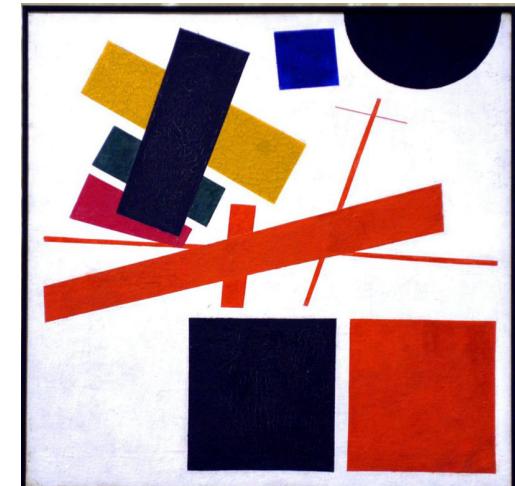


CPEN 422

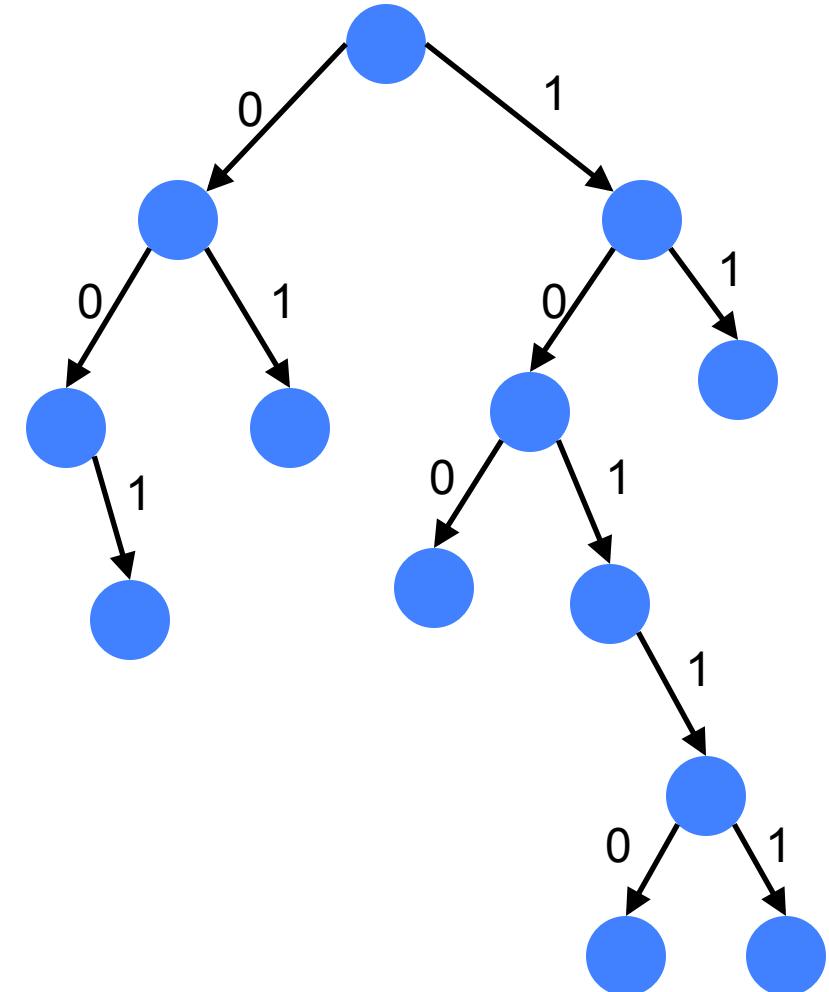
Software Testing and Analysis



Lecture 13

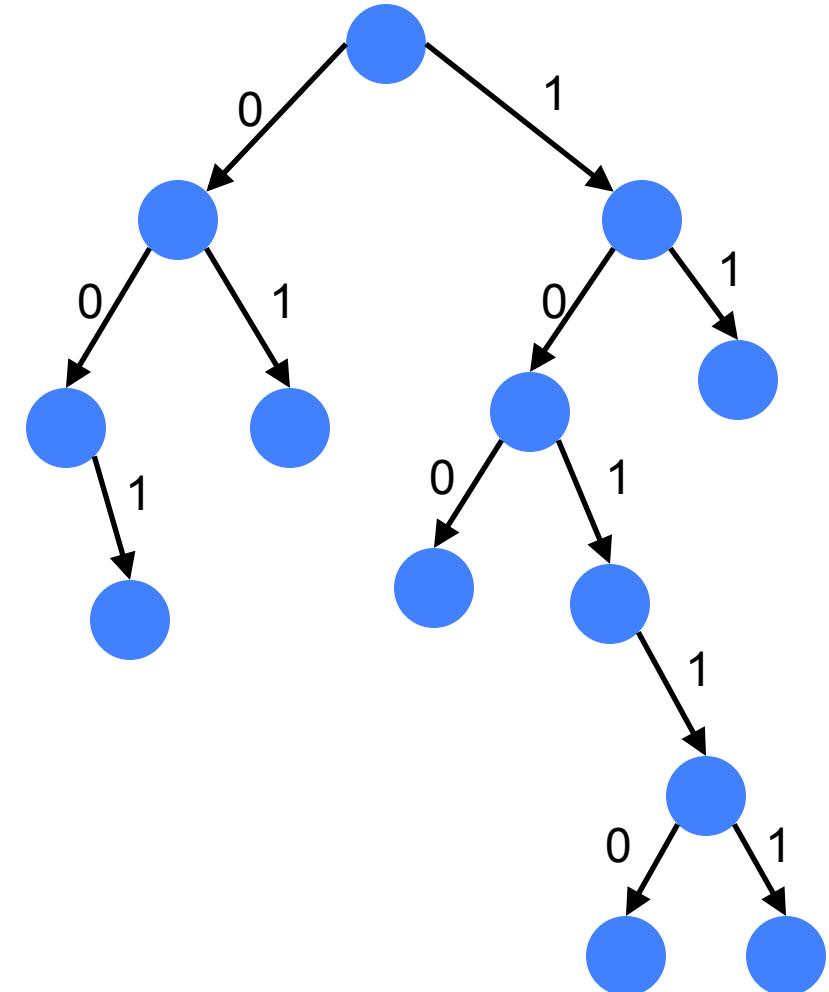
Dynamic Symbolic Execution (concolic testing)

What is Symbolic Execution? What is it good for?



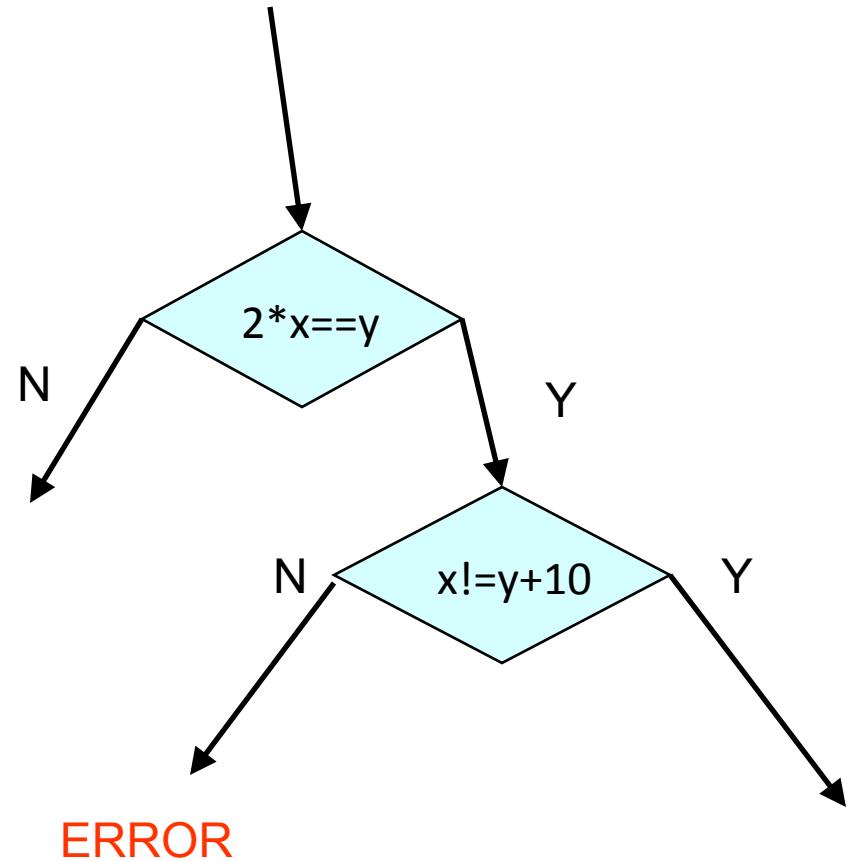
Symbolic Execution: Motivation

- Execution paths of a program can be seen as a **binary tree** with possibly infinite depth
 - **Computation tree**
- Each **node** represents the execution of a **“if then else”** statement
- Each **edge** represents the execution of a sequence of non-conditional statements
- Each path in the tree represents an equivalence class of inputs



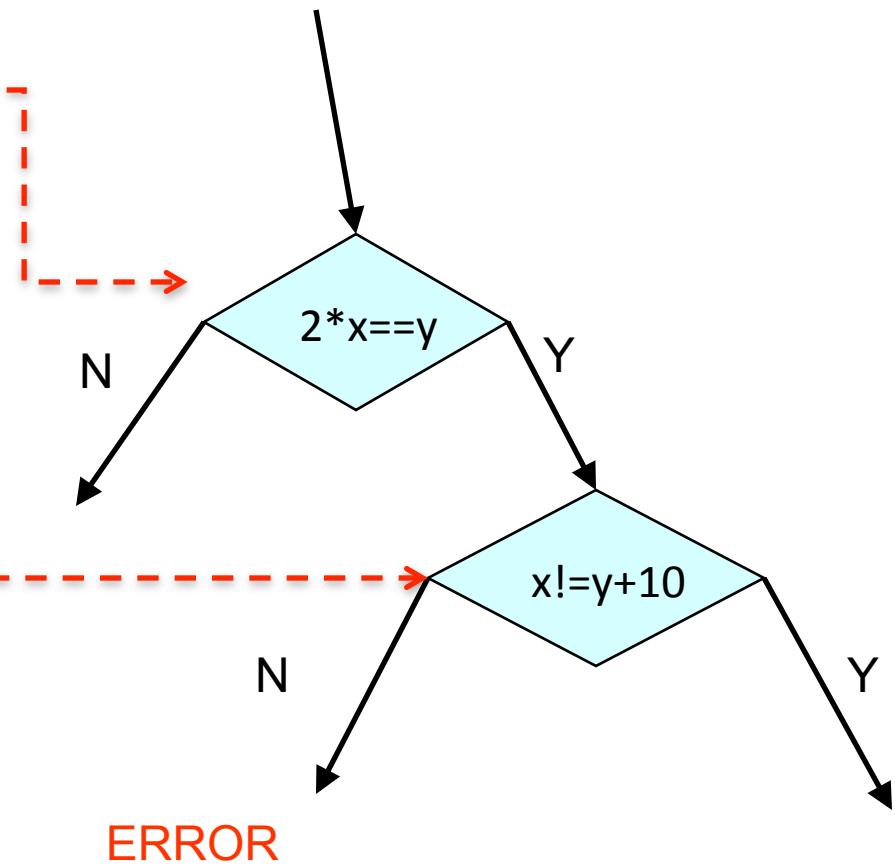
Example of Computation Tree

```
void test_me(int x, int y) {  
    if(2*x==y) {  
        if(x != y+10) {  
            printf("I am fine here");  
        } else {  
            printf("I should not reach here");  
            ERROR;  
        }  
    }  
}
```

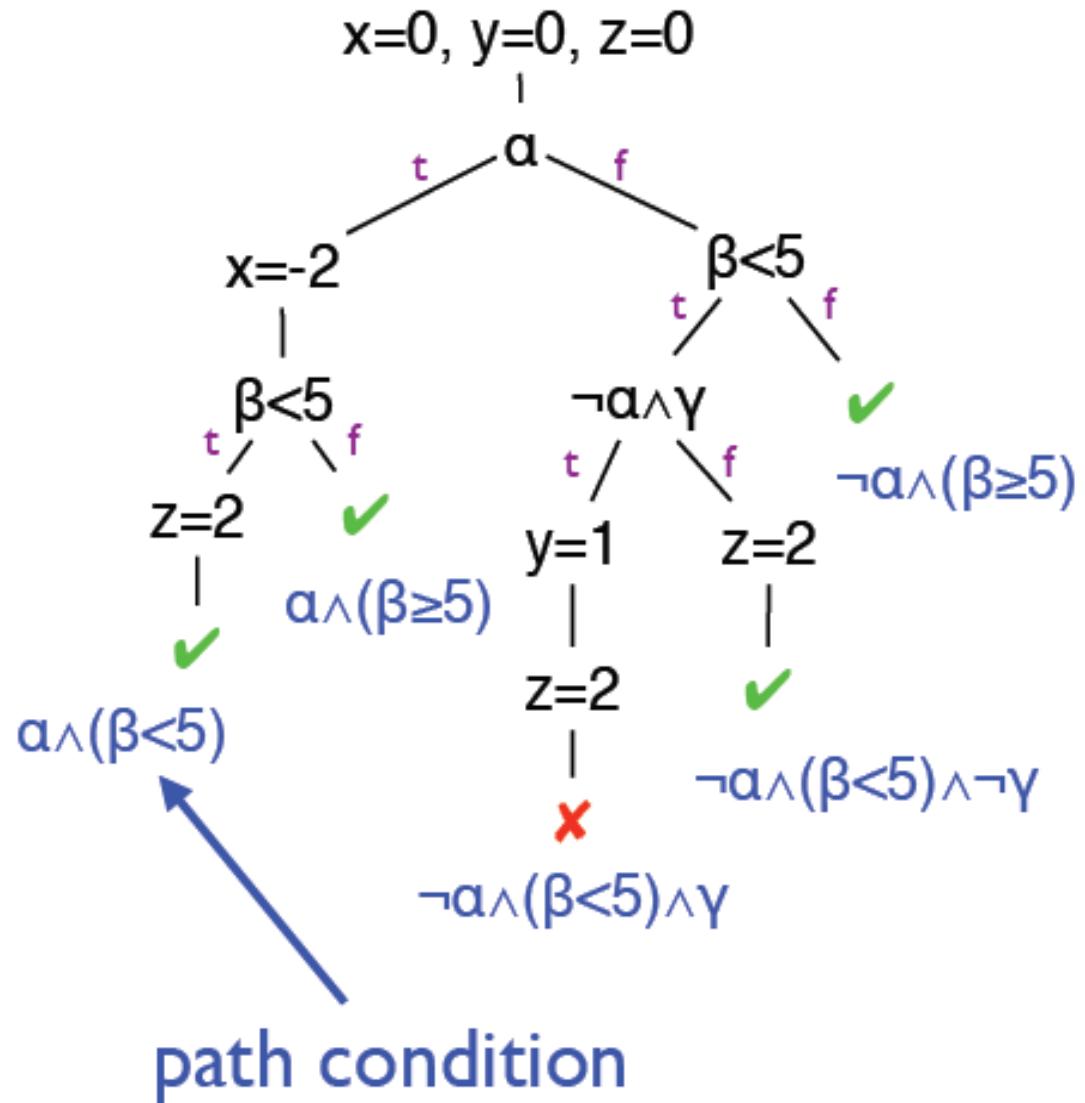


Example of Computation Tree

```
void test_me(int x, int y) {  
    if(2*x==y){  
        if(x != y+10){  
            printf("I am fine here");  
        } else {  
            printf("I should not reach here");  
            ERROR;  
        }  
    }  
}
```



```
int x = 0, y = 0, z = 0;  
if (a) {  
    x = -2;  
}  
if (b < 5) {  
    if (!a && c) { y = 1; }  
    z = 2;  
}  
assert(x+y+z != 3);
```



Symbolic Execution: Limitations?

- Sym-ex is computationally infeasible for many programs
 - Tries to find every execution path, which is exponential in the number of branches.
 - Does not **scale** for large programs.

