

Neural Networks

Jay chotaliya
Supervisor : Dr. Bernd Bauerhenne

Objectives

1. What are Neural Networks?
2. How we train them? (Back Propagation)
3. What is Convolution
4. How to write a Convolutional Neural Network to classify images

Neurons

- Perceptrons

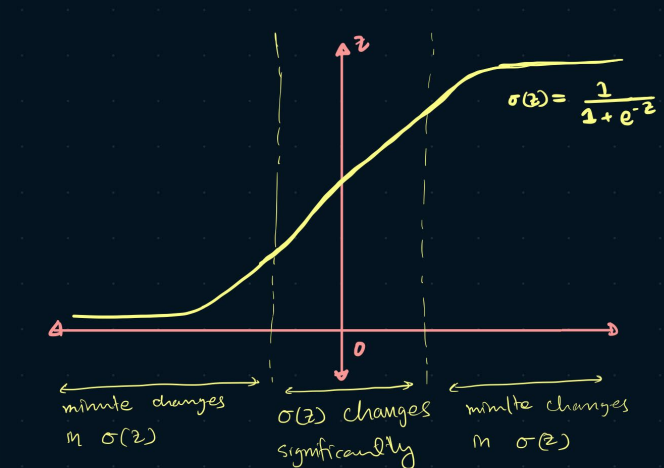
- Activation is step-function
- Not differentiable

- Sigmoid Neurons

- Activation is sigmoid function
- Differentiable

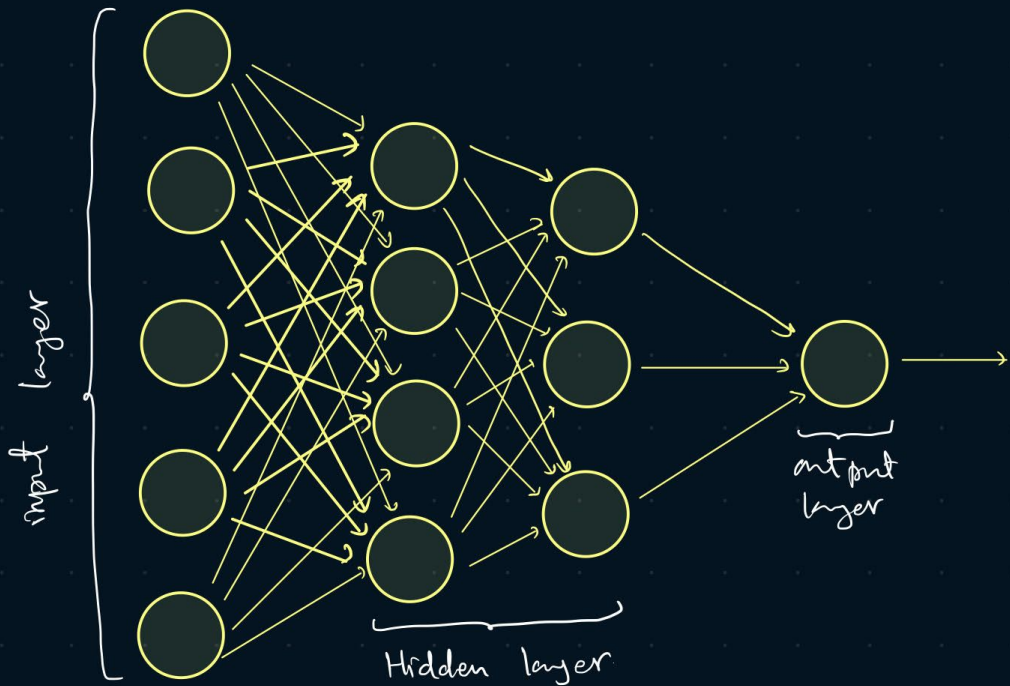
- Output of Sigmoid Neurons

- $\sigma(w.x + b)$
 - $\sigma(z) = 1 / 1 + \exp(-z)$



The Network - Feed Forward

- Connections are Weights
- Each neurons have a Bias.



