

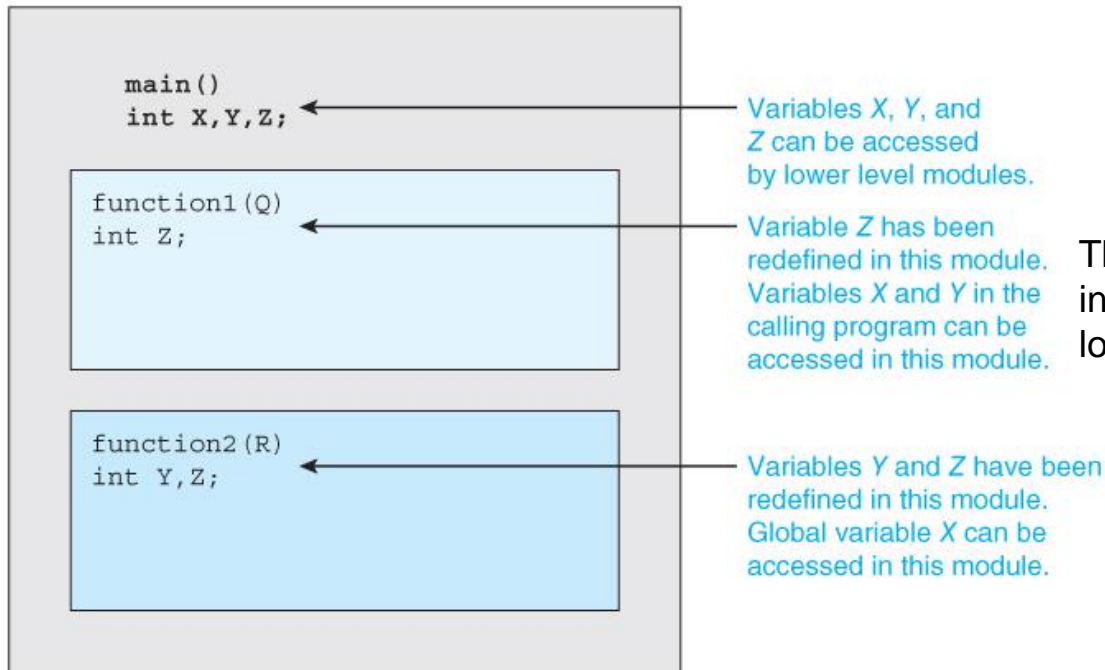
## 3.7 Stack, parameter passing and local variables

# Stack frame

- In the subroutine section, we learned how to:
  - pass parameter in a subroutine
  - return a value in a register
  - preserve registers on a stack
- The mechanism would not be sufficient if:
  - we need more parameters than can be supported by built-in registers
  - we need to set aside local variables within a subroutine
- *Stack frame* is a more sophisticated mechanism for passing parameters, handling local variables and preserving registers.
- Some concepts before introducing the stack frame  
.....

# Local and global variables

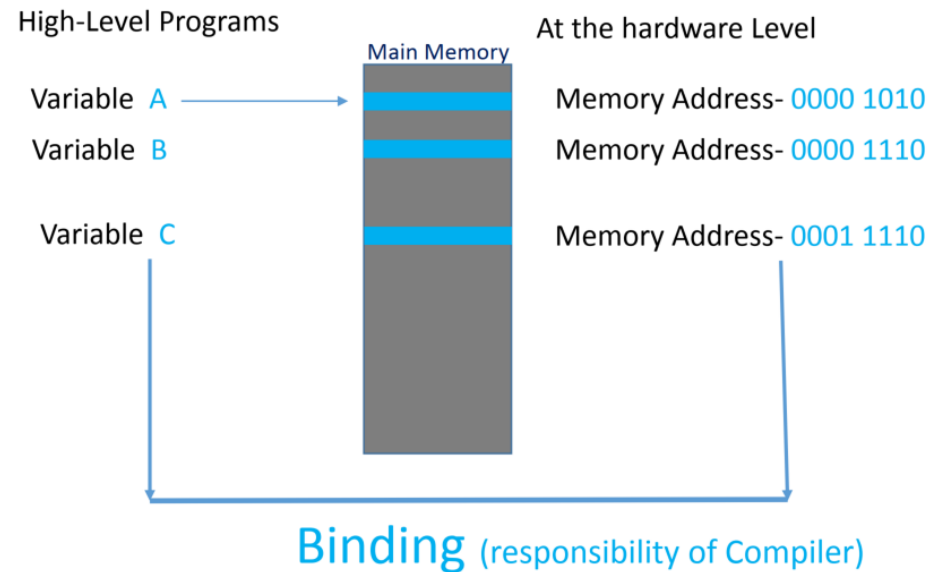
FIGURE 4.1 The concept of scope



The local variable Z is only accessible inside function1. The scope of the local variable Z is within function 1.

# Binding

- Binding: Associating a variable with its storage location
- Static binding:
  - this association is made at compile time.
- Dynamic binding:
  - this association is made at run-time.



# Recursion

- Recursive function: a function calling itself.