Symbolic Execution: Limitations

```
void again_test_me(int x,int y){  
    z = x*x*x + 3*x*x + 9;  
    if(z != y){  
        printf("Good branch");  
    } else {  
        printf("Bad branch");  
        abort();  
    }  
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x+9$
- take then branch with constraint $x*x*x+ 3*x*x+9 \neq y$
- solve $x*x*x+ 3*x*x+9 = y$ to take else branch
- **Don't know how to solve !!**
 - **Stuck ?**

Concolic Testing

CONCRETE EXECUTION + SYMBOLIC EXECUTION

= **CONCOLIC EXECUTION**

Koushik Sen, Darko Marinov, and Gul Agha. 2005. **CUTE: a concolic unit testing engine for C**. In *Proc. International Symposium on Foundations of Software Engineering (ESEC/FSE-13)*. ACM, 263-272.

Goal

Automated Unit Testing of real-world Programs

- Generate test inputs
- Execute unit under test on generated test inputs
 - so that all reachable statements are executed
- Any generic assertion violation gets caught
 - Examples: exceptions thrown, crashes, out of memory issues, etc

Concolic Execution

- Generates **concrete inputs** one by one.
- The program is executed on that input simultaneously (both **concretely & symbolically**).
- The symb. ex. follows the path taken by the concrete ex. maintains a symb. state, generates path constraints.
- The info. collected by the concrete ex. guides symb. ex. and is used to generate inputs for the next ex.
- This process continues until all different feasible paths are executed at least once.

Concolic vs. Symbolic Execution

- Sym-ex is computationally infeasible for many programs
 - Tries to find every execution path, which is exponential in the number of branches.
- Concolic tries to reduce the number of paths and also addresses problems with constraint solver
 - If constraint can't be solved, it defaults to **random values**.
 - Symbolic execution helps to generate concrete inputs for next execution.

Concolic Testing Example

```
int double (int v) {  
    return 2*v;  
}  
  
void testme (int x, int y) {  
    z = double (y);  
    if (z == x) {  
        if (x > y+10) {  
            ERROR;  
        }  
    }  
}
```

- Random Test Driver:
 - random values for x and y
- Probability of reaching **ERROR** is extremely low

Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

$x = 22, y = 7$

Symbolic
Execution

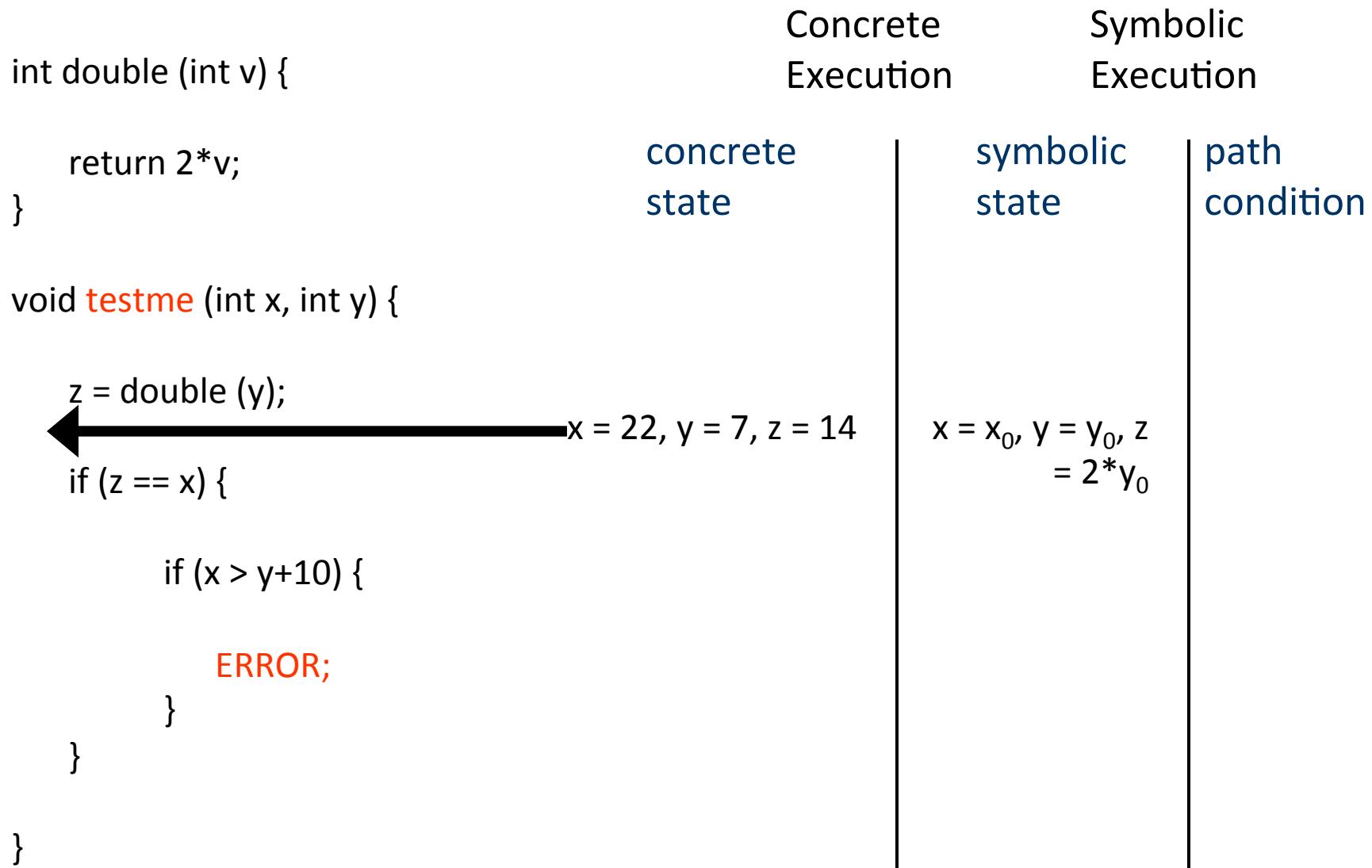
symbolic
state

$x = x_0, y = y_0$

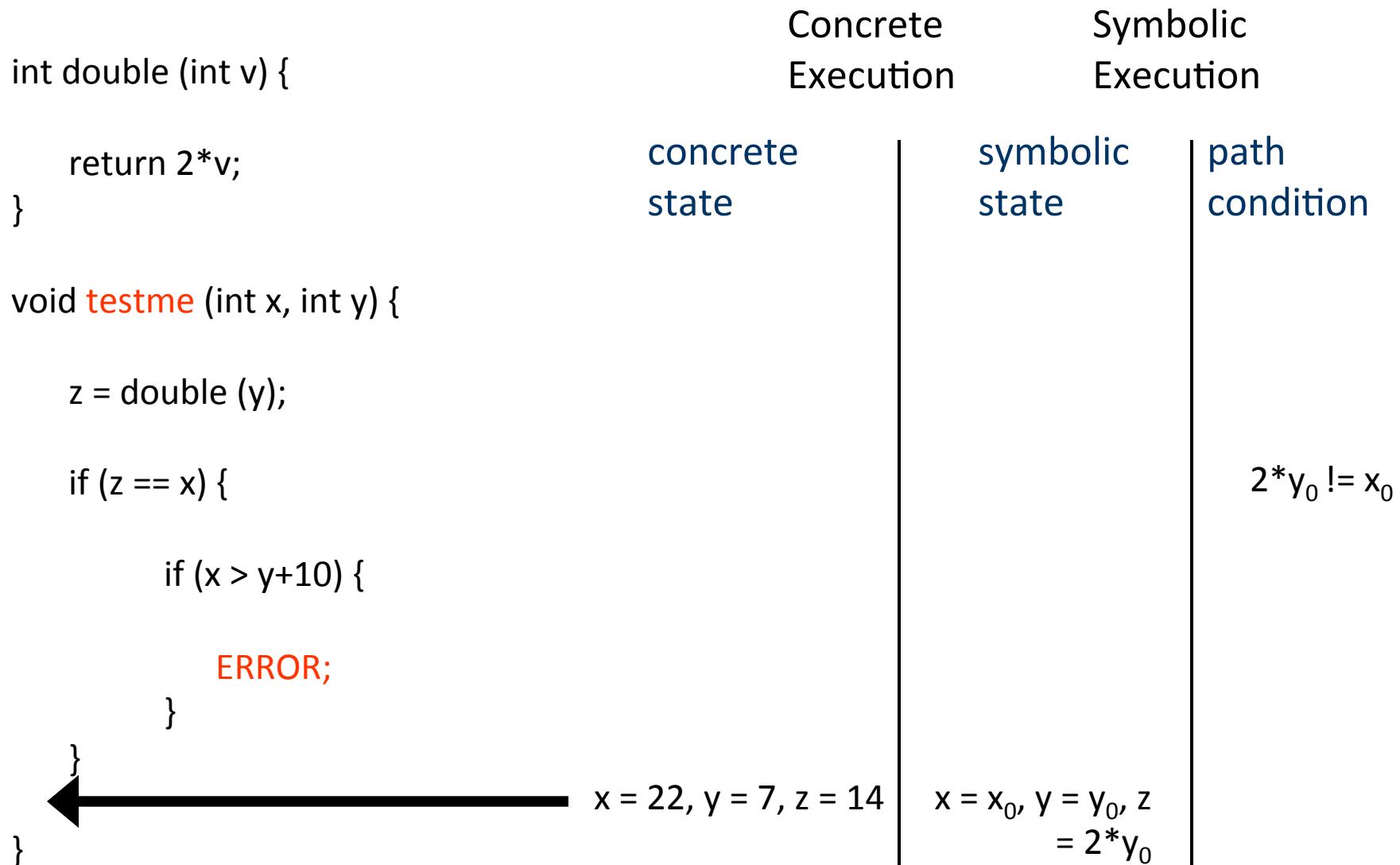
path
condition



Concolic Testing Approach



Concolic Testing Approach



Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
```

```
void testme (int x, int y) {  
    z = double (y);  
  
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

path
condition

Solve: $2*y_0 == x_0$

Solution: $x_0 = 2, y_0 = 1$

$2*y_0 != x_0$

$x = 22, y = 7, z = 14$

$x = x_0, y = y_0, z = 2*y_0$

Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

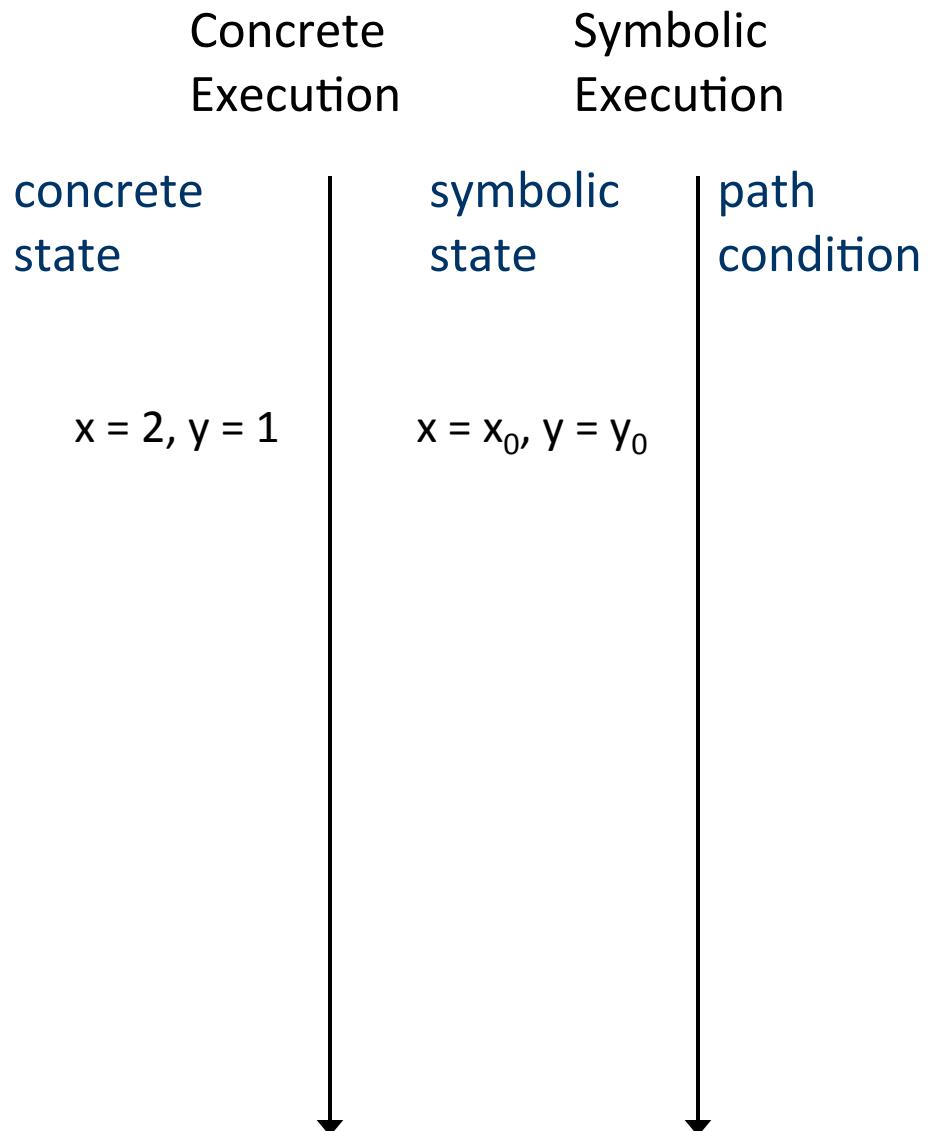
```
        if (x > y+10) {
```