Learning Algorithm

- Cost Functions

- Quadratic Cost Function

$$C = \frac{1}{2n} \sum_x \| \underbrace{y(x)}_{\text{True output}} - \underbrace{a^L(x)}_{\substack{\text{output of a layer} \\ \text{Activation}}} \|^2$$

L: no. of layers

- Cross Entropy Cost Function

$$C = -\frac{1}{n} \sum_x [y (\ln a) + (1-y) \ln (1-a)]$$

- Log likelihood Cost Function

$$C = \ln a_y^L$$

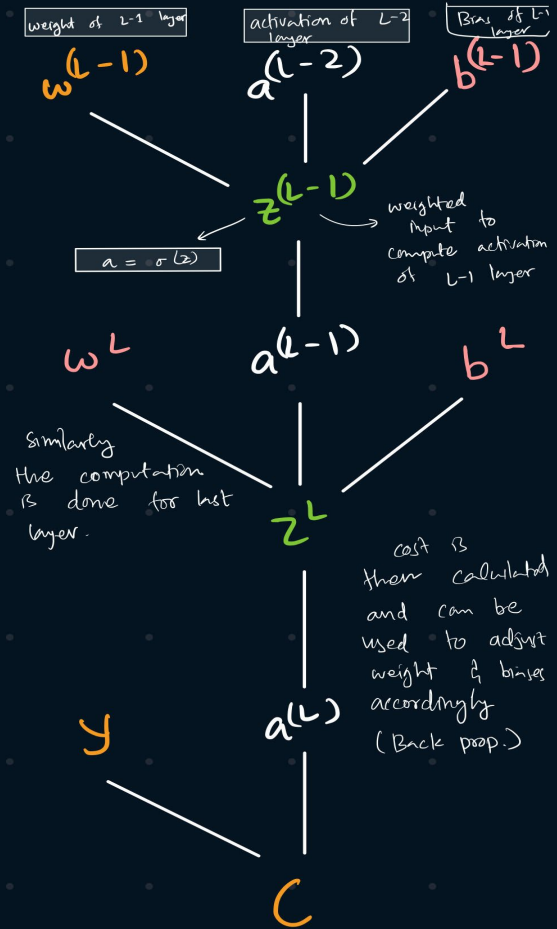
Learning Algorithm - Back Propagation

- The idea is to Minimize the Cost Function - Negative Gradient of Cost
- We feed backwards how the cost function changes with weights and biases

$$a^l = \sigma(w^l a^{l-1} + b^l)$$

$$a^l = \sigma(z^l) \quad \left\{ \begin{array}{l} z^l \equiv w^l a^{l-1} + b^l \end{array} \right.$$

weighted input to layer l.



Convolutional Neural Networks

- Convolution Operation -

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



0	0	1
1	0	0
0	1	1

Feature
Detector



0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

Effects of Convolution

Sharpen

0	0	0	0	0
0	0	-1	0	0
0	-1	5	-1	0
0	0	-1	0	0
0	0	0	0	0



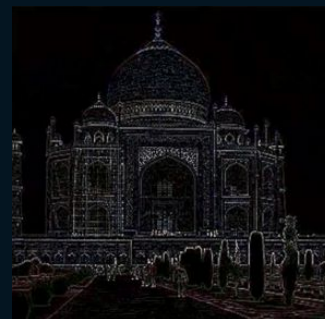
Blur

0	0	0	0	0
0	1	1	1	0
0	1	1	1	0
0	1	1	1	0
0	0	0	0	0



Edge Detection

	0	1	0	
	1	-4	1	
	0	1	0	



Padding, Stride and Max Pooling

- Padding :

0	0	0	0	0	0	0	0
0							0
0							0
0							0
0							0
0							0
0							0
0							0
0	0	0	0	0	0	0	0

- Stride : How much you move the filter

- Max-Pooling :

8	1	3	6
3	2	2	1
5	0	7	1
2	4	9	7



To The Code