

$$\begin{aligned}
 & t \cdot \sqrt{\Delta^2 + \Omega^2} \\
 &= t \Delta \sqrt{1 + \frac{\Omega^2}{\Delta^2}} \\
 &\approx \Delta \left(1 + \frac{\Omega^2}{2\Delta^2} \right) \qquad = t \Omega \sqrt{1 + \frac{\Delta^2}{\Omega^2}} \\
 &\qquad \qquad \qquad = t \Omega \left(1 + \frac{\Delta^2}{2\Omega^2} \right)
 \end{aligned}$$

$$\varepsilon(a+a^\dagger) \text{ or } \frac{\varepsilon}{\delta}(a+a^\dagger)$$

$$H = \varepsilon(t) \cdot (a+a^\dagger) \qquad \varepsilon(z) = \bar{\varepsilon} e^{-\frac{t^2}{2\sigma^2}}$$

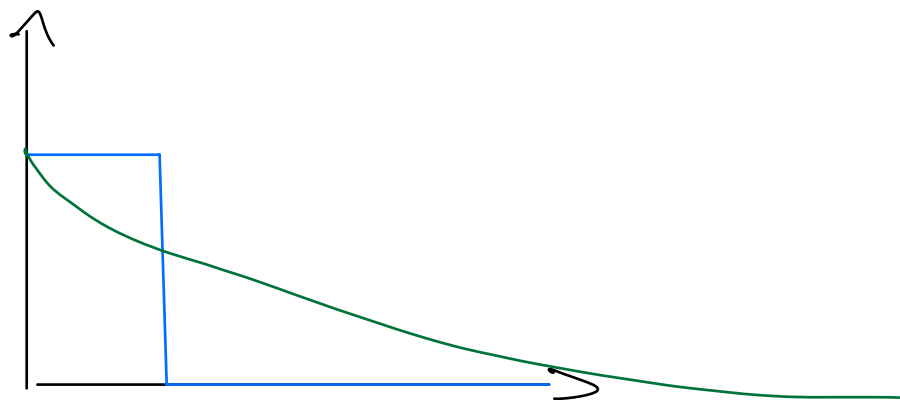
$$U = e^{-i \int_0^t \varepsilon(z) (a+a^\dagger) dz} = D(f(z))$$

$$D(f(z))|0\rangle = |f(z)\rangle$$

What coherent state has $P(1)$ maximal?

$$|\alpha\rangle = e^{-\frac{|\alpha|^2}{2}} \sum_n \frac{\alpha^n}{\sqrt{n!}} |n\rangle$$

for what α is $\alpha e^{-|\alpha|^2/2}$ maximal



$$|4\rangle \rightarrow K_{gg}|4\rangle$$

$$|4\rangle: N$$

$$|4\rangle: N^2$$

$$\rho = K_{gg}\rho K_{gg}^\dagger + K_{ge}\rho K_{ge}^\dagger + \dots$$

$$= \sum_j K_{ij}\rho K_{ij}^\dagger$$

$$\rho = N^2$$

$$F = |\langle \varphi | \phi \rangle| = \sqrt{\langle \phi | \rho | \phi \rangle}$$

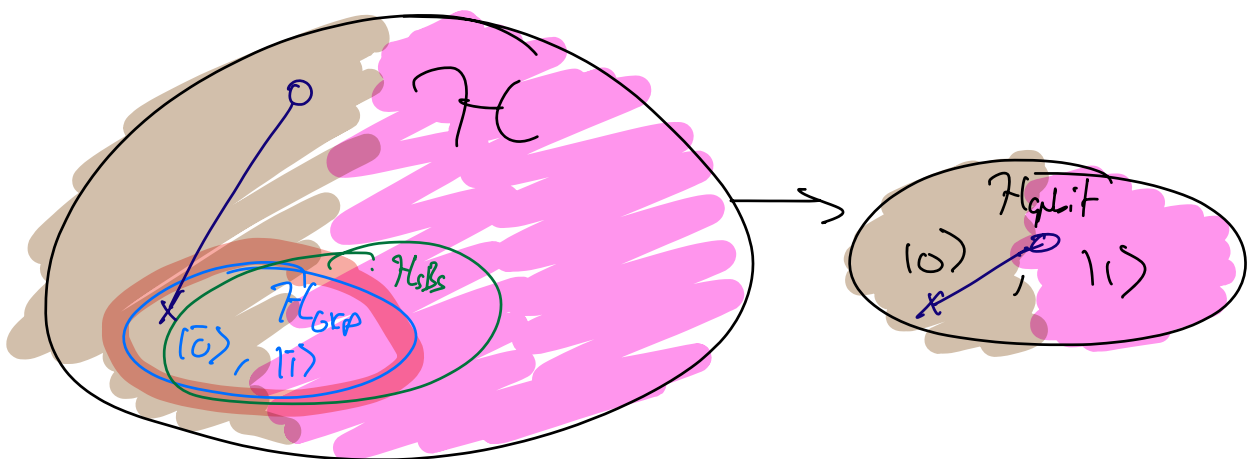
$$F = |\langle \varphi | \phi \rangle|^2$$

