QP-1 : Single-photon interferometer coding and simulation

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The Single-Photon interferometer experiment:

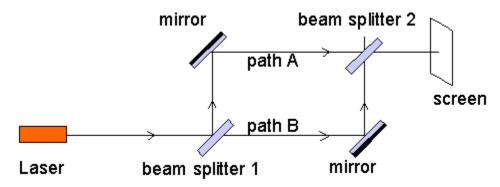


Fig 01 : Demonstration of a Single-Photon interferometer experiment

In the figure above, the incident photon is in horizontal direction. But in this assignment, I will convert the input state to |1> using a NOT gate, which makes it **vertical**.

1. Quantum Circuit code and output

i) Imports:

```
In [1]: # Importing the QuantumCircuit class from Qiskit
# The QuantumCircuit class is used to create quantum circuits
from qiskit import QuantumCircuit

# Importing the numpy library
# Numpy is used for working with arrays and perform numerical operations
import numpy as np
```

ii) Quantum circuit creation:

```
In [2]: # My Circuit will use 1 qubit and 1 classical bit
# So parameterizing the value to use it in all places
n = 1
```

```
# I am creating a new object of the QuantumCircuit class
# I am assigning this object to the variable named 'circuit'
# The QuantumCircuit constructor takes 2 arguments: (Qubits, Classical bits)
# In my circuit, parameter n = 1, so 1 qubit and 1 classical bit is there
circuit = QuantumCircuit(n, n)
```

iii) Adding different components to my circuit :

```
In [3]: # By default, the input state is |0>
        # So, I am transforming the default state |0) to |1)
        # So, applied an X gate to flip |0) to |1) , so the Input state is now |1>
        circuit.x(0)
        # 1st Beam splitter:
        # I am applying a rotation gate Rx around the x-axis by -\pi/2 rad to qubit 0.
        # The rx method takes 2 arguments (angle of rotation, qubit index)
        # The angle of rotation is -90^{\circ} = -\pi/2 rad. Numpy computes this value.
        # The rx gate is applied on the first index gubit 0
        circuit.rx(-np.pi/2, 0)
        # Mirror :
        # I am applying an X gate on the first index gubit 0.
        # This X gate is equivalent to NOT gate which reverses the qubit state.
        circuit.x(0)
        # 2nd Beam splitter :
        # I am applying another rotation gate Rx
        # around the x-axis by -\pi/2 rad to qubit 0.
        circuit.rx(-np.pi/2, 0)
```

Out[3]: <qiskit.circuit.instructionset.InstructionSet at 0x1d7f7638b50>

iv) Measurement and circuit diagram:

```
In [4]: # The measure method is used to measure qubit
# and store the result in classical bit.
# It takes 2 arguments (qubits, classical bits)
# I am measuring the single qubit index 0
# I am storing the result in single classical bit 0
circuit.measure([0], [0])

# The draw method is used to visualize the quantum circuit.
# I am drawing the circuit using the 'mpl' output and 'iqp' style
# mpl is used to render the quantum circuit using Matplotlib library.
# iqp is used for styling the circuit diagram.
circuit.draw(output='mpl', style='iqp')
```

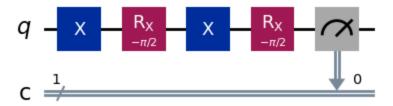


Fig 02: Quantum Circuit for the Single Photon Interferometer

The above circuit diagram comprises of following notations and components :

Circuit Notations:

- **q** is the quantum bit which is represented by the solid horizontal line.
- **c** is the classical bit after measurement which is represented by the double lines.
- 1/ above the double lines represents the no. of classical data bits.

Circuit Components:

- X in blue box represents the NOT gate. It is used to flip the input state from |0> to |1> i.e Horizontal to Vertical conversion.
- $\mathbf{R}\mathbf{x}$ in red box represents the 1st Beam-Splitter. It is used to apply rotation around the x-axis by $-\pi/2$ rad.
- X in blue box represents the Mirror. It is used to reflect the photon's path.
- $\mathbf{R}\mathbf{x}$ in red box represents the 2nd Beam-Splitter. It is used to apply rotation around the x-axis by $-\pi/2$ rad.
- Meter in gray box represents the Measurement operation.

2. Simulation code and output

i) Imports:

```
In [5]: # The qiskit_aer library provides backend quantum simulators
# I am importing the Aer module which contains various type of simulators.
from qiskit_aer import Aer

# I am importing the transpile function from the qiskit library
# Transpile function is required to ensure that my circuit
# is able to run on the simulator.
from qiskit import transpile

# Importing the plot_histogram function from qiskit
# It used to visualize the simulation result.
from qiskit.visualization import plot_histogram
```

ii) Getting the Simulator and running it

```
In [6]: # I am creating a new backend object of Aer
# I am assigning this object to the variable named 'simulator'
# I am using the "qasm_simulator" backend from Aer.
# The qasm simulator runs the circuit and its result is classical bits.
simulator = Aer.get_backend("qasm_simulator")

# Transpile transforms the circuit to something appropriate for the machine.
# I am transpiling my circuit for the backend qasm simulator
# I am storing my transpiled circuit in variable named'sim_circuit'
sim_circuit = transpile(circuit, backend = simulator)

# The run method in the simulator executes the transpiled circuit
# run method returns a job object which I am storing in variable named 'job'
job = simulator.run(sim_circuit)
```

iii) Fetching the result and plotting histogram:

```
In [7]: # I am fetching the results of the simulation job execution.
# I am storing this result in variable named 'result'.
# This result contains the counts of each measurement outcome.
result = job.result()

# I am generating and displaying a histogram of the simulation outcomes.
# result.get_counts() method is used to find the count of different outcomes
# By default, the no. of trials is 1024.
plot_histogram(result.get_counts())
```

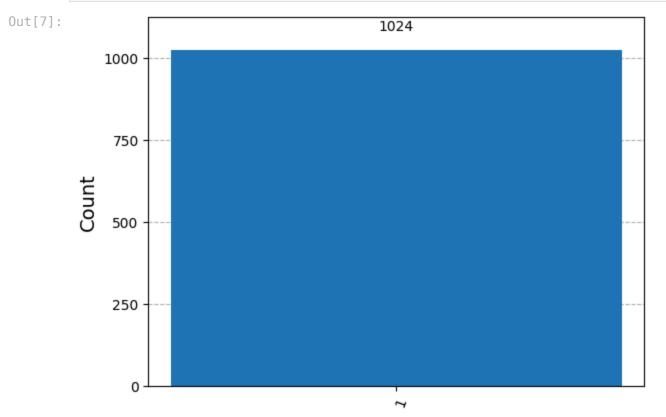


Fig 03 : Measured state Vs Counts

The histogram represents the probability of measuring the output state when my quantum circuit runs on the simulator.

In the above histogram:

- The **x-axis** represents the measured state.
- The **y-axis** represents the number of times each state was measured. By default, it is 1024 times.

Here, there is 1 on x-axis, which means that the measurement found the qubit in $|1\rangle$ state. The qubit remained in the $|1\rangle$ state after 1024 trials. This is in accordance with our vertical setup.