```
            ERROR;
```

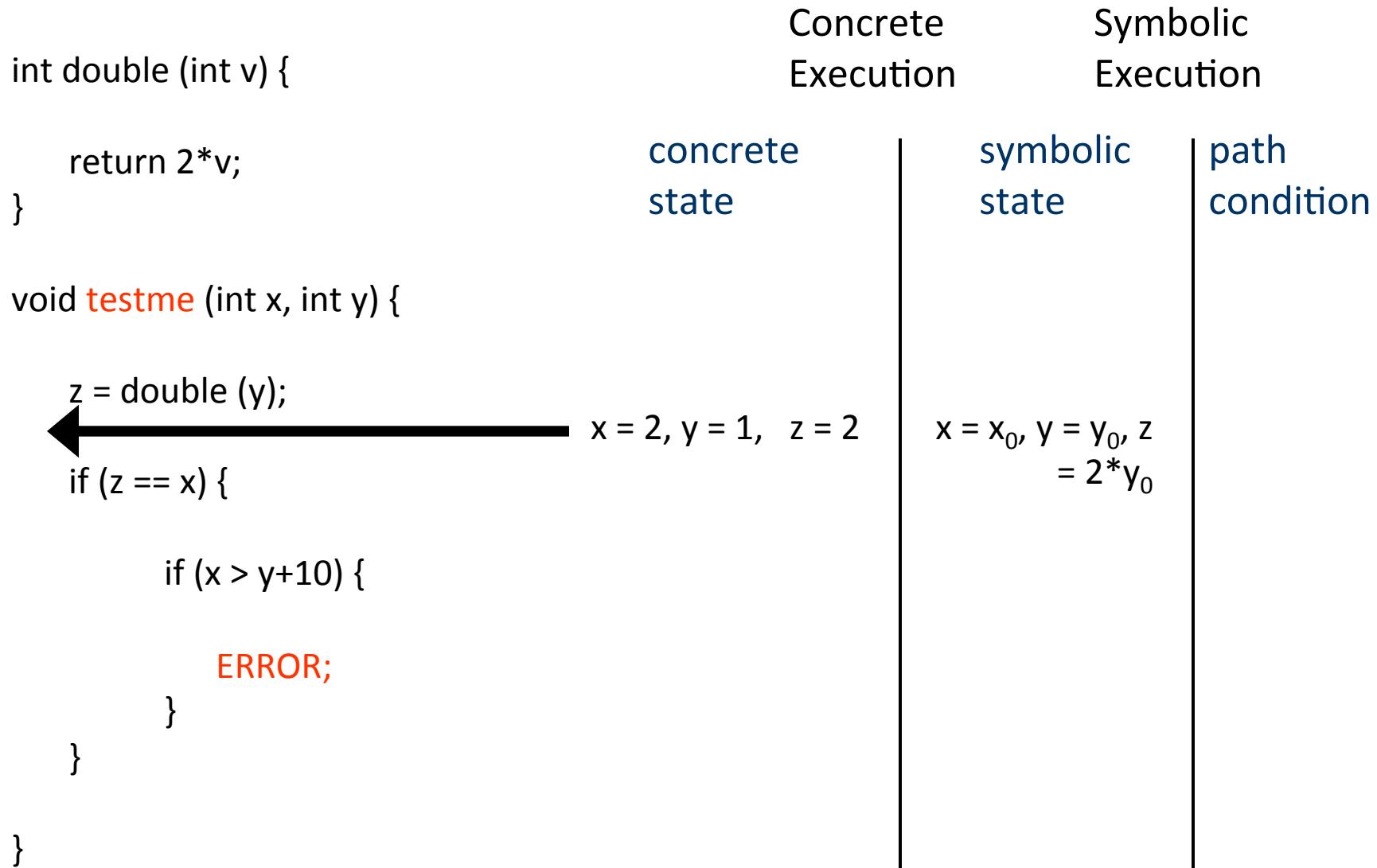
```
}
```

```
}
```

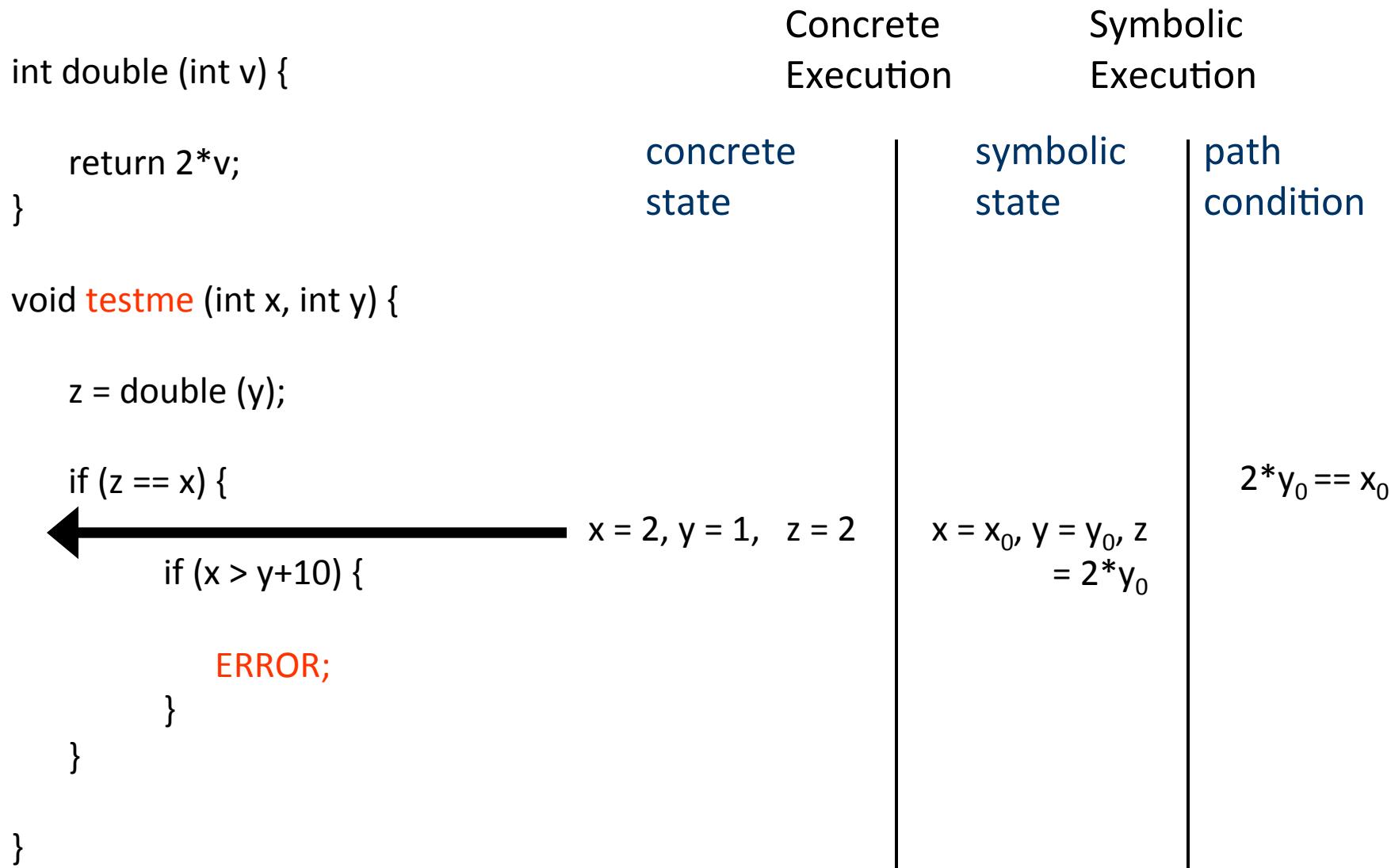
```
}
```



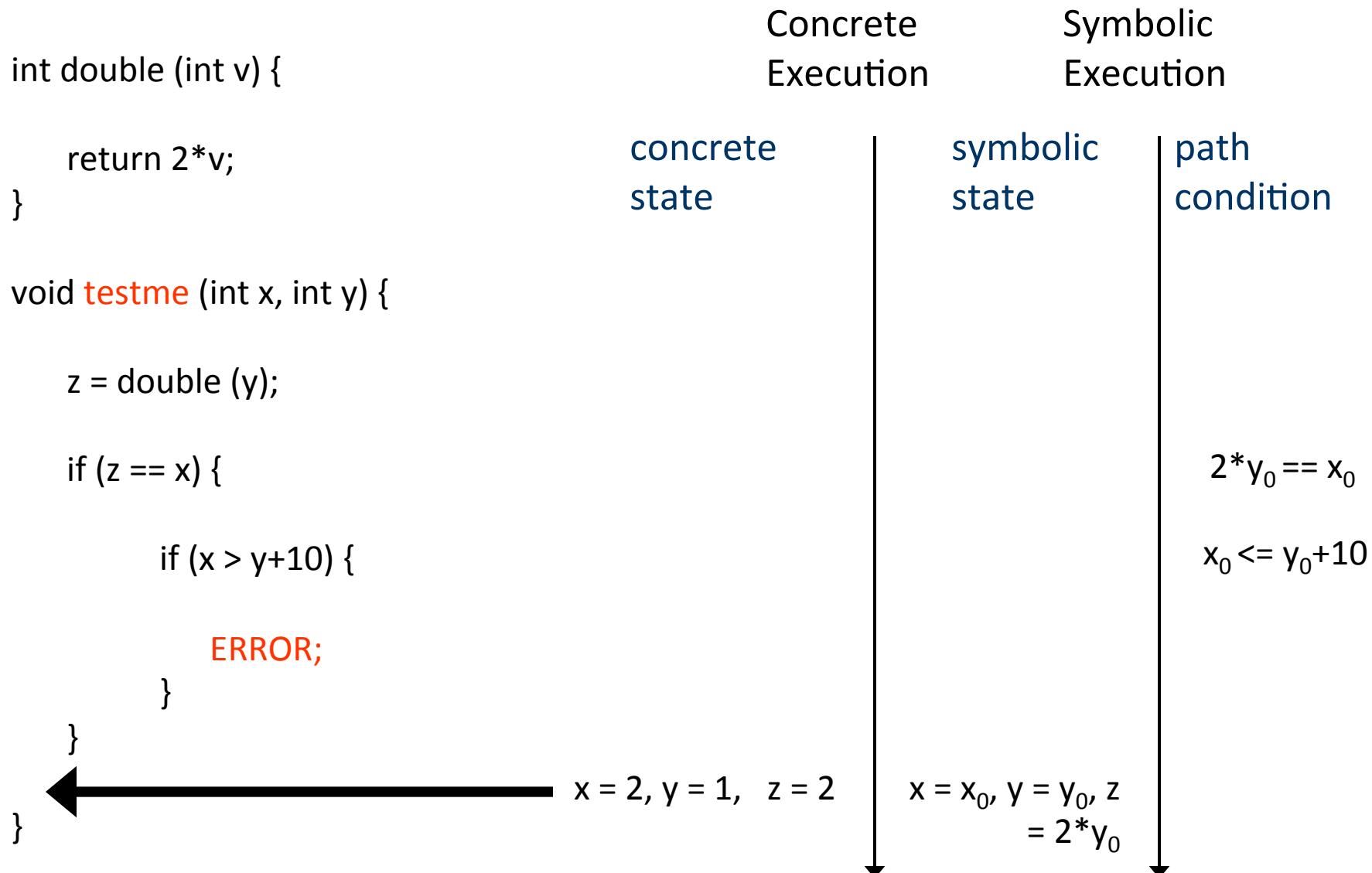
Concolic Testing Approach



Concolic Testing Approach



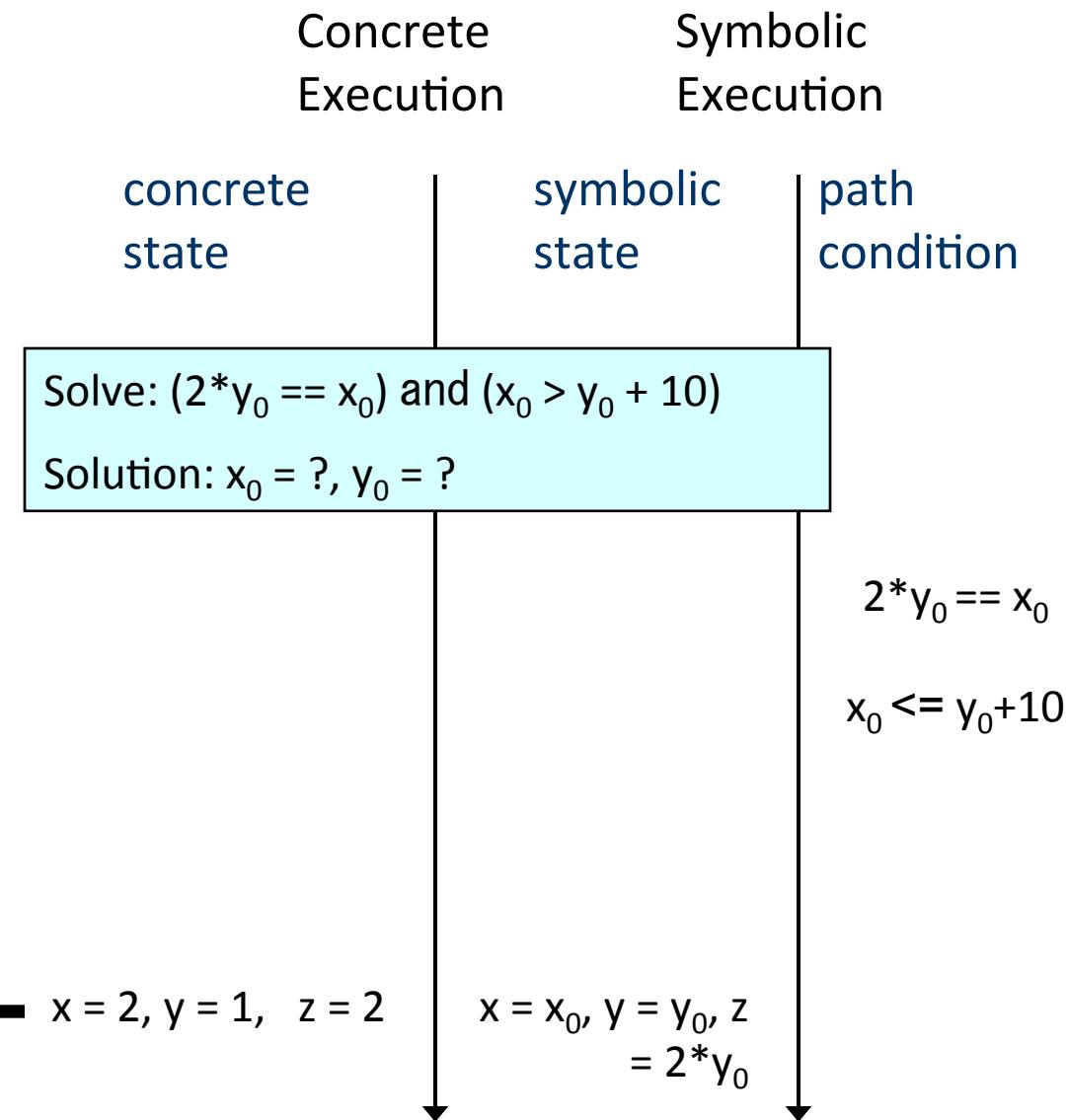
Concolic Testing Approach



Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
```

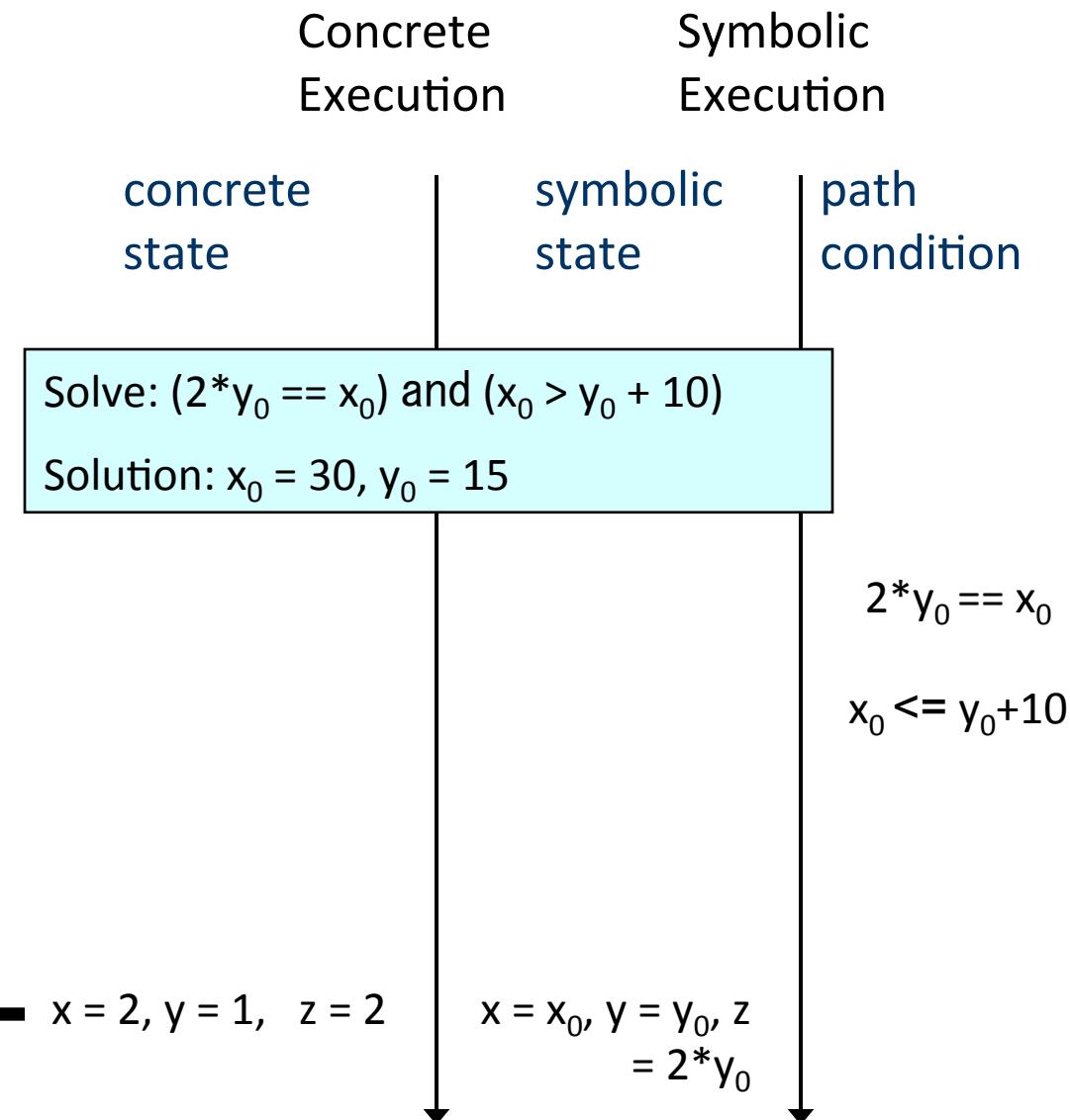
```
void testme (int x, int y) {  
    z = double (y);  
  
    if (z == x) {  
  
        if (x > y+10) {  
  
            ERROR;  
        }  
    }  
}
```