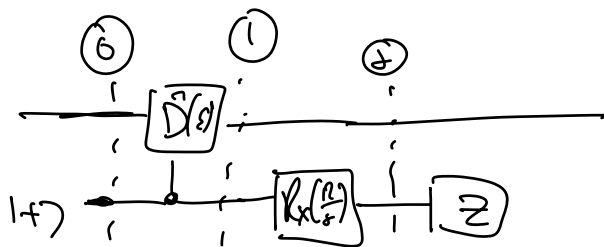
$$F_{\phi, \rho} = \langle \phi | \rho | \phi \rangle$$

$$\rho = |\psi\rangle\langle\psi|$$

$$\rho = p_1 |\psi_1\rangle\langle\psi_1| + p_2 |\psi_2\rangle\langle\psi_2|$$

$$F_{\phi, \rho} = p_1 |\langle \phi | \psi_1 \rangle|^2 + p_2 |\langle \phi | \psi_2 \rangle|^2$$





$$C\hat{D}(\epsilon) = |g\rangle\langle g| \otimes D(\frac{\epsilon}{2}) + |e\rangle\langle e| \otimes D(-\frac{\epsilon}{2})$$

$$\textcircled{0} |\psi\rangle \otimes |\phi\rangle = |\psi\rangle \otimes \frac{|g\rangle + |e\rangle}{\sqrt{2}}$$

$$\textcircled{1} = C\hat{D}(\epsilon) \left[|\psi\rangle \otimes \frac{|g\rangle + |e\rangle}{\sqrt{2}} \right] = \frac{\hat{D}(\frac{\epsilon}{2})|\psi, g\rangle}{\sqrt{2}} + \frac{\hat{D}(-\frac{\epsilon}{2})|\psi, e\rangle}{\sqrt{2}}$$

$R_x(\frac{\pi}{2}) = \frac{-iX}{\sqrt{2}}$
 $e^{-i\frac{\theta}{2}X} = \cos\frac{\theta}{2}I - i\sin\frac{\theta}{2}X$

$$\textcircled{2} = \frac{\hat{D}(\frac{\epsilon}{2})|\psi\rangle \otimes (|g\rangle - i|e\rangle)}{2} + \frac{\hat{D}(-\frac{\epsilon}{2})|\psi\rangle \otimes (|e\rangle - i|g\rangle)}{2}$$

$$= \frac{1}{2} \left\{ \left[\hat{D}(\frac{\epsilon}{2}) - i\hat{D}(-\frac{\epsilon}{2}) \right] |\psi, g\rangle + \left[i\hat{D}(\frac{\epsilon}{2}) + \hat{D}(-\frac{\epsilon}{2}) \right] |\psi, e\rangle \right\}$$

