open and close. Trading volume, and changes to volume over the course of time, are important inputs for technical traders.

```
# Now let's plot the total volume of stock being traded each day
plt.figure(figsize=(15, 10))
plt.subplots_adjust(top=1.25, bottom=1.2)

for i, company in enumerate(company_list, 1):
    plt.subplot(2, 2, i)
    company['Volume'].plot()
    plt.ylabel('Volume')
    plt.xlabel(None)
    plt.title(f"Sales Volume for {tech_list[i - 1]}")

plt.tight_layout()
```

Now that we've seen the visualizations for the closing price and the volume traded each day, let's go ahead and calculate the moving average for the stock.

✓ 2. What was the moving average of the various stocks?

The moving average (MA) is a simple technical analysis tool that smooths out price data by creating a constantly updated average price. The average is taken over a specific period of time, like 10 days, 20 minutes, 30 weeks, or any time period the trader chooses.

```
ma_day = [10, 20, 50]

for ma in ma_day:
    for company in company_list:
        column_name = f"MA for {ma} days"
        company[column_name] = company['Adj Close'].rolling(ma).mean()

fig, axes = plt.subplots(nrows=2, ncols=2)
fig.set_figheight(10)
fig.set_figwidth(15)

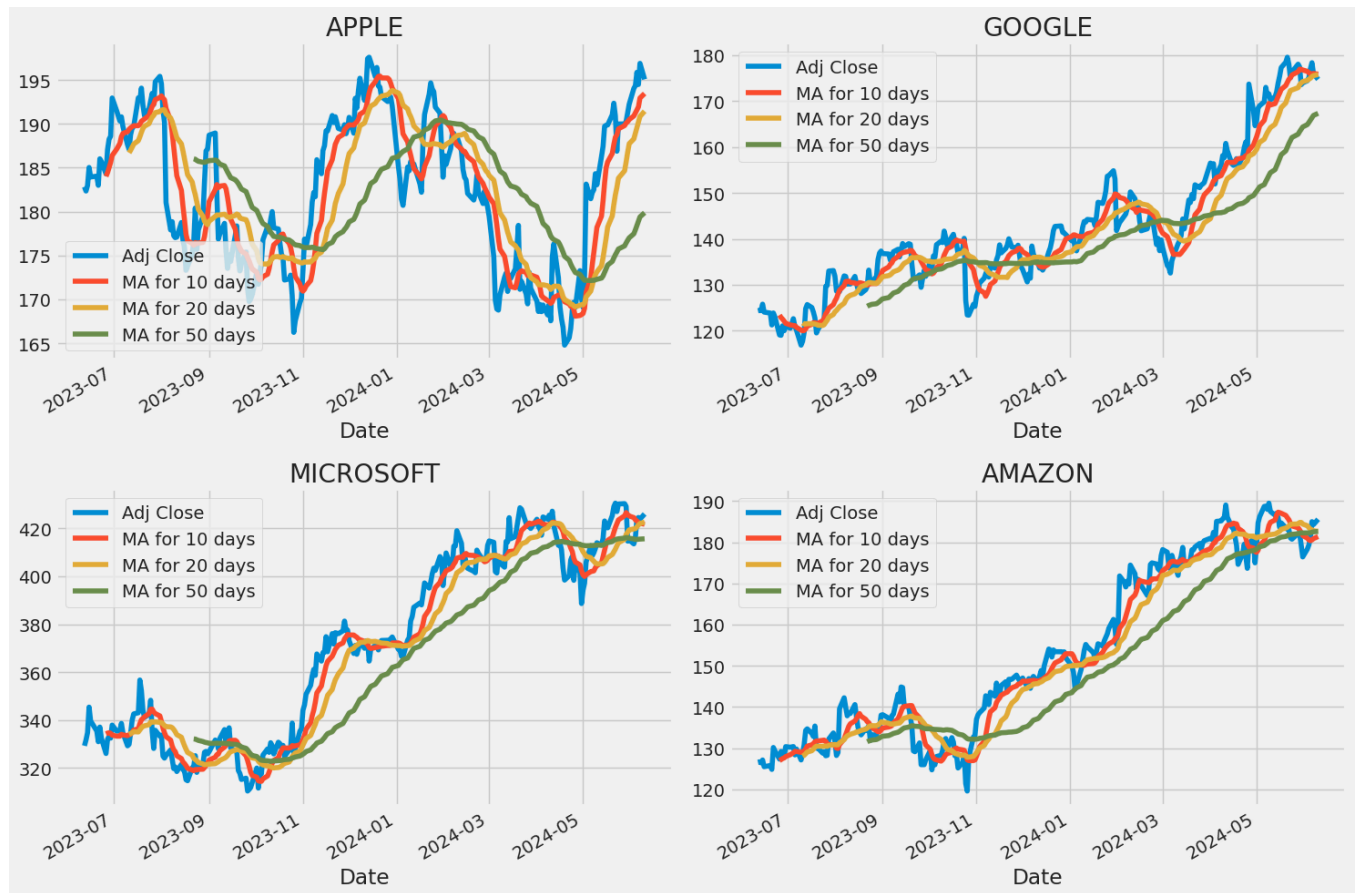
AAPL[['Adj Close', 'MA for 10 days', 'MA for 20 days', 'MA for 50 days']].plot(ax=axes[0,0])
axes[0,0].set_title('APPLE')

GOOG[['Adj Close', 'MA for 10 days', 'MA for 20 days', 'MA for 50 days']].plot(ax=axes[0,1])
axes[0,1].set_title('GOOGLE')

MSFT[['Adj Close', 'MA for 10 days', 'MA for 20 days', 'MA for 50 days']].plot(ax=axes[1,0])
axes[1,0].set_title('MICROSOFT')

AMZN[['Adj Close', 'MA for 10 days', 'MA for 20 days', 'MA for 50 days']].plot(ax=axes[1,1])
axes[1,1].set_title('AMAZON')

fig.tight_layout()
```



We see in the graph that the best values to measure the moving average are 10 and 20 days because we still capture trends in the data without noise.

✓ 3. What was the daily return of the stock on average?