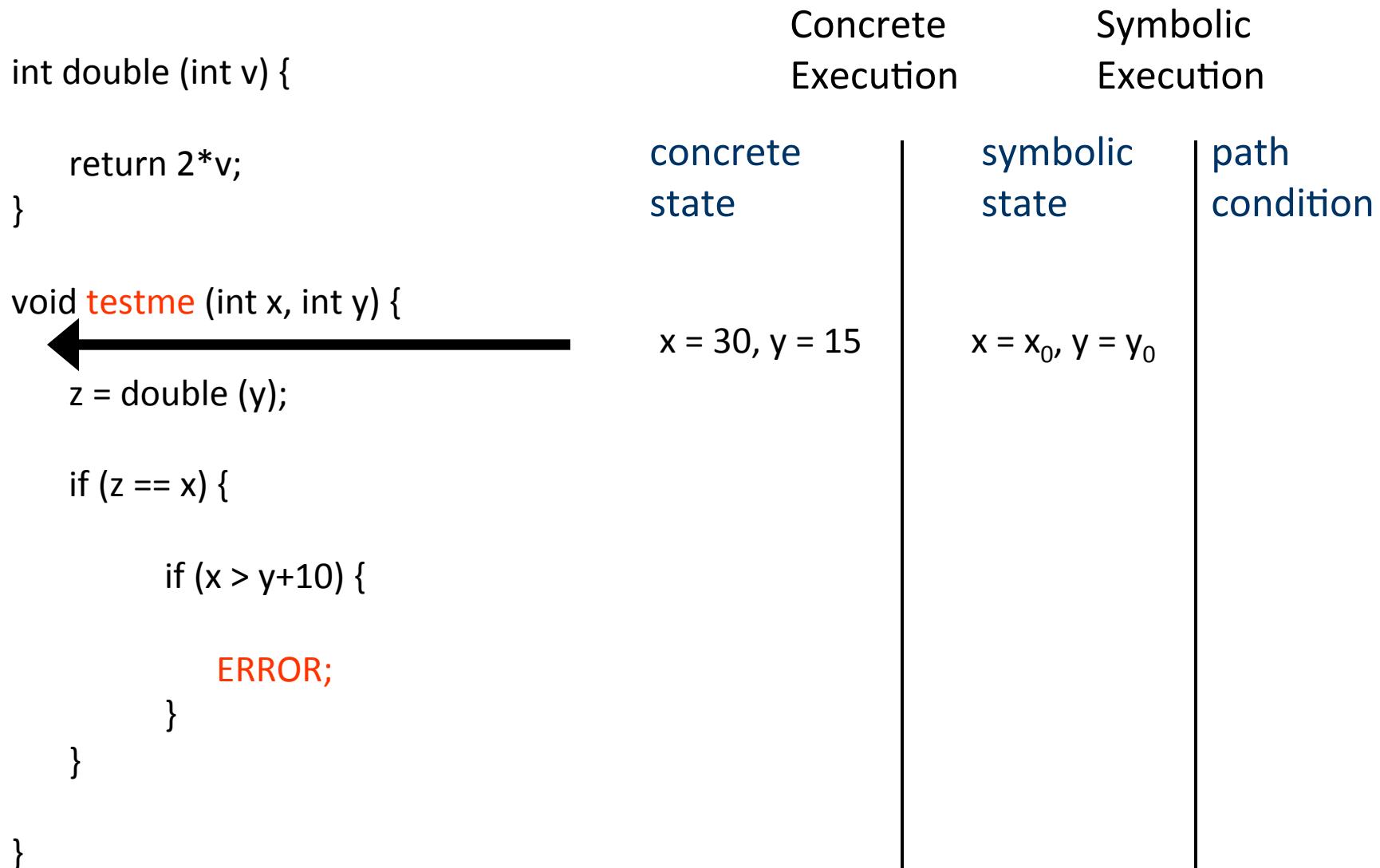
Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
```

```
void testme (int x, int y) {  
    z = double (y);  
  
    if (z == x) {  
  
        if (x > y+10) {  
  
            ERROR;  
        }  
    }  
}
```



Concolic Testing Approach



Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

Concrete
Execution

Symbolic
Execution

path
condition

concrete

symbolic
state

Program Error

$x = 30, y = 15$

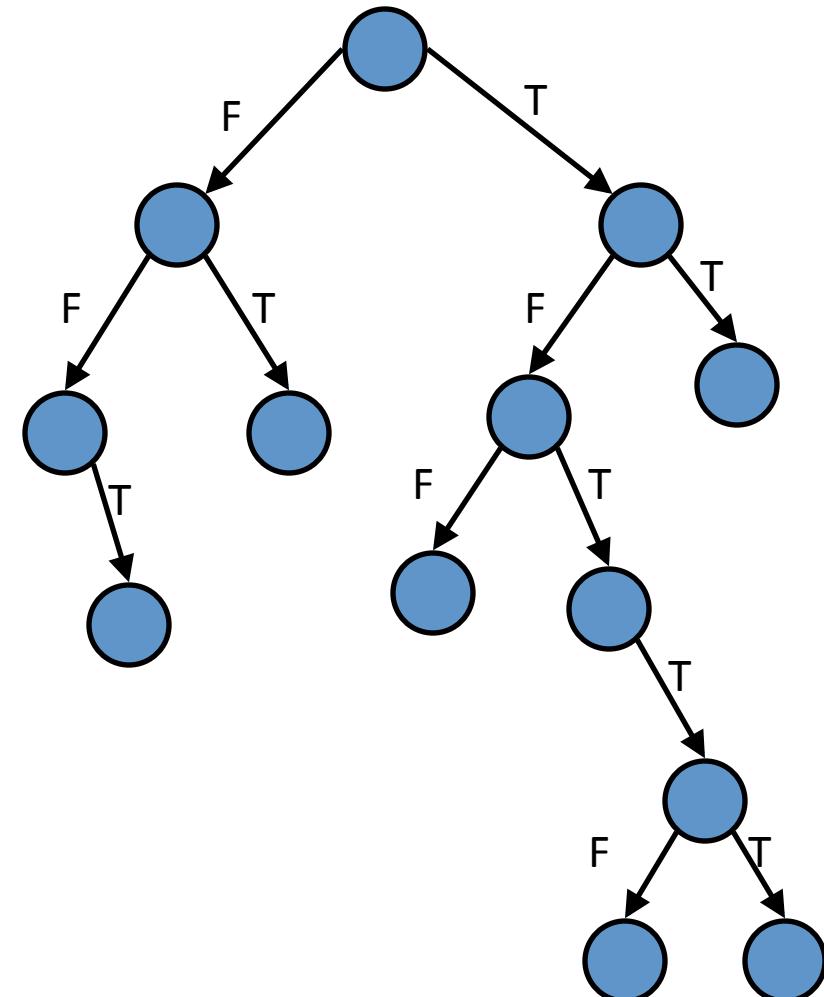
$x = x_0, y = y_0$

$2 * y_0 == x_0$

$x_0 > y_0 + 10$

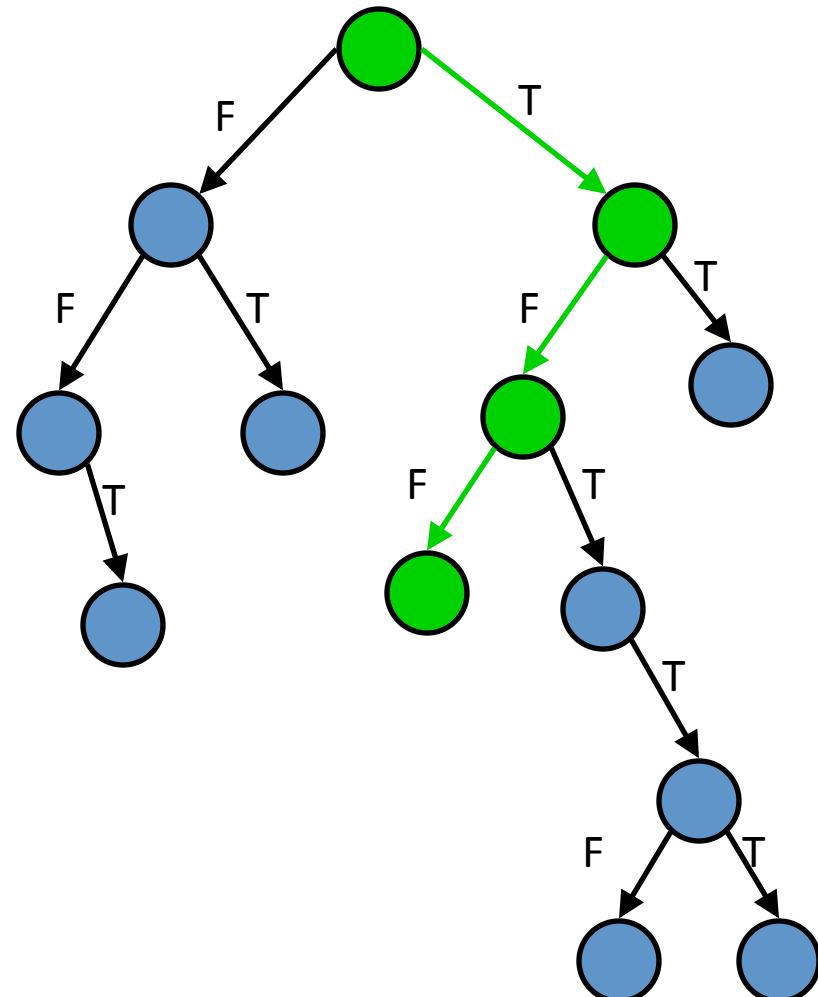
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions



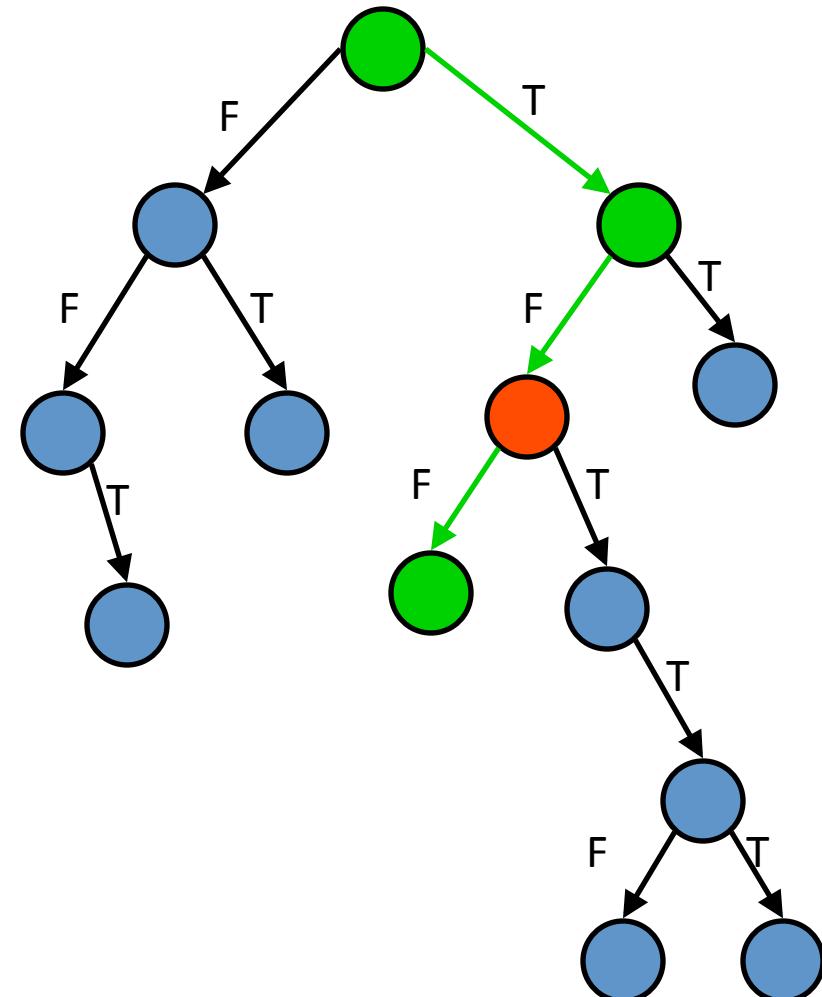
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions



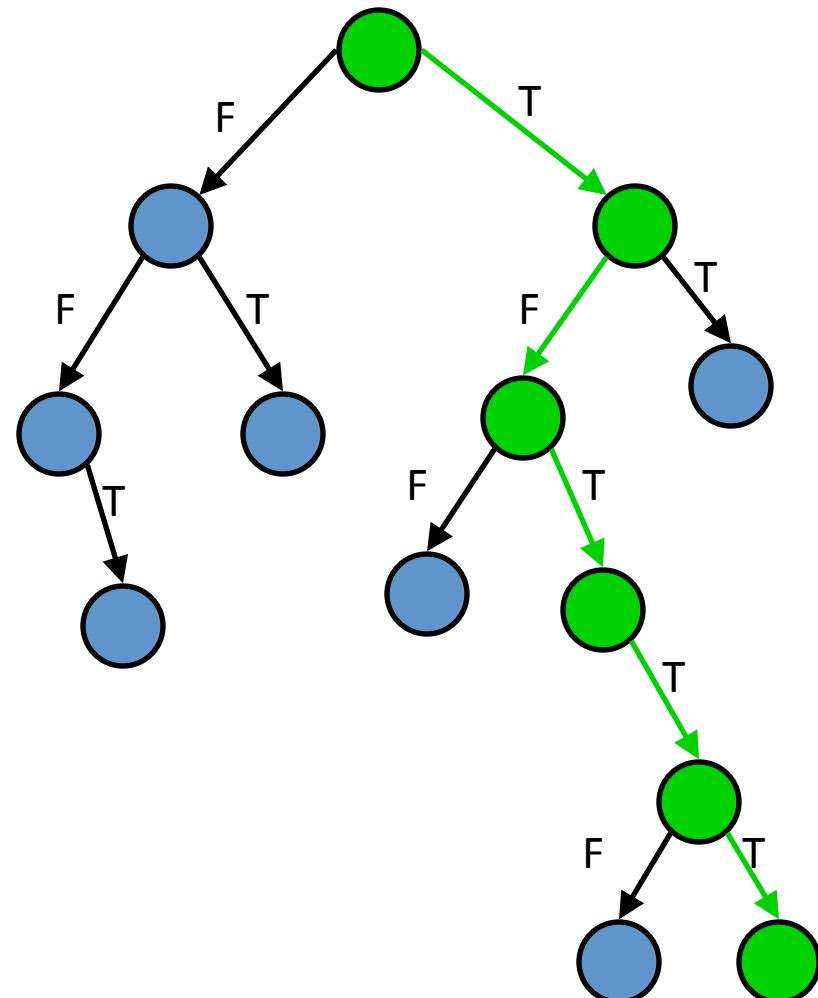
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions



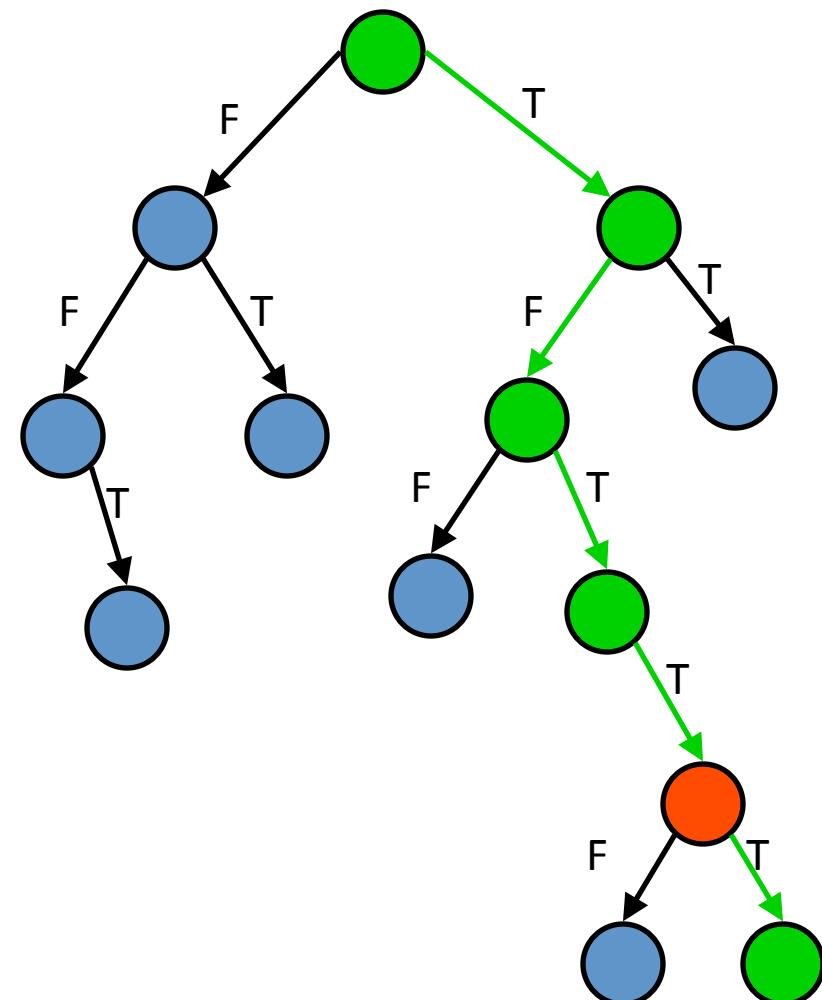
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
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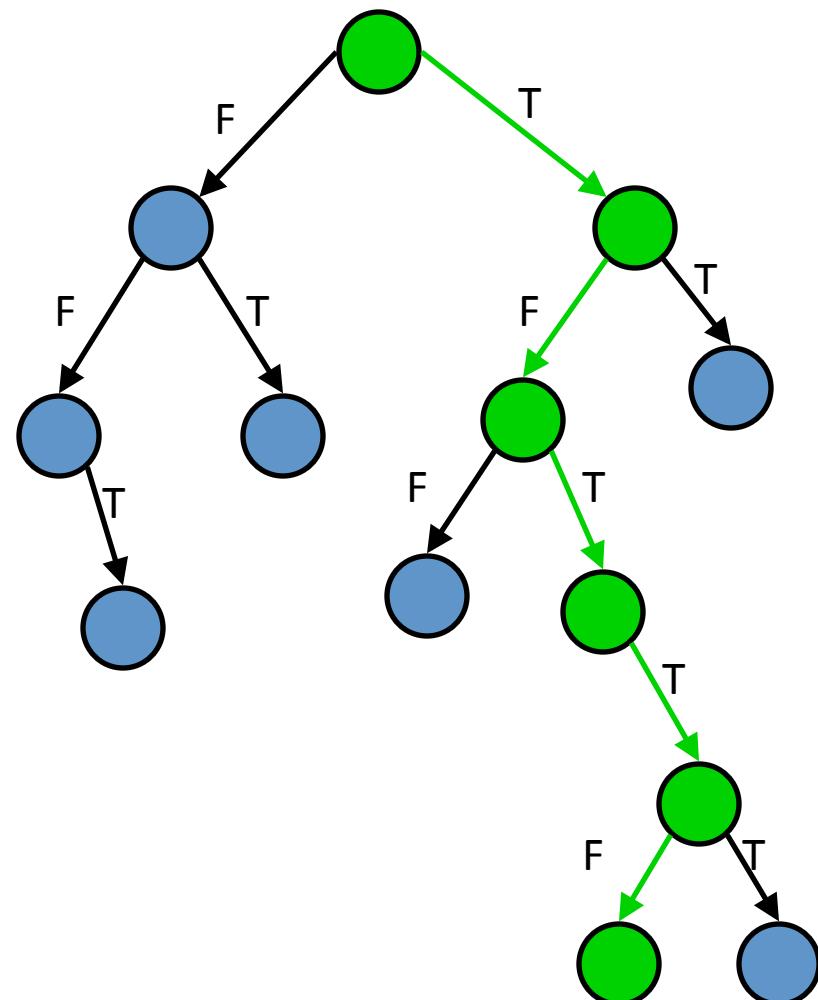
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions



Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions



Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x+9$
- take then branch with constraint $x*x*x+3*x*x+9 \neq y$
- solve $x*x*x+3*x*x+9 = y$ to take else branch
- Don't know how to solve !!
 - Stuck ?

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x+9$
- take then branch with constraint $x*x*x+ 3*x*x+9 \neq y$
- solve $x*x*x+ 3*x*x+9 = y$ to take else branch
- Don't know how to solve !!
 - Stuck ?
 - NO : concolic testing handles this.

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$

Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
        printf("Good branch");
    } else {
        printf("Bad branch");
        abort();
    }
}
```