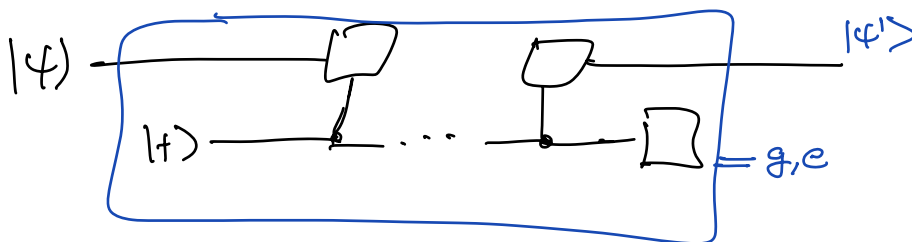
$\underbrace{\quad}_{=K_g}$

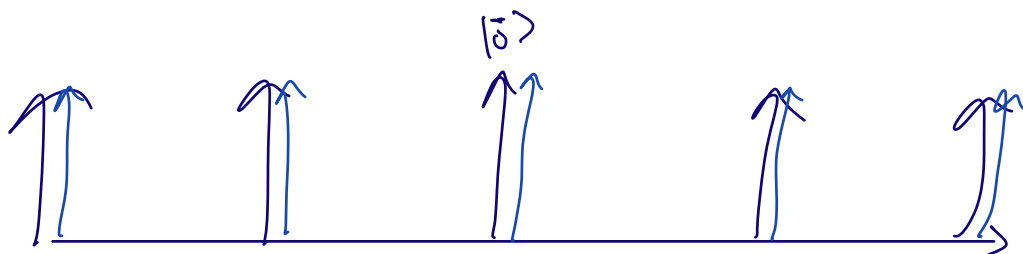
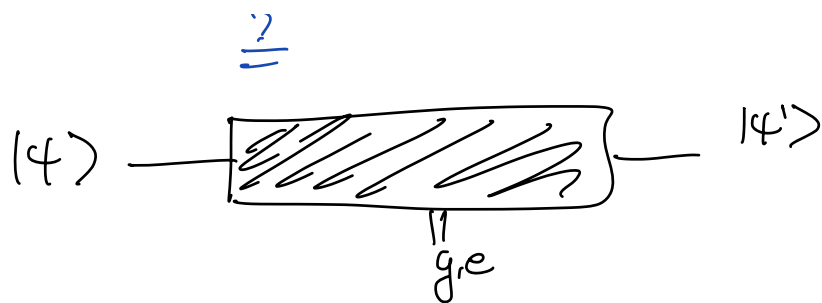
measure
down: $|\psi'\rangle = \frac{1}{2} \left[\hat{D}(\frac{\epsilon}{2}) - i\hat{D}(-\frac{\epsilon}{2}) \right] |\psi\rangle$

avec prob. $\langle \psi' | \psi' \rangle =$

reverse
up: $|\psi'\rangle = \frac{-i}{2} \left[\hat{D}(\frac{\epsilon}{2}) + i\hat{D}(-\frac{\epsilon}{2}) \right] |\psi\rangle$