Now that we've done some baseline analysis, let's go ahead and dive a little deeper. We're now going to analyze the risk of the stock. In order to do so we'll need to take a closer look at the daily changes of the stock, and not just its absolute value. Let's go ahead and use pandas to retrieve the daily returns for the Apple stock.

```
# We'll use pct_change to find the percent change for each day
for company in company_list:
    company['Daily Return'] = company['Adj Close'].pct_change()

# Then we'll plot the daily return percentage
fig, axes = plt.subplots(nrows=2, ncols=2)
fig.set_figheight(10)
fig.set_figwidth(15)

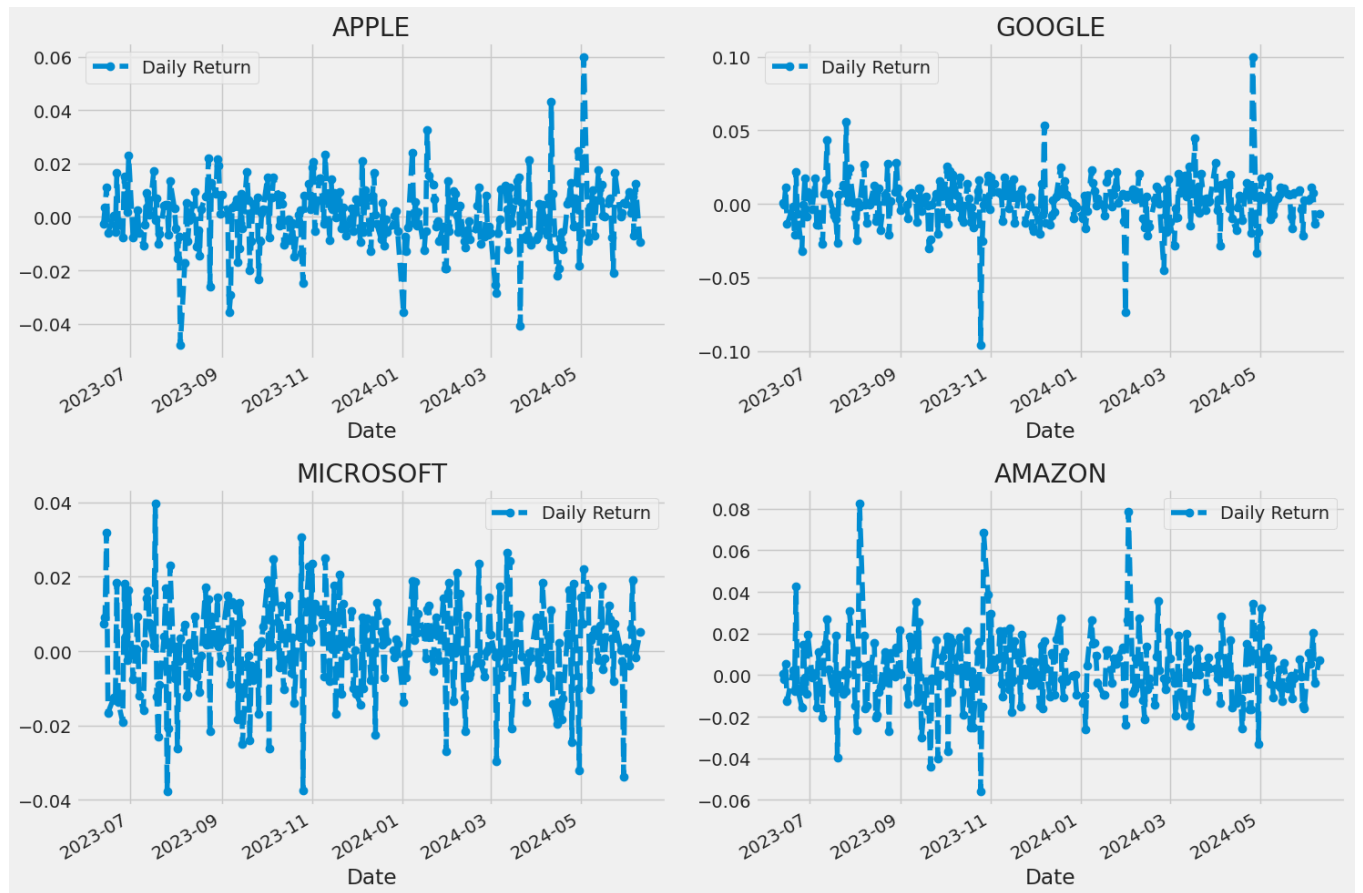
AAPL['Daily Return'].plot(ax=axes[0,0], legend=True, linestyle='--', marker='o')
axes[0,0].set_title('APPLE')

GOOG['Daily Return'].plot(ax=axes[0,1], legend=True, linestyle='--', marker='o')
axes[0,1].set_title('GOOGLE')

MSFT['Daily Return'].plot(ax=axes[1,0], legend=True, linestyle='--', marker='o')
axes[1,0].set_title('MICROSOFT')

AMZN['Daily Return'].plot(ax=axes[1,1], legend=True, linestyle='--', marker='o')
axes[1,1].set_title('AMAZON')

fig.tight_layout()
```