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$
- solve $9 = y$ to take else branch
- execute next run with $x = -3$ and $y = 9$
 - got error (reaches abort)

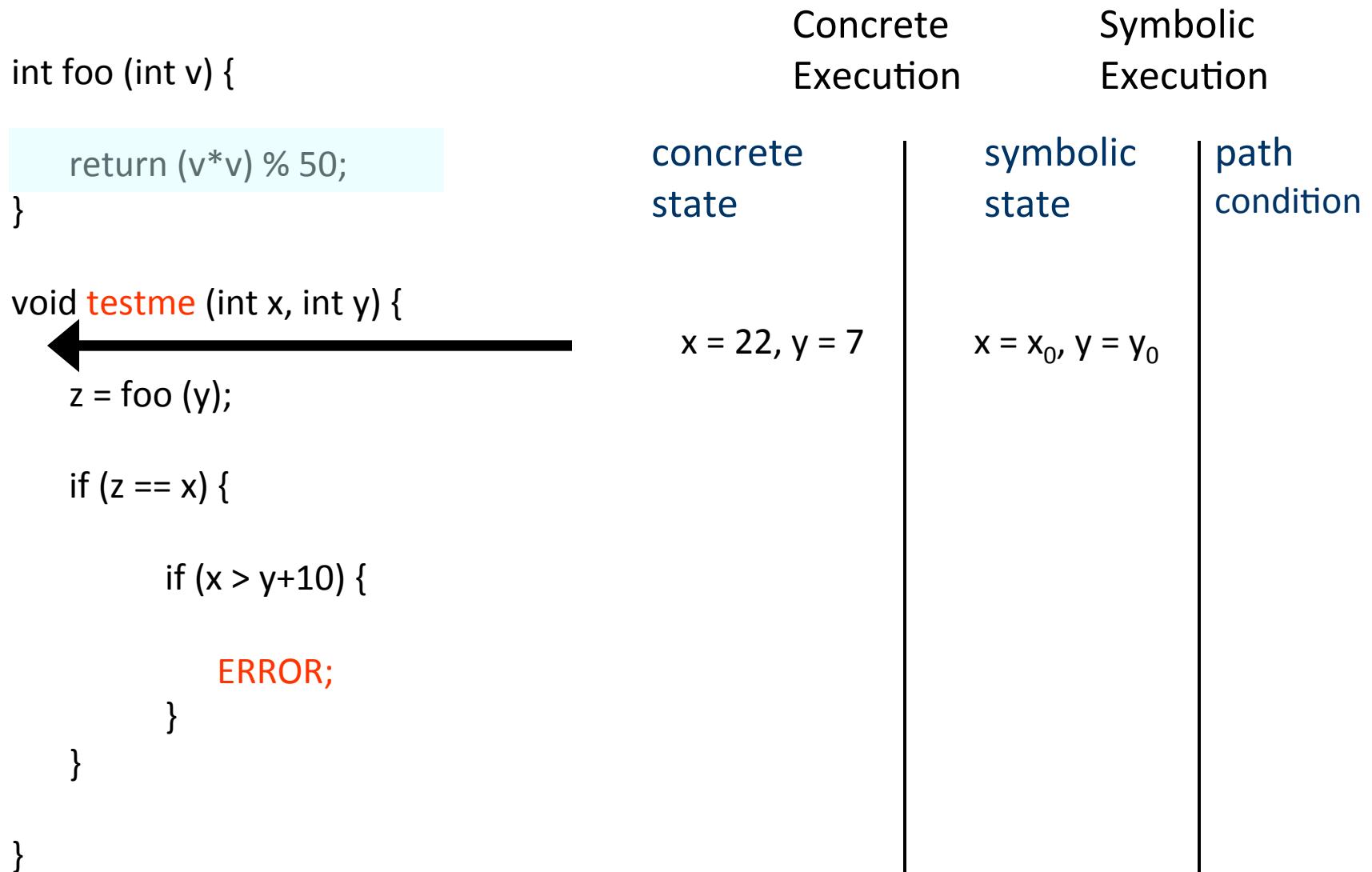
Simultaneous Symbolic & Concrete Execution

```
void again_test_me(int x,int y)
{
    z = x*x*x + 3*x*x + 9;
    if(z != y){
    }
}
```

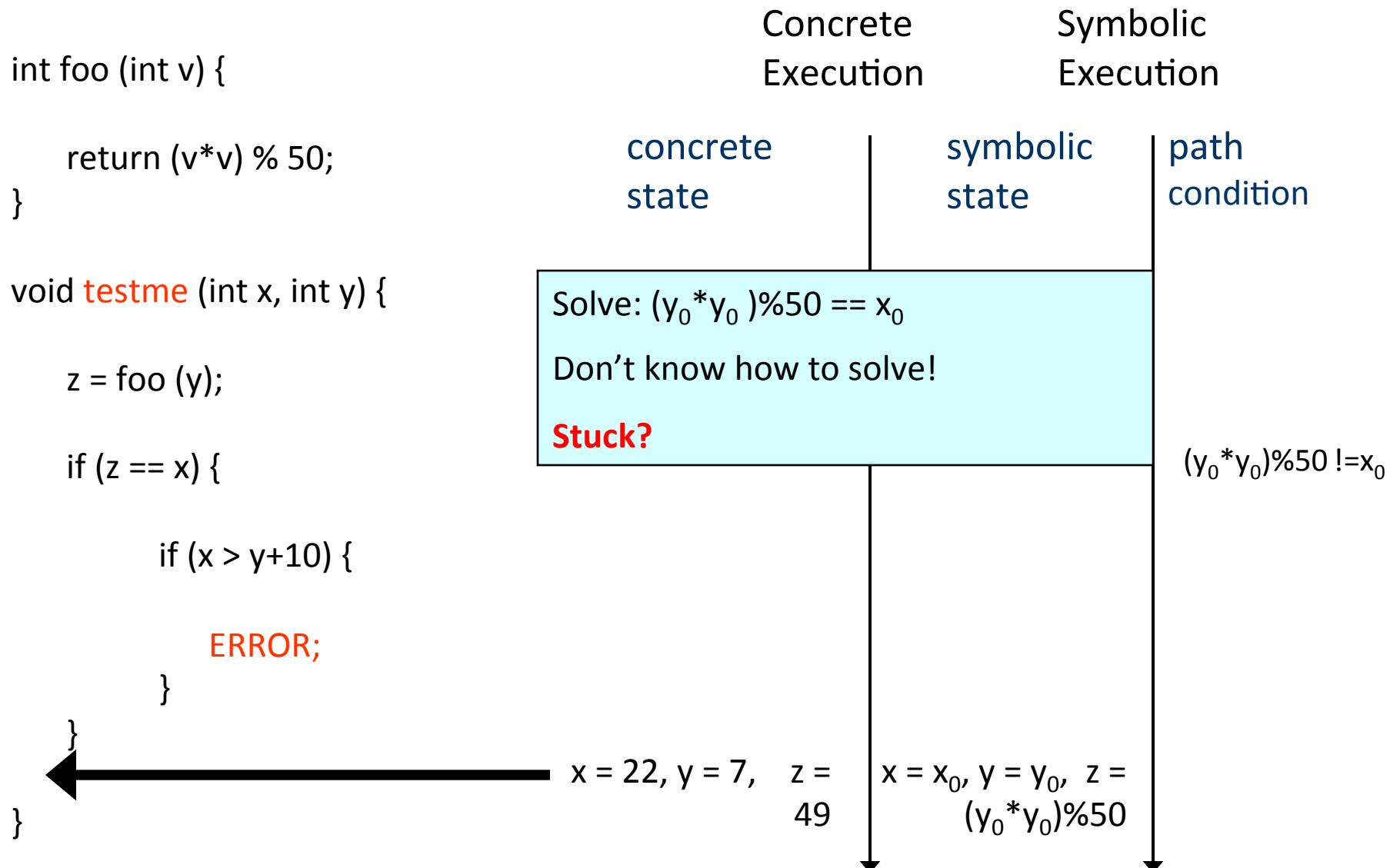
Replace symbolic expression by concrete value when symbolic expression becomes unmanageable (i.e. non-linear)

- Let initially $x = -3$ and $y = 7$ generated by random test-driver
- concrete $z = 9$
- symbolic $z = x*x*x + 3*x*x + 9$
 - cannot handle symbolic value of z
 - make symbolic $z = 9$ and proceed
- take then branch with constraint $9 \neq y$
- solve $9 = y$ to take else branch
- execute next run with $x = -3$ and $y = 9$
 - got error (reaches abort)

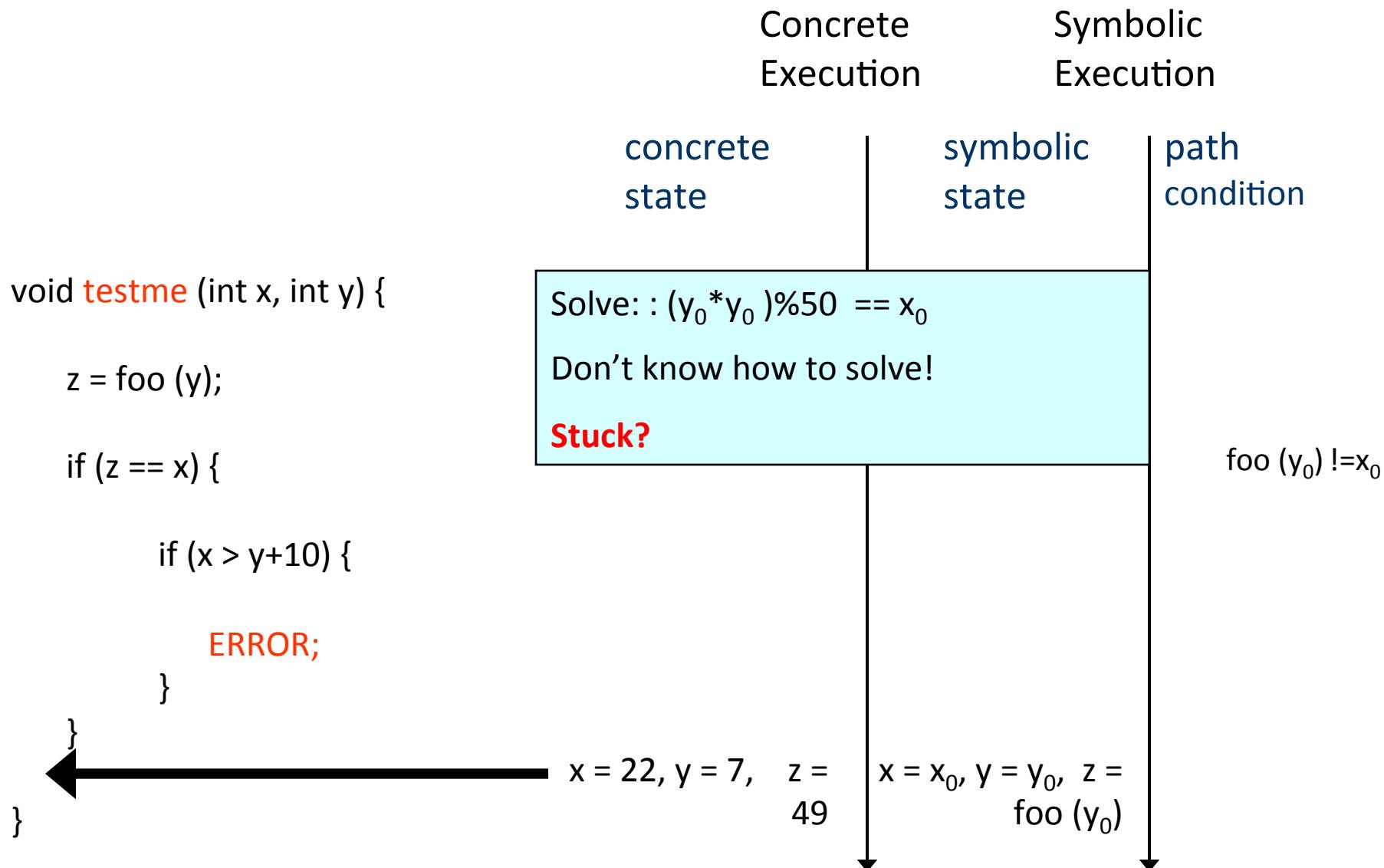
Novelty: Simultaneous Concrete and Symbolic Execution



Novelty: Simultaneous Concrete and Symbolic Execution



Novelty: Simultaneous Concrete and Symbolic Execution



Novelty: Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

path
condition

Solve: $(y_0 * y_0) \% 50 == x_0$

Don't know how to solve!

Not Stuck!