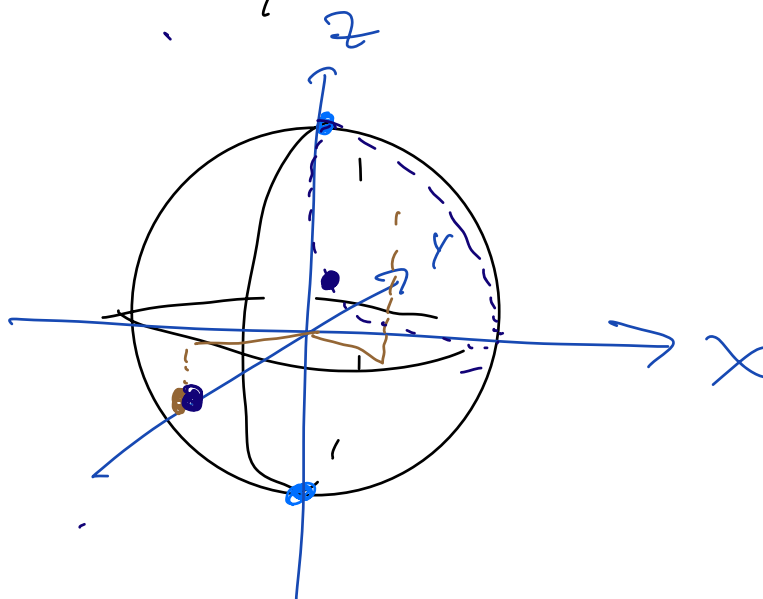
$\underbrace{\quad}_{=K_e}$

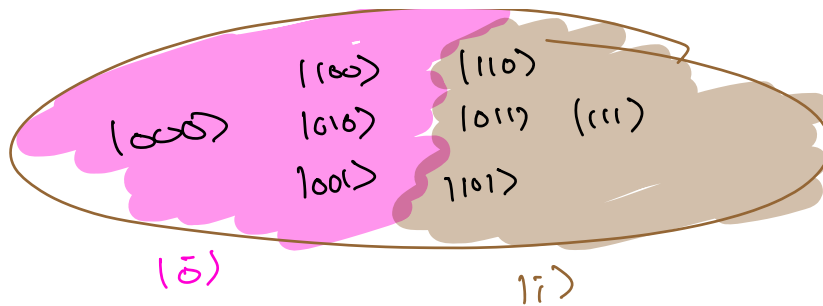




Prepare $|0_{\text{aux}}\rangle$
 J^x apply SBs
 J^z compute $\langle 0 | \rho | 0 \rangle$

$$\rho = \frac{|0\rangle\langle 0| + |\chi\rangle\langle \chi|}{2}$$





$$\begin{aligned} \alpha|000\rangle + \beta|111\rangle &\rightarrow \alpha|0\rangle + \beta|1\rangle \\ \alpha|100\rangle + \beta|011\rangle &\rightarrow \alpha|0\rangle + \beta|1\rangle \\ \alpha|000\rangle + \beta|011\rangle &\rightarrow \rho = |\alpha|^2 |0\rangle\langle 0| + |\beta|^2 |1\rangle\langle 1| \end{aligned}$$

mesurer $Z_1 Z_2$ $+1$ avec prob $|\alpha|^2$
 $Z_2 Z_3$ $+1$

$$|4\rangle \rightarrow \rho_{\text{qubit}} = \frac{1 + \vec{r} \cdot \vec{\sigma}}{2}$$

$$\vec{\sigma} = (\sigma_x, \sigma_y, \sigma_z)$$

$$\langle \sigma_z \rangle = \text{Tr}(\sigma_z \rho_{\text{qubit}}) = r_z$$



$$\langle \bar{Z} \rangle_4 = r_z$$

$$\langle \bar{X} \rangle_4 = r_x$$

$$\langle \bar{Y} \rangle_4 = r_y$$

$$\bar{Z} = \frac{1}{\sqrt{2}} (i\sqrt{2})$$

$$|\phi_{\sqrt{H}}\rangle = \sqrt{H} \cdot |0\rangle$$

$$F = \langle \phi_{\sqrt{H}} | \rho | \phi_{\sqrt{H}} \rangle$$

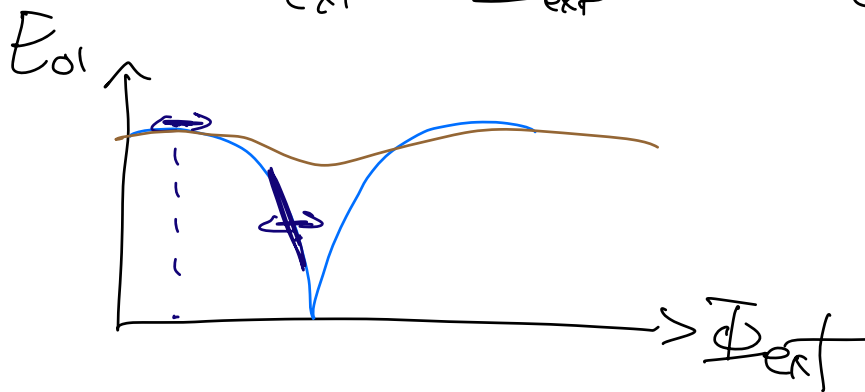
$$\rho = \rho_1 \psi_1 + \rho_2 \psi_2$$

$$= \rho_1 \left(\frac{1 + \vec{r}_1 \cdot \vec{\sigma}}{2} \right) + \rho_2 \left(\frac{1 + \vec{r}_2 \cdot \vec{\sigma}}{2} \right)$$

$$= \frac{1 + (\rho_1 \vec{r}_1 + \rho_2 \vec{r}_2) \cdot \vec{\sigma}}{2}$$

$$\frac{\partial E_0}{\partial \Phi}$$

$$\Phi_{\text{ext}} = \overline{\Phi}_{\text{ext}} + \delta \Phi(t)_{\text{env}}$$



$$T_2 \sim \frac{\partial E_{01}}{\partial \Phi} \cdot S(0)$$