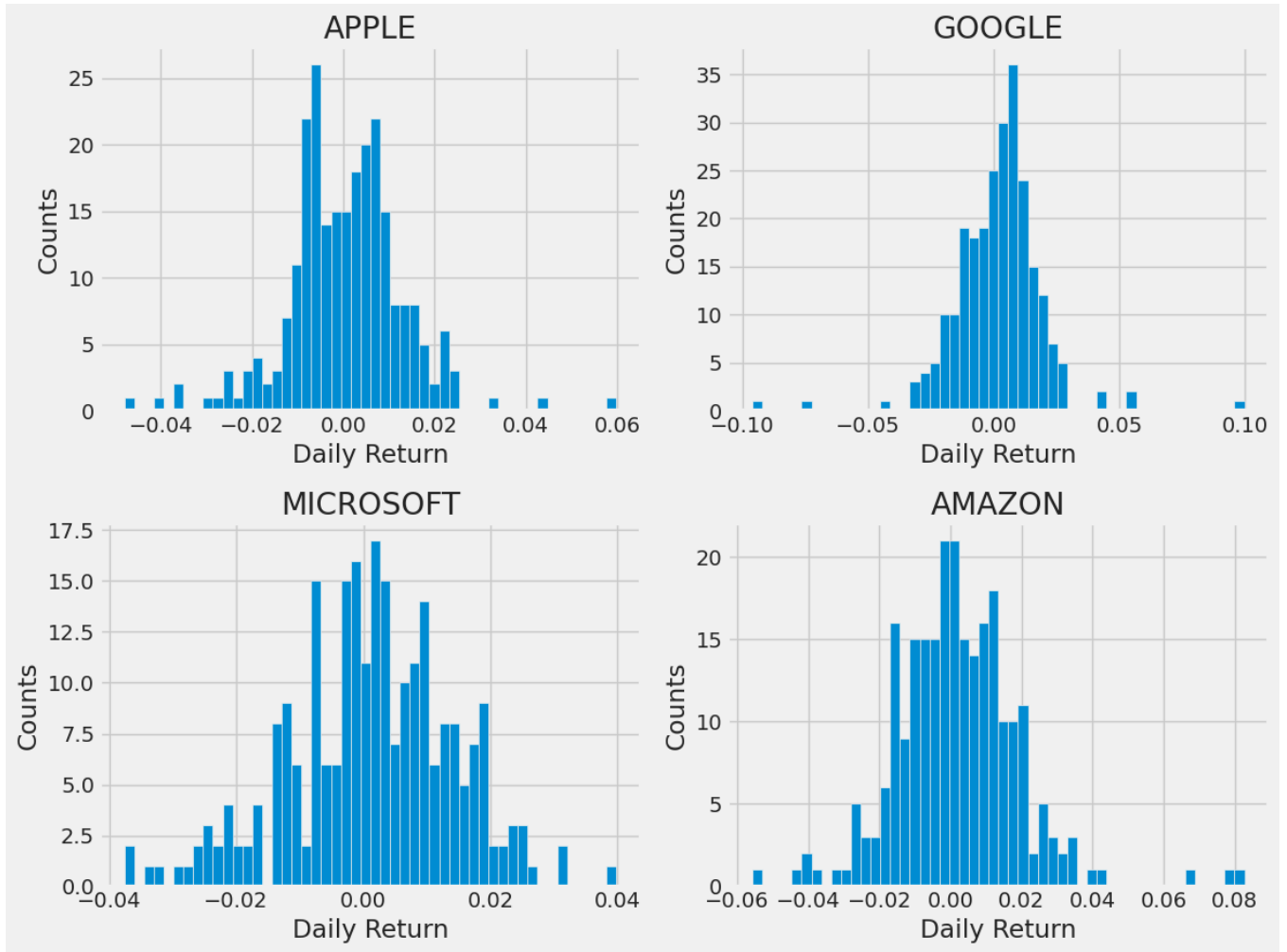


Great, now let's get an overall look at the average daily return using a histogram. We'll use seaborn to create both a histogram and kde plot on the same figure.

```
plt.figure(figsize=(12, 9))

for i, company in enumerate(company_list, 1):
    plt.subplot(2, 2, i)
    company['Daily Return'].hist(bins=50)
    plt.xlabel('Daily Return')
    plt.ylabel('Counts')
    plt.title(f'{company_name[i - 1]}')

plt.tight_layout()
```



✓ 4. What was the correlation between different stocks closing prices?

Correlation is a statistic that measures the degree to which two variables move in relation to each other which has a value that must fall between -1.0 and +1.0. Correlation measures association, but doesn't show if x causes y or vice versa — or if the association is caused by a third factor[1].

Now what if we wanted to analyze the returns of all the stocks in our list? Let's go ahead and build a DataFrame with all the ['Close'] columns for each of the stocks dataframes.

```
# Grab all the closing prices for the tech stock list into one DataFrame
```

```
closing_df = pdr.get_data_yahoo(tech_list, start=start, end=end)['Adj Close']
```

```
# Make a new tech returns DataFrame
```

```
tech_rets = closing_df.pct_change()
```

```
tech_rets.head()
```

 [*****100%*****] 4 of 4 completed


Ticker	AAPL	AMZN	GOOG	MSFT
Date				
2023-06-12	NaN	NaN	NaN	NaN
2023-06-13	-0.002612	0.000711	0.000643	0.007353
2023-06-14	0.003491	-0.001895	-0.000402	0.009124
2023-06-15	0.011199	0.005458	0.011336	0.031897
2023-06-16	-0.005860	-0.012745	-0.013753	-0.016576

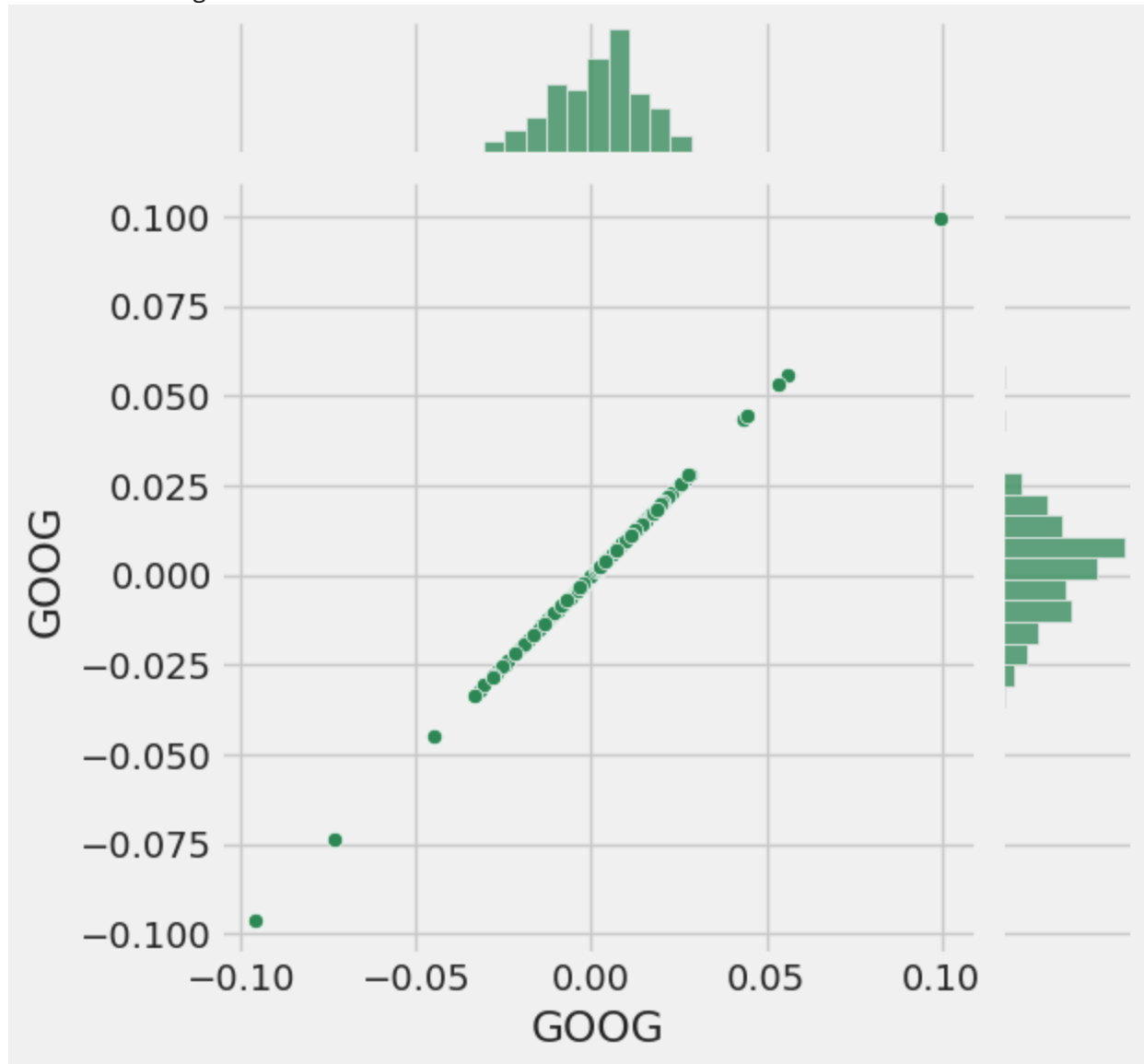
Next steps: [View recommended plots](#)