Use concrete state

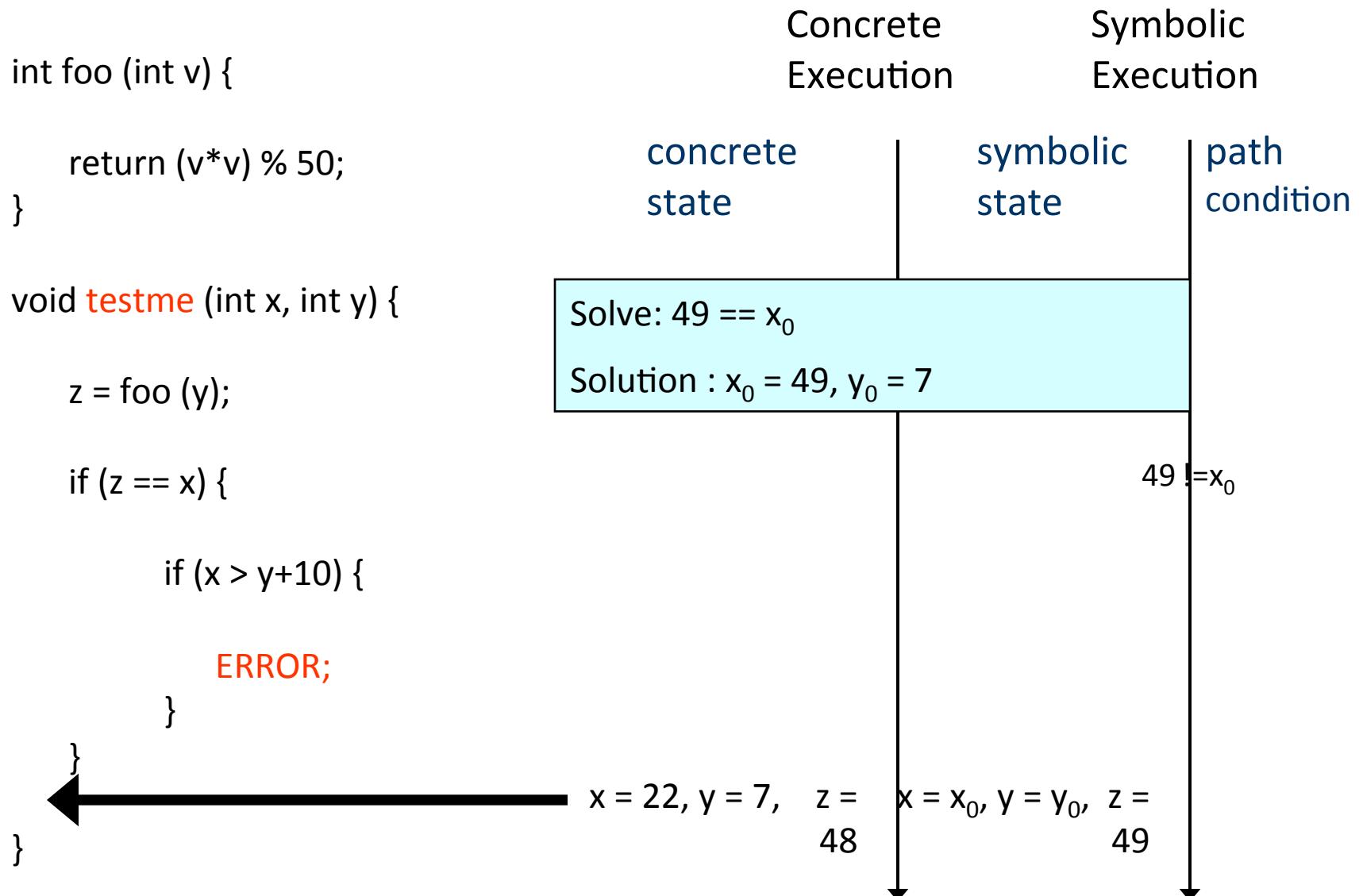
Replace y_0 by 7 (sound)

$(y_0 * y_0) \% 50 != x_0$

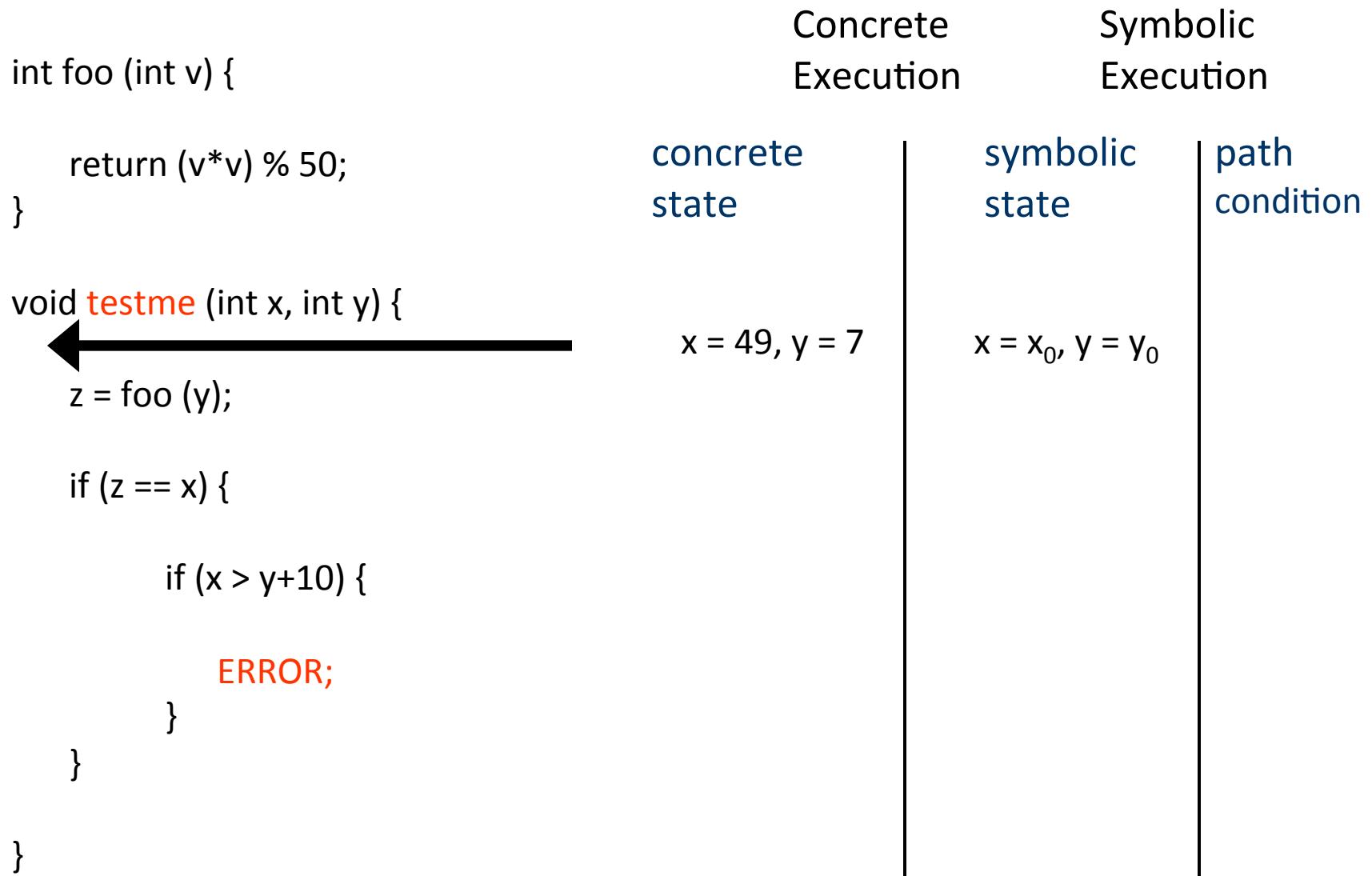
$x = 22, y = 7, z = 49$

$x = x_0, y = y_0, z = (y_0 * y_0) \% 50$

Novelty: Simultaneous Concrete and Symbolic Execution

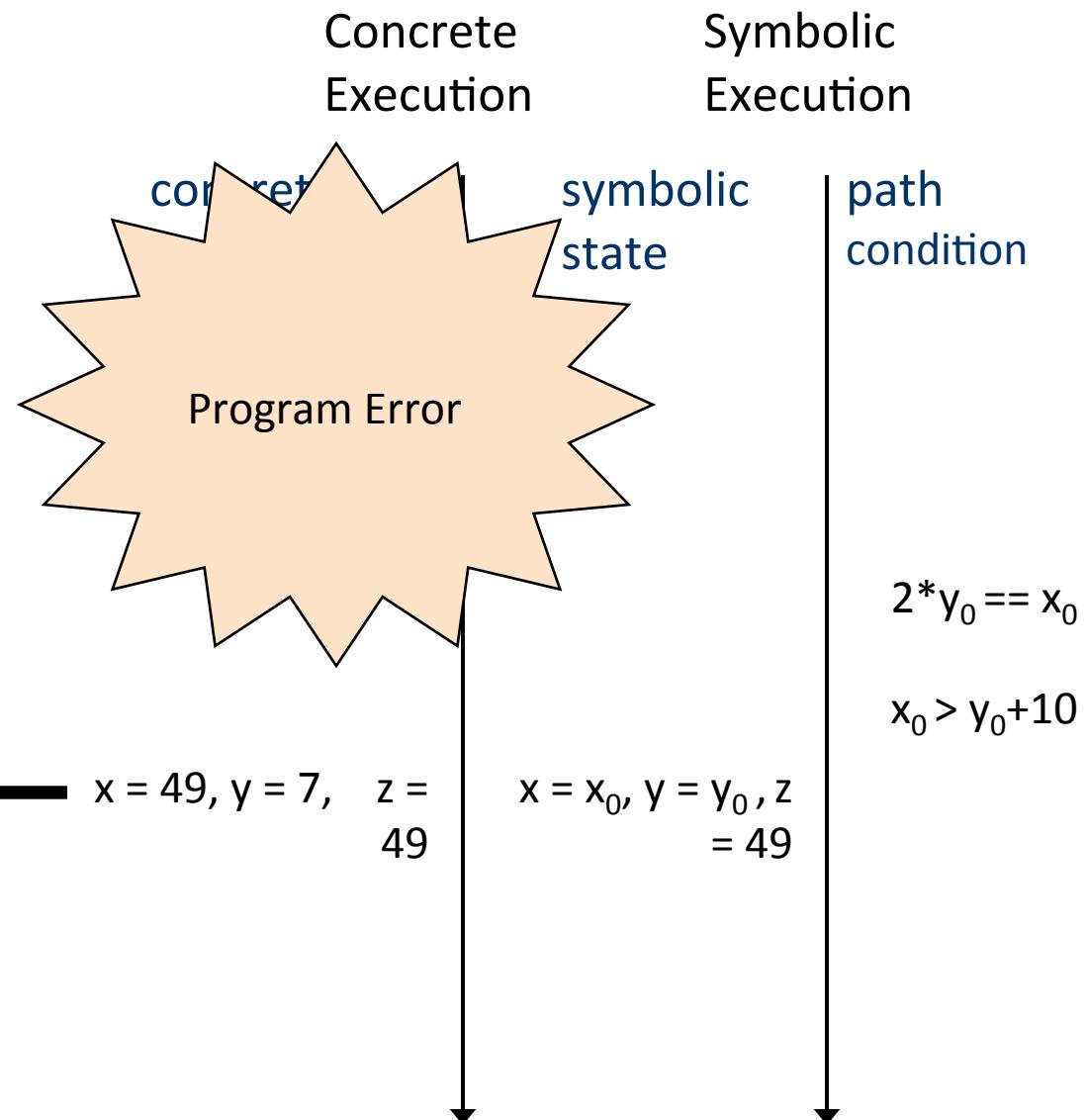


Novelty: Simultaneous Concrete and Symbolic Execution



Novelty: Simultaneous Concrete and Symbolic Execution

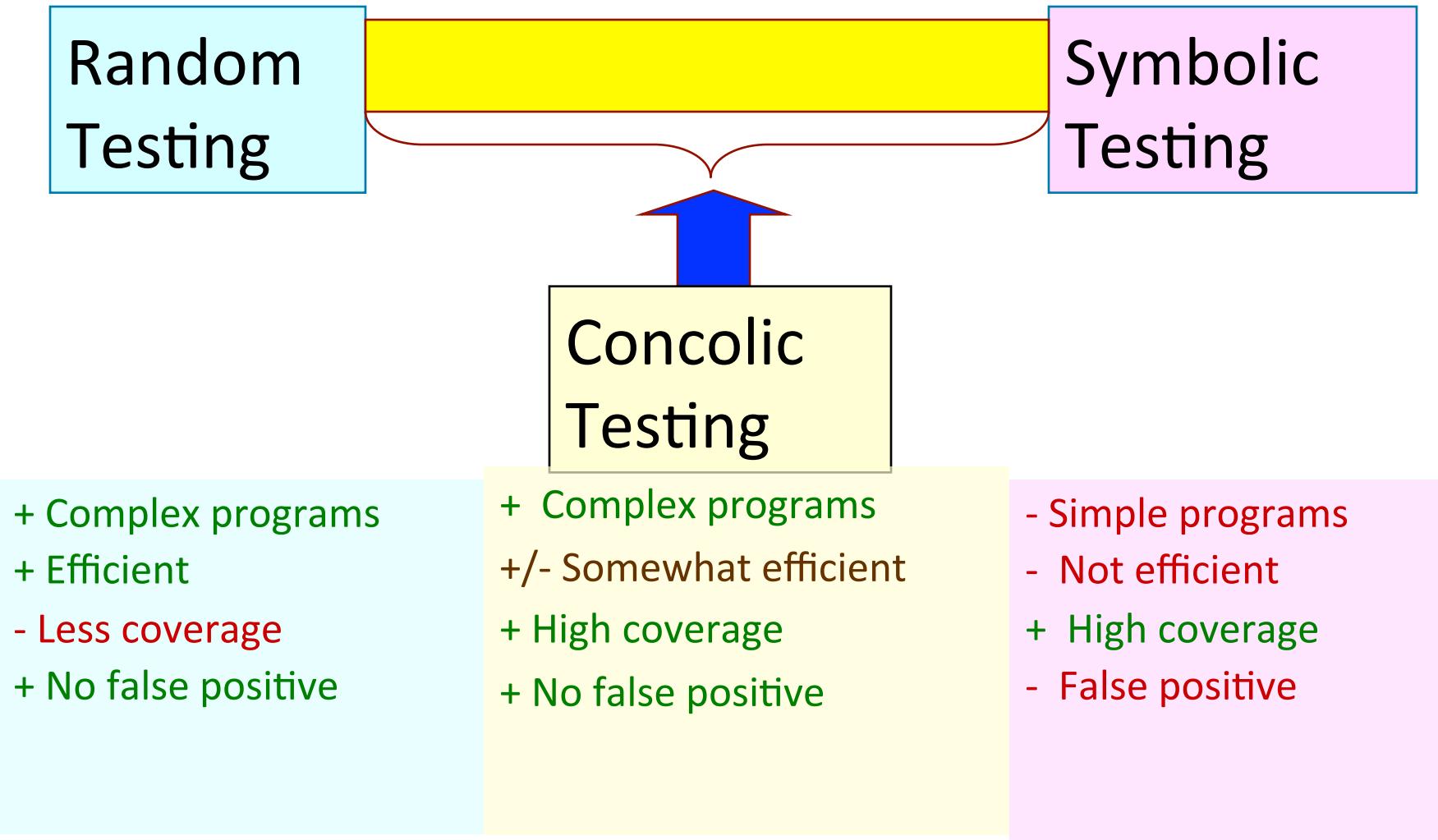
```
int foo (int v) {  
    return (v*v) % 50;  
}  
  
void testme (int x, int y) {  
    z = foo (y);  
  
    if (z == x) {  
        if (x > y+10) {  
            }  
    }  
}
```



Concolic Execution: Handling unmanageable symbolic expressions

- Concrete execution enables symbolic execution to overcome incompleteness of constraint solvers
 - replace symbolic expressions by concrete values if symbolic expressions become too complex.