Now we can compare the daily percentage return of two stocks to check how correlated. First let's see a stock compared to itself.

```
# Comparing Google to itself should show a perfectly linear relationship
```

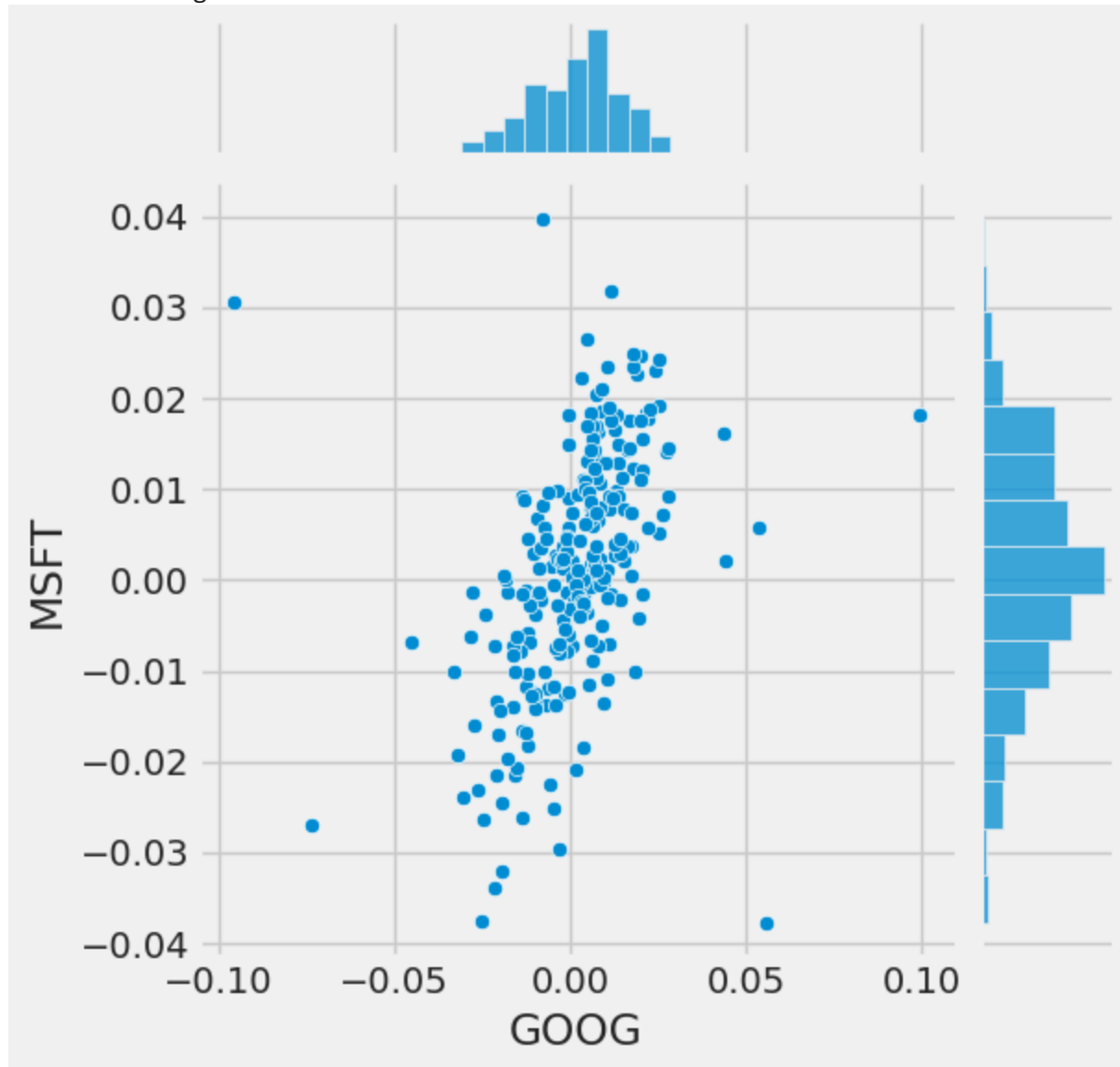
```
sns.jointplot(x='GOOG', y='GOOG', data=tech_rets, kind='scatter', color='seagreen')
```


 <seaborn.axisgrid.JointGrid at 0x7fb67115ff70>



```
# We'll use joinplot to compare the daily returns of Google and Microsoft
sns.jointplot(x='GOOG', y='MSFT', data=tech_rets, kind='scatter')
```

 <seaborn.axisgrid.JointGrid at 0x7fb67107b250>



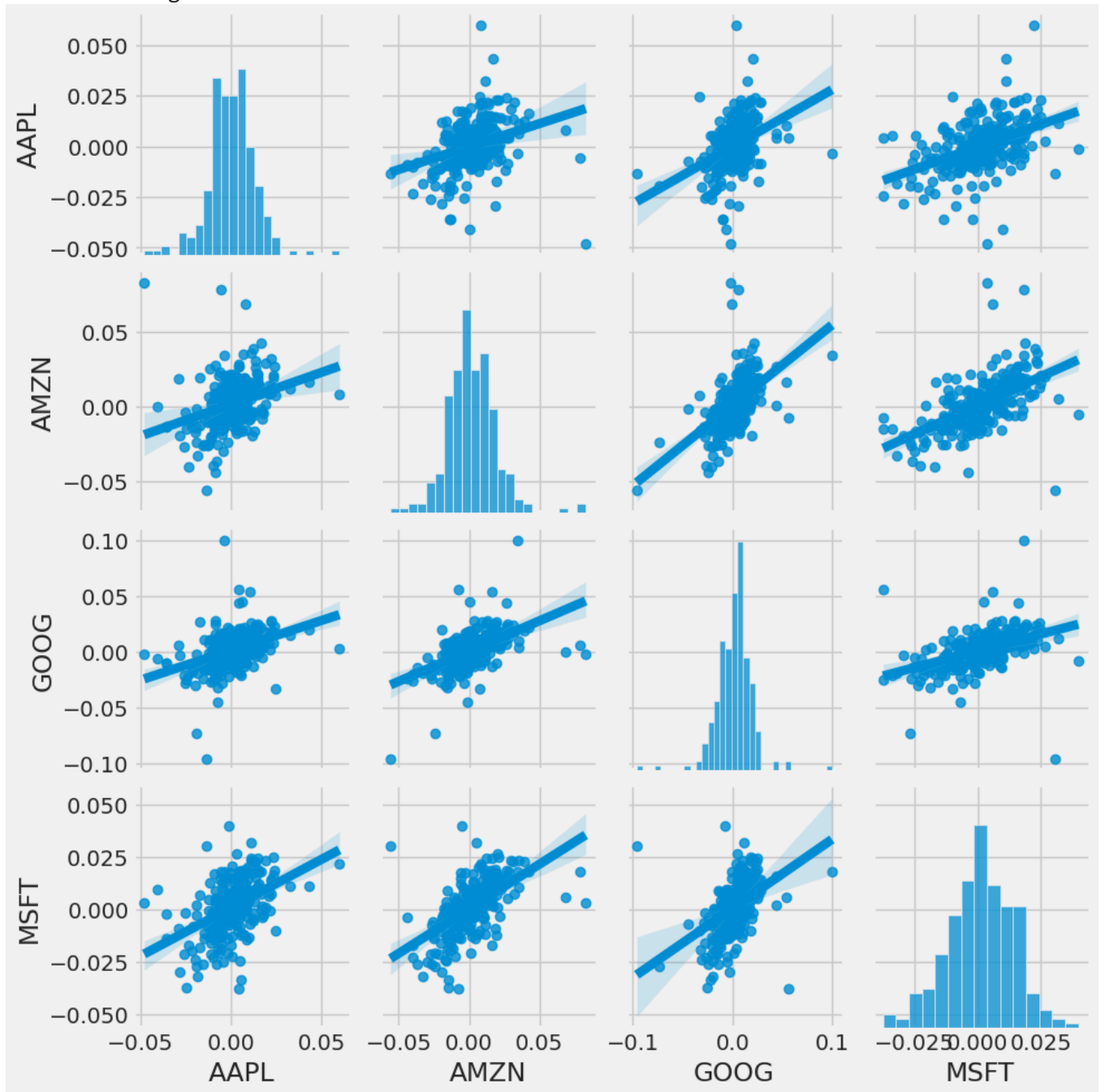
So now we can see that if two stocks are perfectly (and positively) correlated with each other a linear relationship between its daily return values should occur.

Seaborn and pandas make it very easy to repeat this comparison analysis for every possible combination of stocks in our technology stock ticker list. We can use `sns.pairplot()` to automatically create this plot

```
# We can simply call pairplot on our DataFrame for an automatic visual analysis  
# of all the comparisons
```

```
sns.pairplot(tech_rets, kind='reg')
```

 <seaborn.axisgrid.PairGrid at 0x7fb6734a2860>



Above we can see all the relationships on daily returns between all the stocks. A quick glance shows an interesting correlation between Google and Amazon daily returns. It might be interesting to investigate that individual comparison.

While the simplicity of just calling `sns.pairplot()` is fantastic we can also use `sns.PairGrid()` for full control of the figure, including what kind of plots go in the diagonal, the upper triangle, and the lower triangle. Below is an example of utilizing the full power of seaborn to achieve this result.

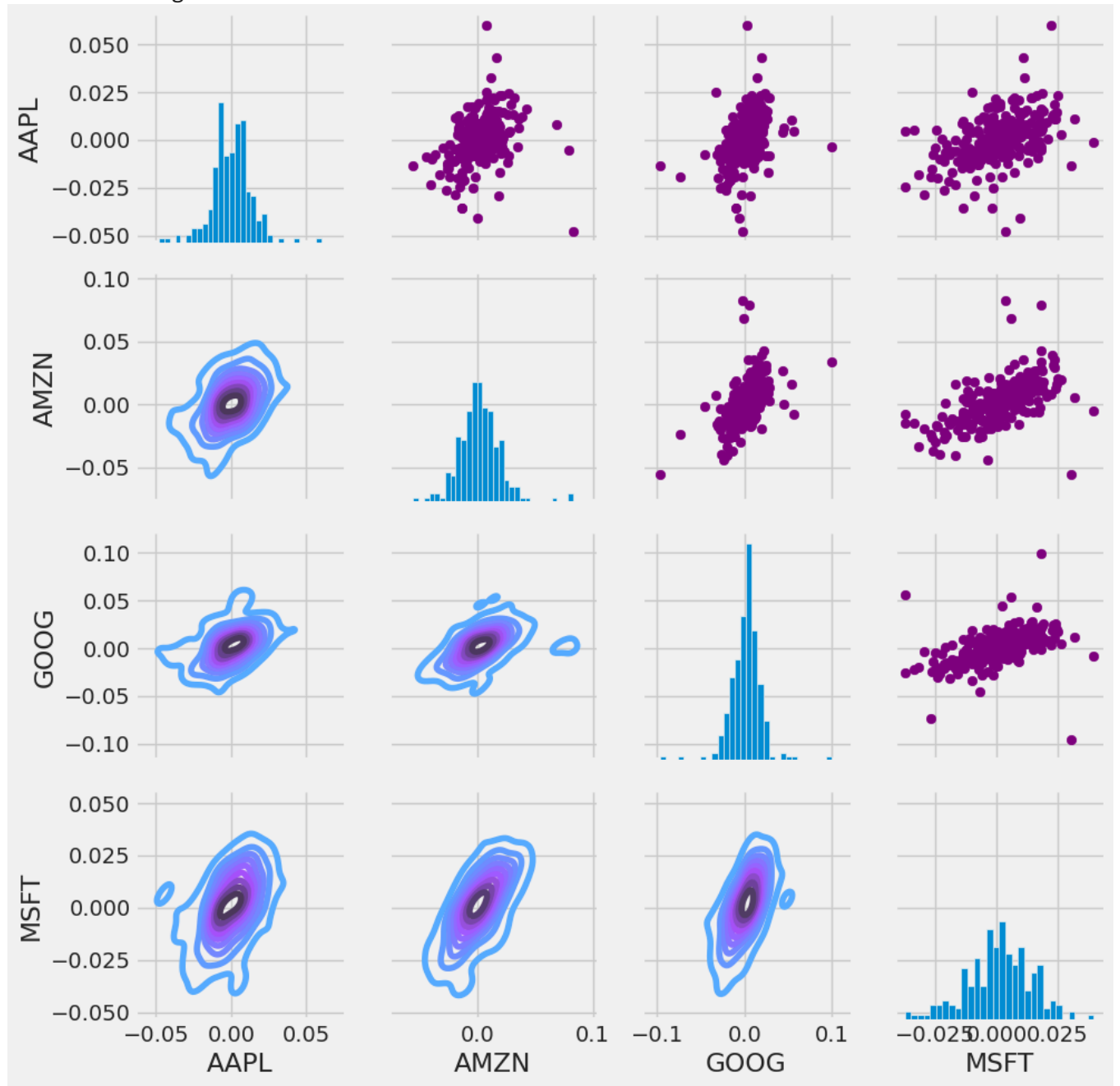
```
# Set up our figure by naming it returns_fig, call PairPlot on the DataFrame
return_fig = sns.PairGrid(tech_rets.dropna())

# Using map_upper we can specify what the upper triangle will look like.
return_fig.map_upper(plt.scatter, color='purple')

# We can also define the lower triangle in the figure, including the plot type (kde)
# or the color map (BluePurple)
return_fig.map_lower(sns.kdeplot, cmap='cool_d')

# Finally we'll define the diagonal as a series of histogram plots of the daily return
return_fig.map_diag(plt.hist, bins=30)
```