Concolic Testing: A Middle Approach



Implementations

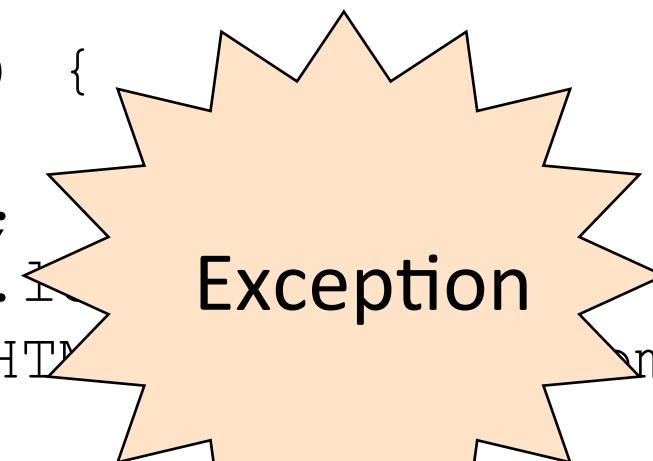
- DART and CUTE for C programs
- jCUTE for Java programs
- Microsoft has four implementations
 - SAGE, PEX, YOGI, Vigilante
- EXE (Stanford)
- JavaScript
 - Jalangi: function arguments (Berkeley)
 - ConFix: DOM interactions (SALT Lab @ UBC)

```
function sumTotalPrice() {  
    sum = 0;  
    itemList = $("items");  
    if (itemList.children.length == 0)  
        dg("message").innerHTML = "List is empty!";  
    else {  
        for(i = 0; i<itemList.children.length; i++) {  
            p = parseInt(itemList.children[i].value);  
            if (p > 0) sum += p;  
            else $("message").innerHTML += "Wrong  
                value " + i;  
        }  
        $("total").innerHTML = sum;  
    }  
    return sum;  
}  
// $ = document.getElementById
```

A test case

```
test("A test for sumTotalPrice", function() {  
  sum = sumTotalPrice();  
  //equal(sum, 170, "Function sums correctly.");  
});
```

```
function sumTotalPrice() {  
    sum = 0;  
    itemList = $("items");  
    if (itemList.children.length == 0) {  
        dg("message").innerHTML = "Empty!";  
    } else {  
        for (i = 0; i < itemList.children.length; i++) {  
            p = parseInt(itemList.children[i].value);  
            if (p > 0) sum += p;  
            else $("message").innerHTML += "Wrong  
                value " + i;  
        }  
        $("total").innerHTML = sum;  
    }  
    return sum;  
}  
// $ = document.getElementById
```



Exception

```

function sumTotalPrice() {
    sum = 0;
    itemList = $("items");
    if (itemList.children.length == 0)
        $("message").innerHTML = "List is empty!";
    else {
        for (i = 0; i < itemList.children.length; i++) {
            p = parseInt(itemList.children[i].value);
            if (p > 0) sum += p;
            else $("message").innerHTML += "Wrong value " + i;
        }
        $("total").innerHTML = sum;
    }
    return sum;
} // $ = document.getElementById

```

```

test("A test for sumTotalPrice", function() {
    sum = sumTotalPrice();
    equal(sum, 170, "Function sums correctly.");
});

```

```
<div id='qunit-fixture'>
```

```
<form id='items'>
```

```
<div id='total'>
```

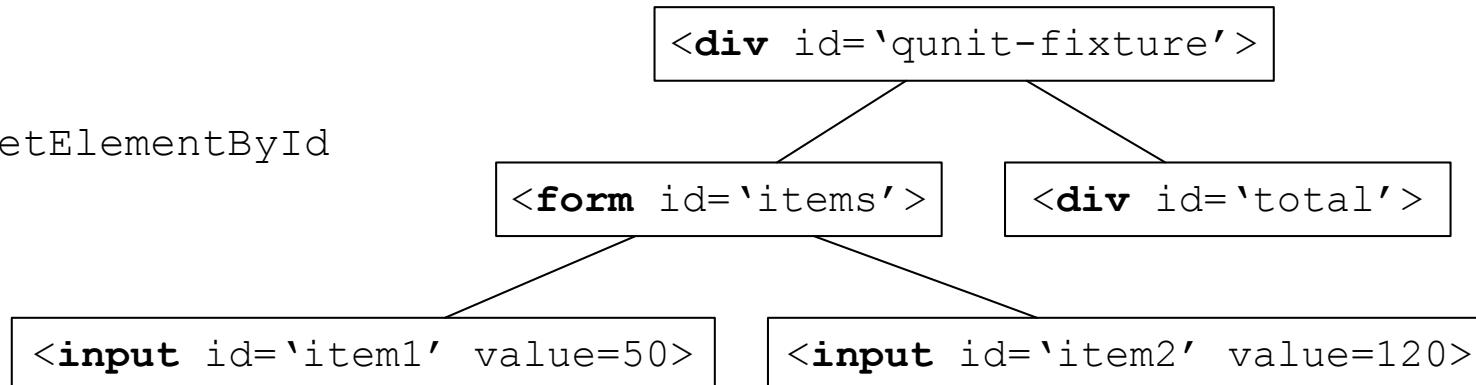
```
<input id='item1' value=50>
```

```
<input id='item2' value=120>
```

```

function sumTotalPrice() {
  sum = 0;
  itemList = $("items");
  if (itemList.children.length == 0)
    $("message").innerHTML = "List is empty!";
  else {
    for(i = 0; i<itemList.children.length; i++) {
      p = parseInt(itemList.children[i].value);
      if (p > 0) sum += p;
      else $("message").innerHTML += "Wrong value " + i;
    }
    $("total").innerHTML = sum;
  }
  return sum;
}
//$ = document.getElementById

```



Test fixture generated by ConFix

```
test("A test for sumTotalPrice", function() {  
  
  $("#qunit-fixture").append('<form id="items"><  
    input type="text" id="item1" value=50><input  
    type="text" id="item2" value=120></form><div  
    id="total"/>');  
  
  sum = sumTotalPrice();  
  equal(sum, 170, "Function sums correctly.");  
});
```

Concolic Testing in a Nutshell

- Generate concrete inputs one by one
 - each input leads program along a different path
- On each input execute program both **concretely** and **symbolically**
 - Both **cooperate** with each other
 - concrete execution **guides** the symbolic execution
 - concrete execution **enables** symbolic execution to overcome incompleteness of theorem prover
 - replace symbolic expressions by concrete values if symbolic expressions become complex
 - symbolic execution **helps to generate** concrete input for next execution
 - increases coverage

Another example: pointees

(POINTERS ARE NOT NEEDED FOR FINAL EXAM)

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

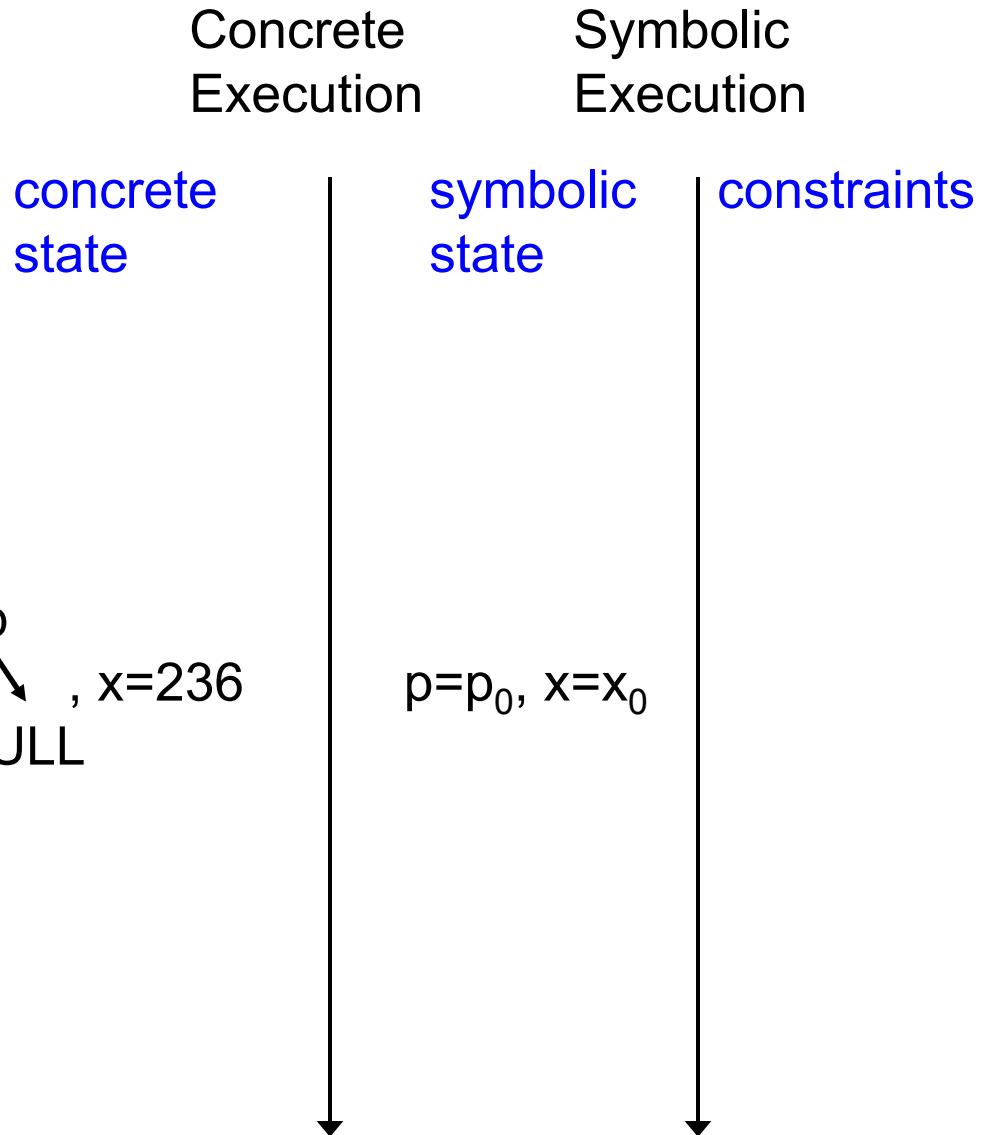
← p
, x=236
NULL

$p=p_0, x=x_0$

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

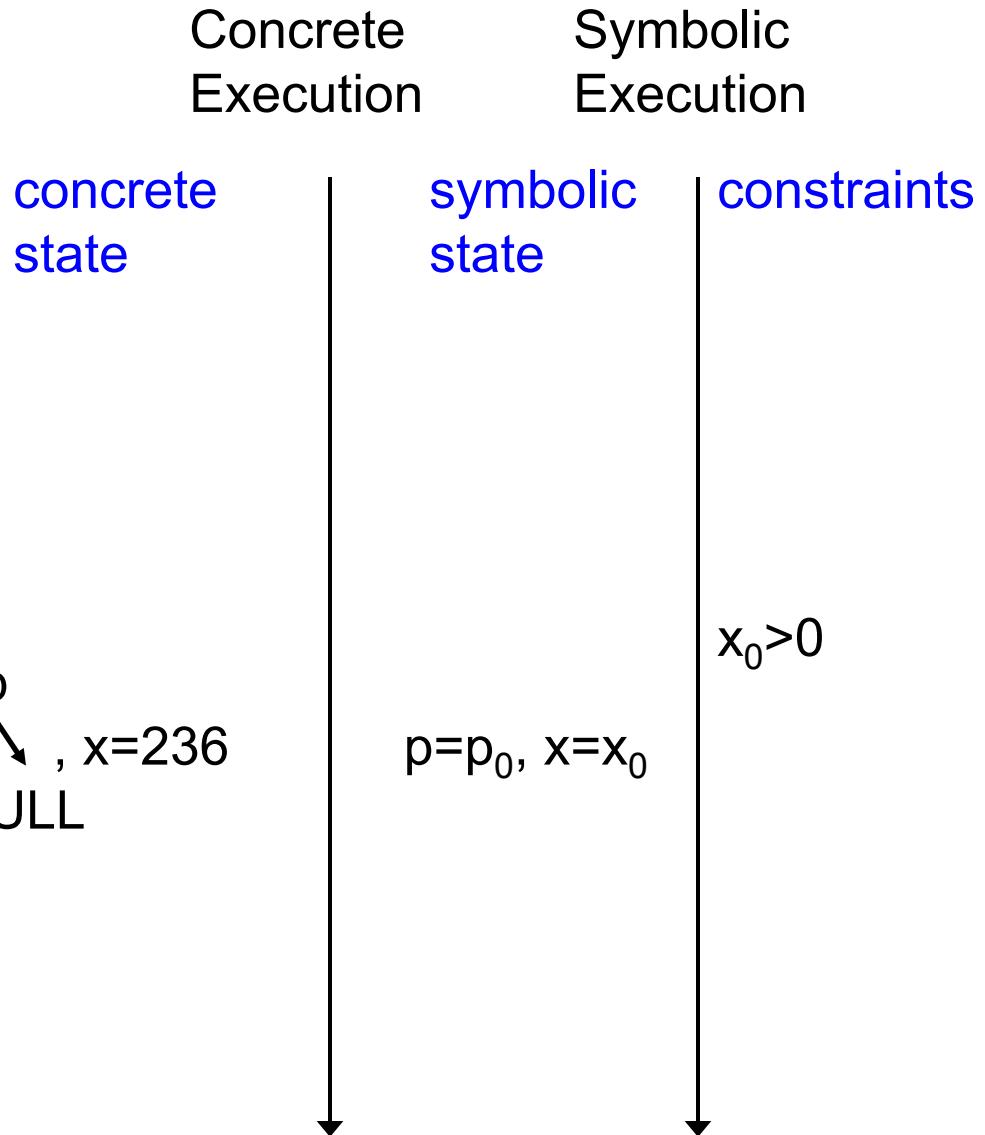
```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



p

NULL

, x=236

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

$x_0 > 0$
 $!(p_0 \neq \text{NULL})$

$p=p_0, x=x_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

concrete

symbolic

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$

$x_0 > 0$
 $p_0 = \text{NULL}$

$p \swarrow$
NULL
, $x=236$

$p=p_0$, $x=x_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

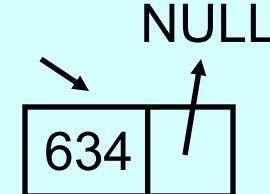
concrete

symbolic

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$

$x_0 = 236, p_0$



$x_0 > 0$
 $p_0 = \text{NULL}$

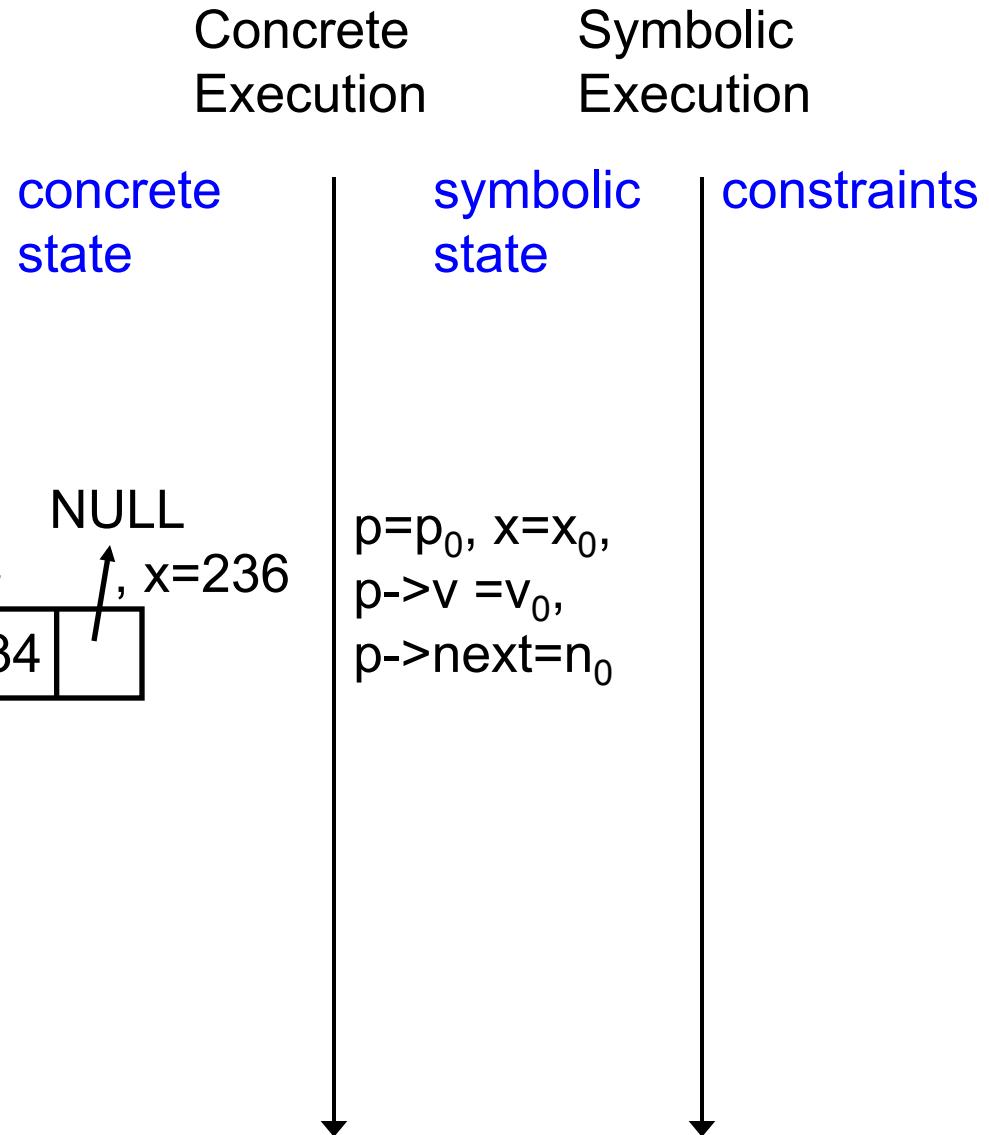
$p \rightarrow$
NULL, $x = 236$

$p = p_0, x = x_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

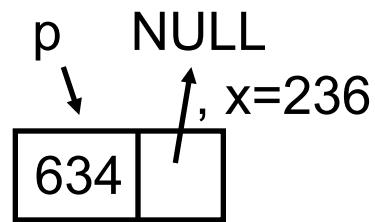
```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