 <seaborn.axisgrid.PairGrid at 0x7fb670305660>



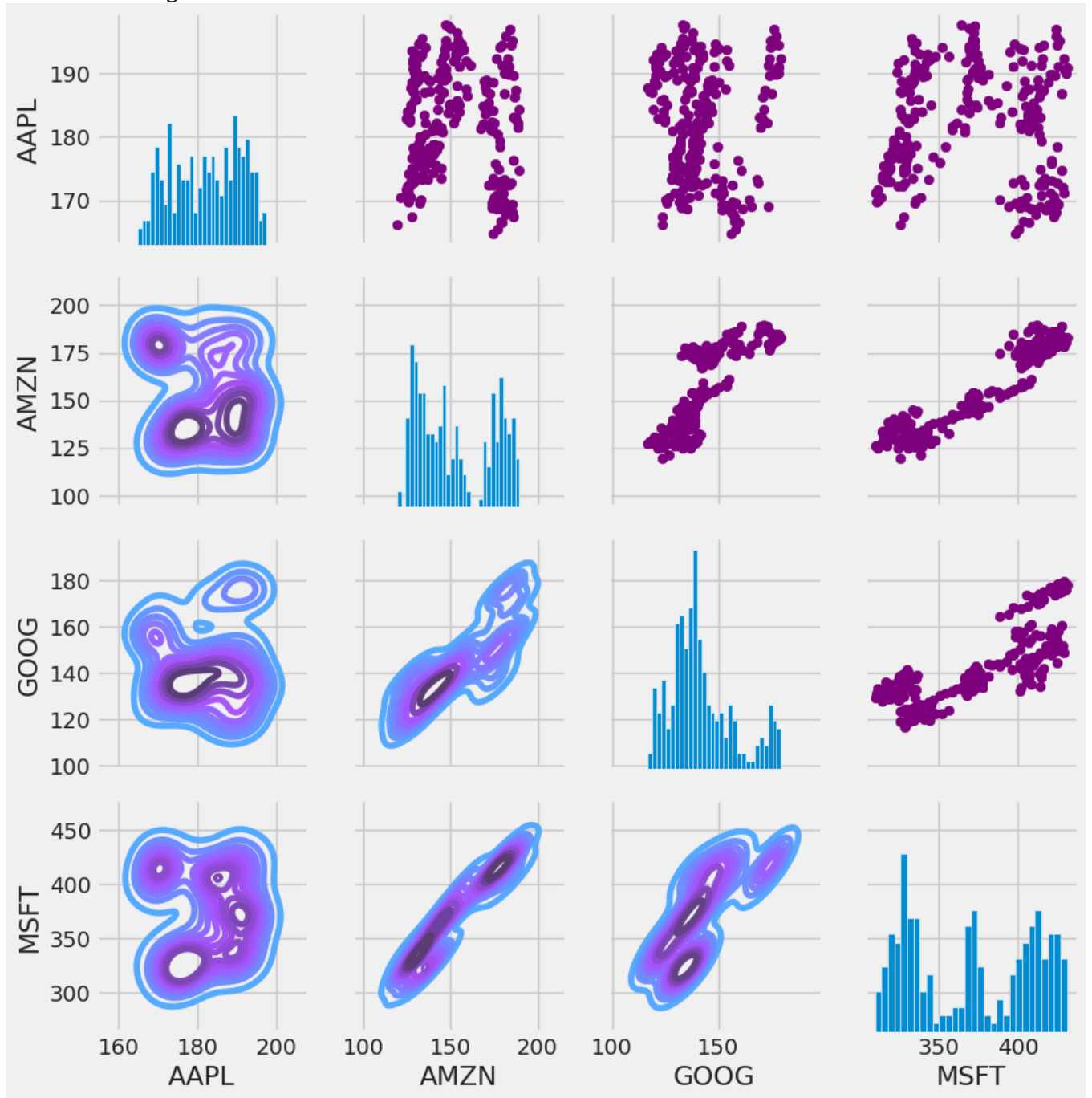
```
# Set up our figure by naming it returns_fig, call PairPlot on the DataFrame
returns_fig = sns.PairGrid(closing_df)

# Using map_upper we can specify what the upper triangle will look like.
returns_fig.map_upper(plt.scatter,color='purple')

# We can also define the lower triangle in the figure, including the plot type (kde) or the
returns_fig.map_lower(sns.kdeplot,cmap='cool_d')

# Finally we'll define the diagonal as a series of histogram plots of the daily return
returns_fig.map_diag(plt.hist,bins=30)
```

 <seaborn.axisgrid.PairGrid at 0x7fb66991a6b0>



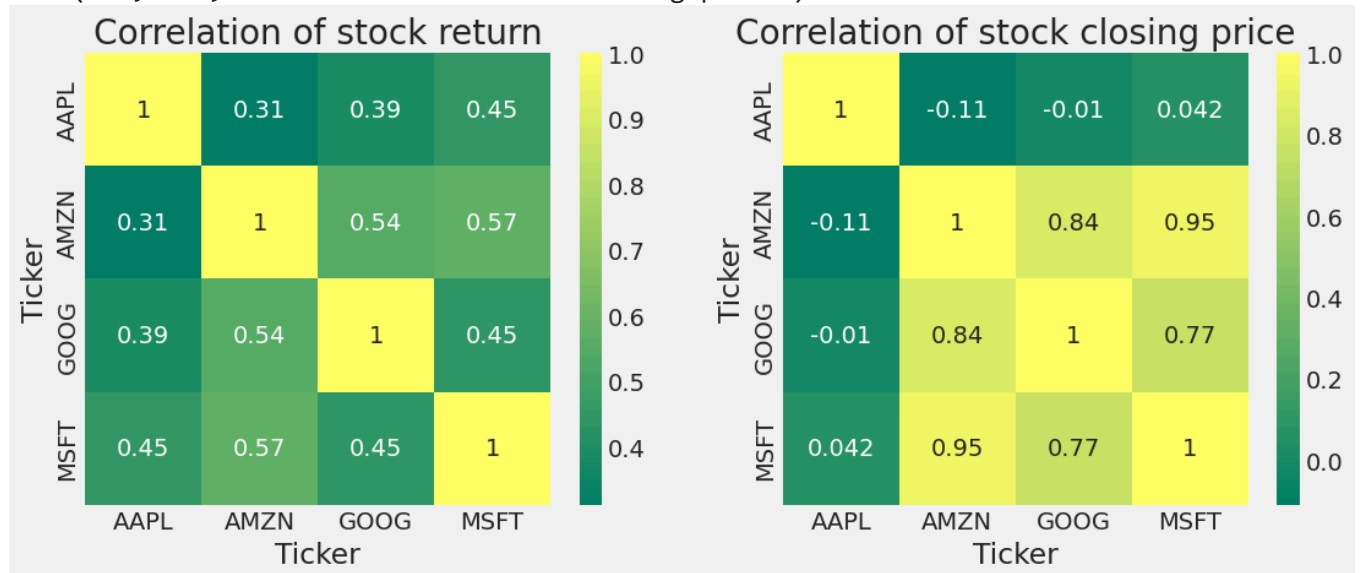
Finally, we could also do a correlation plot, to get actual numerical values for the correlation between the stocks' daily return values. By comparing the closing prices, we see an interesting relationship between Microsoft and Apple.

```
plt.figure(figsize=(12, 10))
```

```
plt.subplot(2, 2, 1)
sns.heatmap(tech_rets.corr(), annot=True, cmap='summer')
plt.title('Correlation of stock return')
```

```
plt.subplot(2, 2, 2)
sns.heatmap(closing_df.corr(), annot=True, cmap='summer')
plt.title('Correlation of stock closing price')
```

```
plt.text(0.5, 1.0, 'Correlation of stock closing price')
```



Just like we suspected in our `PairPlot` we see here numerically and visually that Microsoft and Amazon had the strongest correlation of daily stock return. It's also interesting to see that all the technology companies are positively correlated.

✓ 5. How much value do we put at risk by investing in a particular stock?

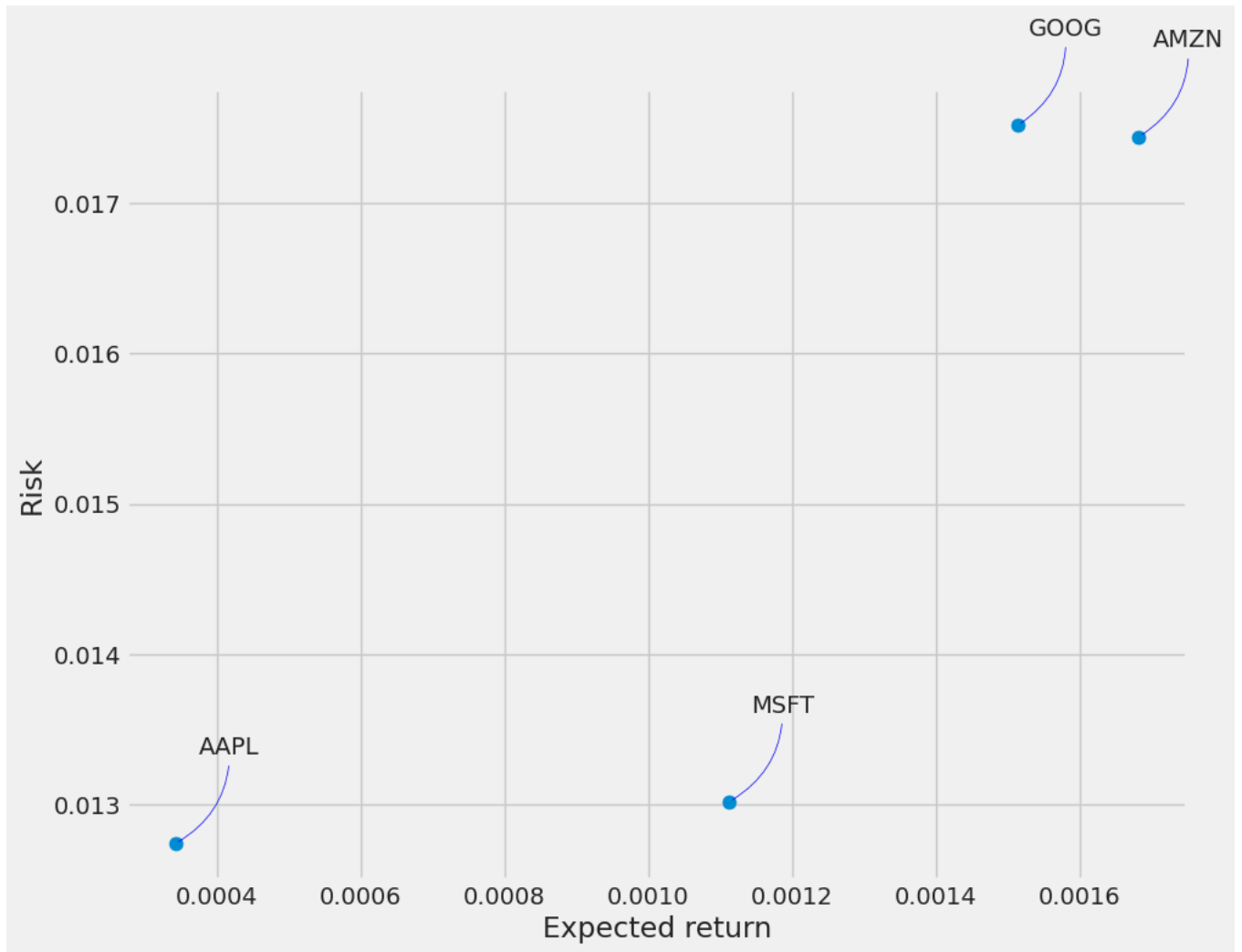
There are many ways we can quantify risk, one of the most basic ways using the information we've gathered on daily percentage returns is by comparing the expected return with the standard deviation of the daily returns.

```
rets = tech_rets.dropna()

area = np.pi * 20

plt.figure(figsize=(10, 8))
plt.scatter(rets.mean(), rets.std(), s=area)
plt.xlabel('Expected return')
plt.ylabel('Risk')

for label, x, y in zip(rets.columns, rets.mean(), rets.std()):
    plt.annotate(label, xy=(x, y), xytext=(50, 50), textcoords='offset points', ha='right',
                  arrowprops=dict(arrowstyle='-', color='blue', connectionstyle='arc3,rad=-0.5))
```