Concrete Execution	Symbolic Execution
concrete state	symbolic state

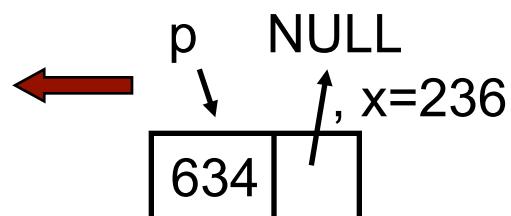
$p=p_0, x=x_0,$
 $p->v =v_0,$
 $p->next=n_0$

$x_0 > 0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



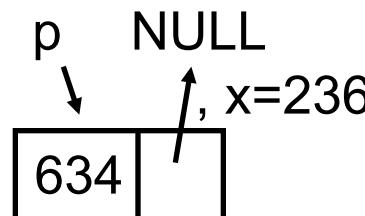
Concrete Execution	Symbolic Execution
concrete state	symbolic state
$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

←

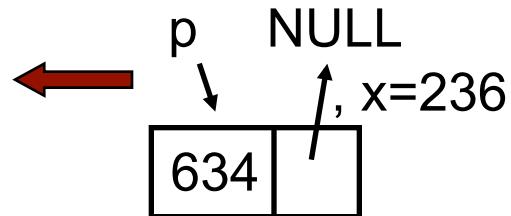


Concrete Execution	Symbolic Execution
concrete state	symbolic state
	constraints
	$x_0 > 0$
	$p_0 \neq \text{NULL}$
	$2x_0 + 1 \neq v_0$

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



Concrete Execution

concrete state

Symbolic Execution

symbolic state

$$\begin{aligned}x_0 &> 0 \\ p_0 &\neq \text{NULL} \\ 2x_0 + 1 &\neq v_0\end{aligned}$$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

concrete

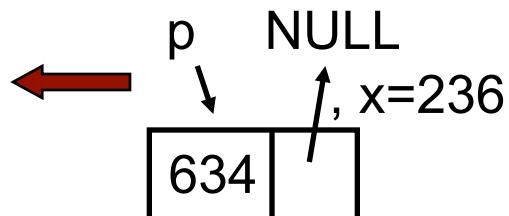
symbolic

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$ and
 $2x_0 + 1 = v_0$

$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 \neq v_0$

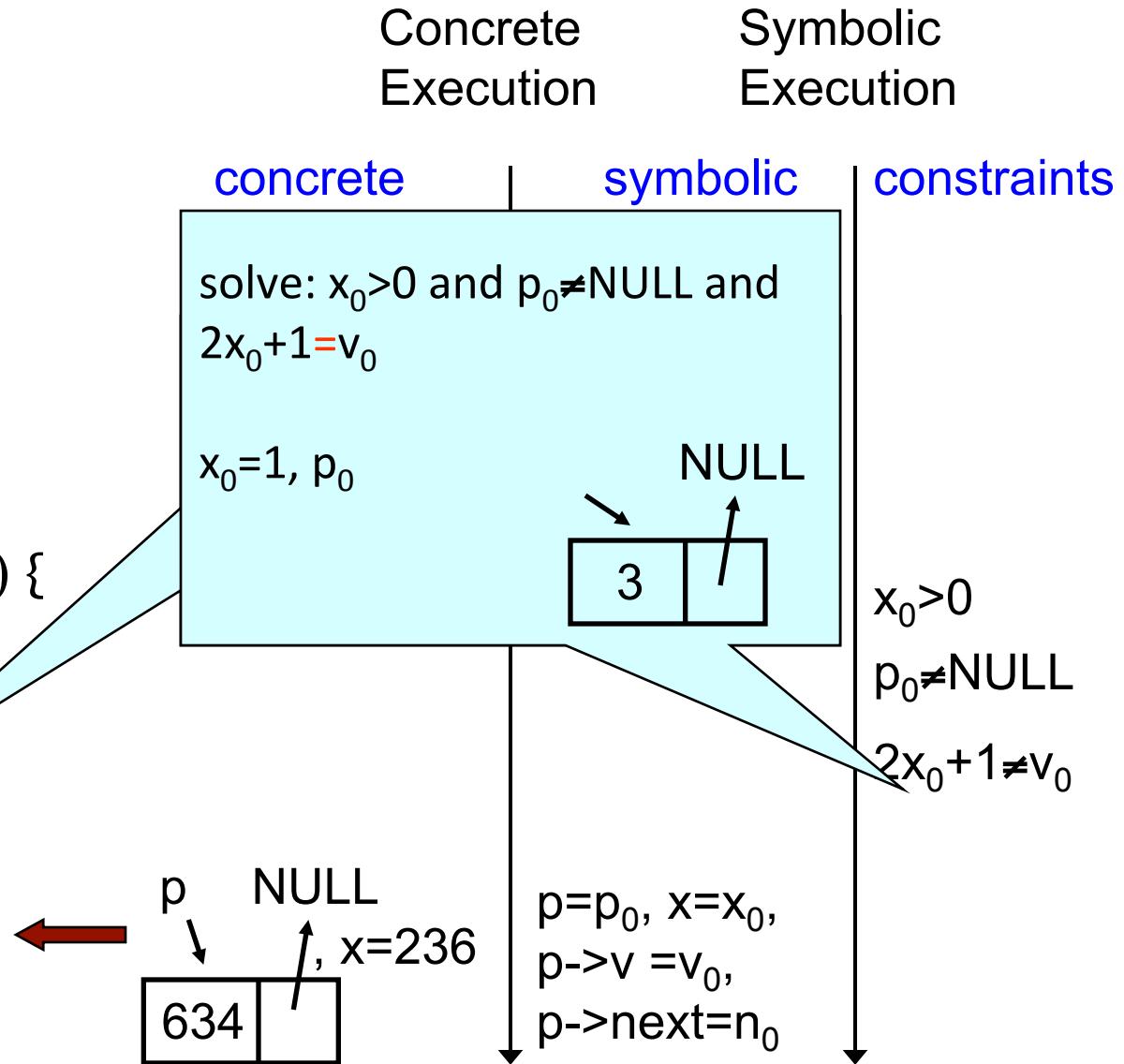
$p = p_0, x = x_0,$
 $p->v = v_0,$
 $p->next = n_0$



```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

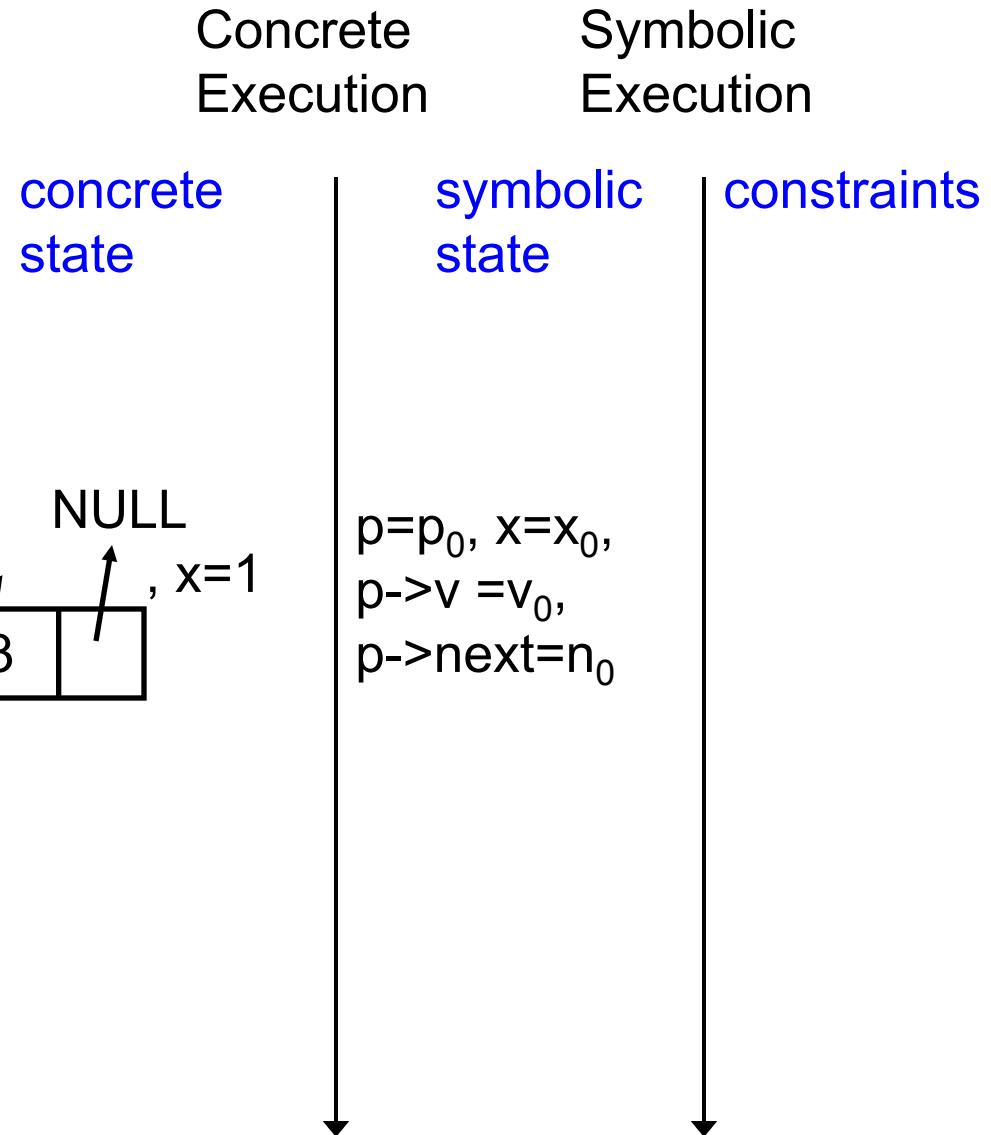
```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

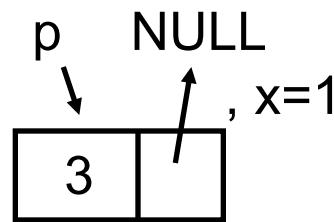
```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

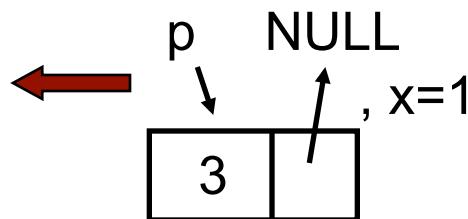


Concrete Execution	Symbolic Execution
concrete state	symbolic state
$p=p_0, x=x_0,$ $p->v =v_0,$ $p->next=n_0$	$x_0 > 0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

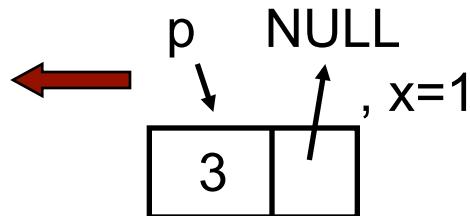


Concrete Execution	Symbolic Execution
concrete state	symbolic state
$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

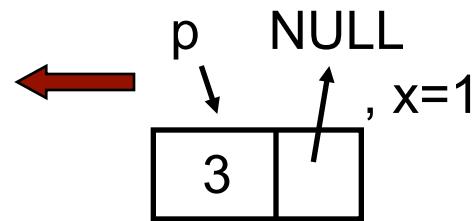


Concrete Execution	Symbolic Execution
concrete state	symbolic state
	constraints
	$x_0 > 0$
	$p_0 \neq \text{NULL}$
	$2x_0 + 1 = v_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

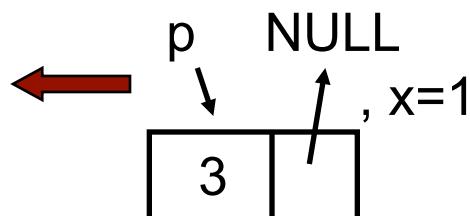


Concrete Execution	Symbolic Execution
concrete state	symbolic state
	constraints
	$x_0 > 0$
	$p_0 \neq \text{NULL}$
	$2x_0 + 1 = v_0$
	$n_0 \neq p_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```



Concrete Execution	Symbolic Execution
concrete state	symbolic state
	constraints
	$x_0 > 0$
	$p_0 \neq \text{NULL}$
	$2x_0 + 1 = v_0$
	$n_0 \neq p_0$
	$p = p_0, x = x_0,$
	$p->v = v_0,$
	$p->next = n_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

concrete
state

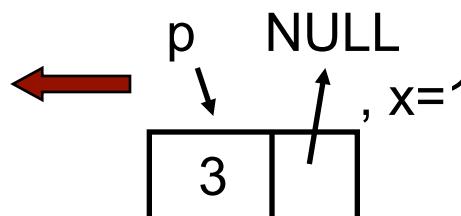
symbolic
state

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$ and
 $2x_0 + 1 = v_0$ and $n_0 = p_0$

.

$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 = v_0$
 $n_0 \neq p_0$



$p = p_0, x = x_0,$
 $p->v = v_0,$
 $p->next = n_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

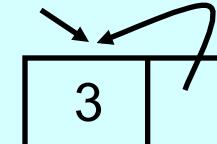
concrete
state

symbolic
state

constraints

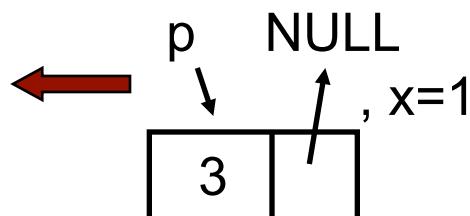
solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$ and
 $2x_0 + 1 = v_0$ and $n_0 = p_0$

$x_0 = 1, p_0$



$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 = v_0$
 $n_0 \neq p_0$

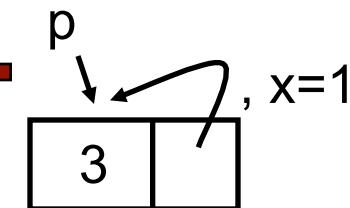
$p = p_0, x = x_0,$
 $p->v = v_0,$
 $p->next = n_0$



```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

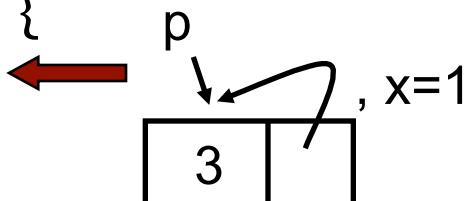
constraints

$p=p_0, x=x_0,$
 $p->v=v_0,$
 $p->next=n_0$

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

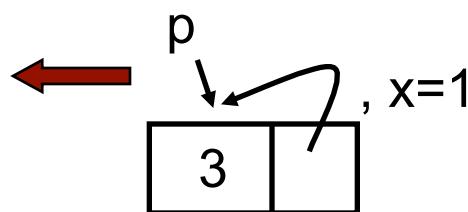


Concrete Execution	Symbolic Execution
concrete state	symbolic state
$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

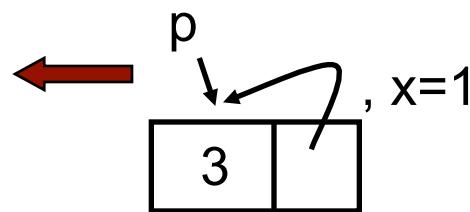


Concrete Execution	Symbolic Execution
concrete state	symbolic state
$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```



Concrete Execution	Symbolic Execution	
concrete state	symbolic state	constraints
 $x=1$	$p=p_0, x=x_0,$ $p \rightarrow v = v_0,$ $p \rightarrow \text{next} = n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$ $2x_0 + 1 = v_0$

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

```
int f(int v) {
    return 2*v + 1;
}
```

```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

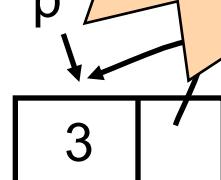
Symbolic
Execution

concrete
state

symbolic
state

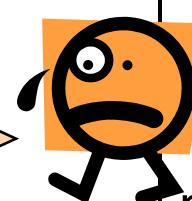
constraints

Program Error



3

x



$x_0 > 0$

$p_0 \neq \text{NULL}$

$2x_0 + 1 = v_0$

$n_0 = p_0$

$p = p_0, x = x_0,$
 $p->v = v_0,$
 $p->next = n_0$