✓ 6. Predicting the closing price stock price of APPLE inc:

```
pip install arch
```



Collecting arch

Downloading arch-7.0.0-cp310-cp310-manylinux_2_17_x86_64.manylinux2014_x86_64.whl (983

983.4/983.4 kB 5.5 MB/s eta 0:00:00

Requirement already satisfied: numpy>=1.22.3 in /usr/local/lib/python3.10/dist-packages
 Requirement already satisfied: scipy>=1.8 in /usr/local/lib/python3.10/dist-packages (fr
 Requirement already satisfied: pandas>=1.4 in /usr/local/lib/python3.10/dist-packages (f
 Requirement already satisfied: statsmodels>=0.12 in /usr/local/lib/python3.10/dist-packa
 Requirement already satisfied: python-dateutil>=2.8.2 in /usr/local/lib/python3.10/dist-
 Requirement already satisfied: pytz>=2020.1 in /usr/local/lib/python3.10/dist-packages (
 Requirement already satisfied: tzdata>=2022.1 in /usr/local/lib/python3.10/dist-packages
 Requirement already satisfied: patsy>=0.5.6 in /usr/local/lib/python3.10/dist-packages (
 Requirement already satisfied: packaging>=21.3 in /usr/local/lib/python3.10/dist-package
 Requirement already satisfied: six in /usr/local/lib/python3.10/dist-packages (from pats
 Installing collected packages: arch
 Successfully installed arch-7.0.0



ARIMA and GARCH models

```
from statsmodels.tsa.arima.model import ARIMA
```

```
from arch import arch_model
```

Get the stock quote

```
df = pdr.get_data_yahoo('AAPL', start='2012-01-01', end=datetime.now())
```

Show teh data

```
df
```



[*****100%*****] 1 of 1 completed

	Open	High	Low	Close	Adj Close	Volume
Date						
2012-01-03	14.621429	14.732143	14.607143	14.686786	12.416981	302220800
2012-01-04	14.642857	14.810000	14.617143	14.765714	12.483709	260022000
2012-01-05	14.819643	14.948214	14.738214	14.929643	12.622306	271269600
2012-01-06	14.991786	15.098214	14.972143	15.085714	12.754258	318292800
2012-01-09	15.196429	15.276786	15.048214	15.061786	12.734029	394024400
...
2024-06-04	194.639999	195.320007	193.029999	194.350006	194.350006	47471400
2024-06-05	195.399994	196.899994	194.869995	195.869995	195.869995	54156800
2024-06-06	195.690002	196.500000	194.169998	194.479996	194.479996	41181800
2024-06-07	194.649994	196.940002	194.139999	196.889999	196.889999	53044700
2024-06-10	197.199997	197.281693	194.830002	195.128998	195.128998	14358294

3129 rows × 6 columns



Next steps: [View recommended plots](#)

```
plt.figure(figsize=(16,6))
plt.title('Close Price History')
plt.plot(df['Close'])
plt.xlabel('Date', fontsize=18)
plt.ylabel('Close Price USD ($)', fontsize=18)
plt.show()
```



```
# Create a new dataframe with only the 'Close column
data = df.filter(['Close'])
# Convert the dataframe to a numpy array
dataset = data.values
# Get the number of rows to train the model on
training_data_len = int(np.ceil( len(dataset) * .95 ))
```


```
training_data_len
```

 2973

```
# Scale the data
from sklearn.preprocessing import MinMaxScaler
```

```
scaler = MinMaxScaler(feature_range=(0,1))
scaled_data = scaler.fit_transform(dataset)
```

```
scaled_data
```


 array([[0.00401431],
[0.00444289],
[0.00533302],
...,
[0.98028912],
[0.99337541],
[0.98381319]])

```
# Create the training data set
# Create the scaled training data set
train_data = scaled_data[0:int(training_data_len), :]
# Split the data into x_train and y_train data sets
x_train = []
y_train = []
```

```
for i in range(60, len(train_data)):
    x_train.append(train_data[i-60:i, 0])
    y_train.append(train_data[i, 0])
    if i<= 61:
        print(x_train)
        print(y_train)
        print()
```

```
# Convert the x_train and y_train to numpy arrays
x_train, y_train = np.array(x_train), np.array(y_train)
```

```
# Reshape the data
x_train = np.reshape(x_train, (x_train.shape[0], x_train.shape[1], 1))
# x_train.shape
```

 [array([0.00401431, 0.00444289, 0.00533302, 0.00618049, 0.00605056,
0.00634339, 0.00620958, 0.00598462, 0.00567821, 0.00662652,

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0.02440779, 0.02557523, 0.0262249 , 0.02809631, 0.02945961,
0.02985329, 0.02999098, 0.02765997, 0.02709757, 0.02718096,
0.02937236, 0.02998905, 0.03131358, 0.03443581, 0.03860139,
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[array([0.00401431, 0.00444289, 0.00533302, 0.00618049, 0.00605056,
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