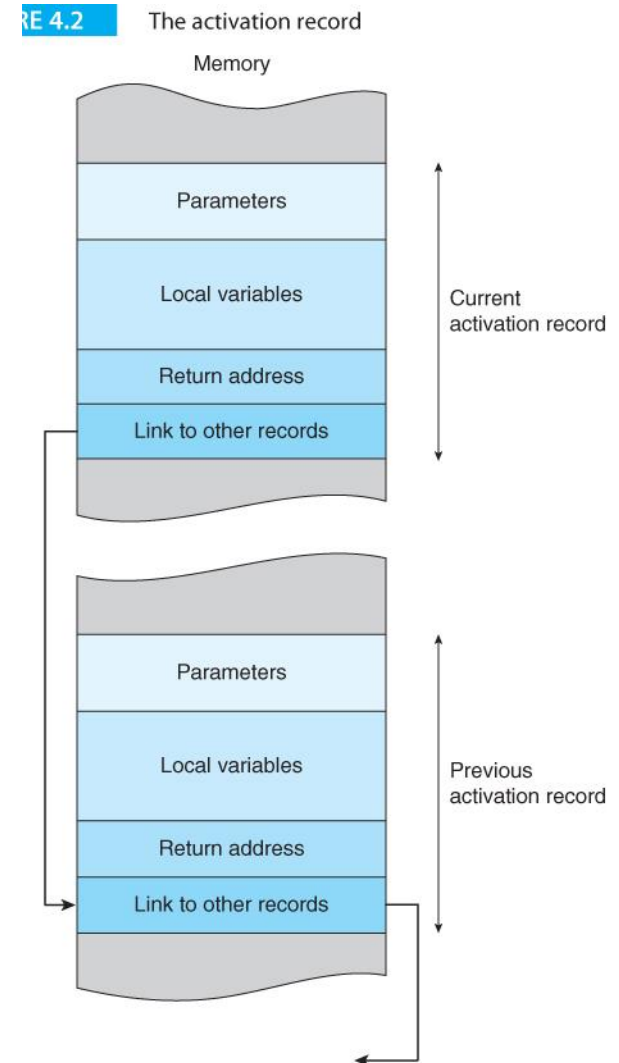
```
int Factorial(int n)
{
    if (n == 1)
        return 1;
    else
        return n * Factorial(n-1);
}
```

$$N! = N \times (N - 1)!$$

- The local variable `n` exists at different levels of the call.
- Static binding does not permit recursion.
- We need dynamic data storage discussed below.

# The stack and dynamic data storage

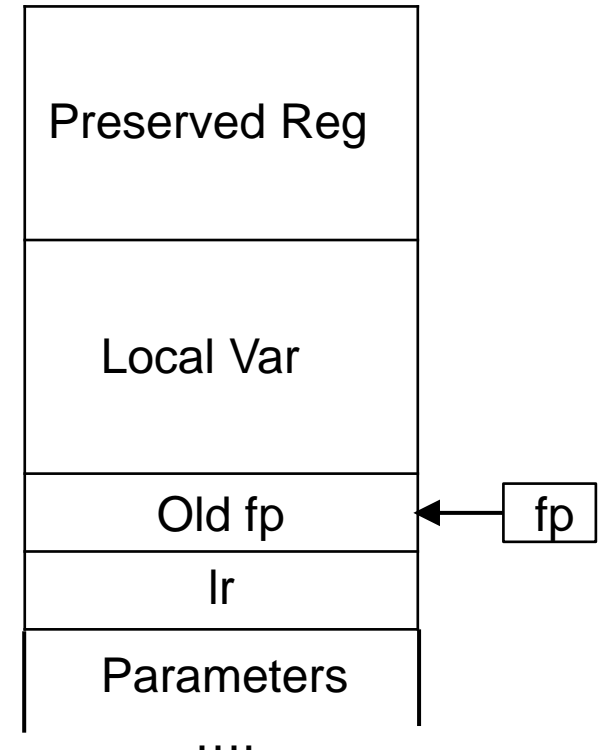
- When a subroutine is called, it is said to be *activated*.
- Each call is associated with an *activation record* (also called as *stack frame*)
- The activation record is the subroutine's view of the world.
- Recursion requires dynamic data storage because storage must be allocated at *runtime*.
- Executing a return from a subroutine *deallocates* or frees the storage taken up by the record.



# Stack frame in subroutine calling

The stack frame involves three major registers:

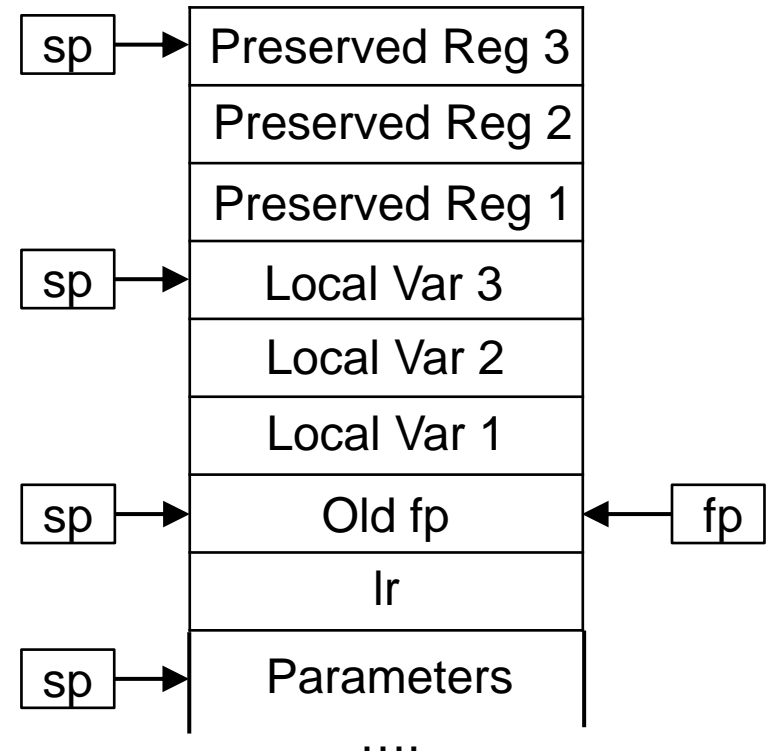
1. Stack pointer (sp) contains the address (points to) the top of stack.
2. Link register (lr) keeps track of the program line to return to after the subroutine finishes.
3. Frame pointer (fp) provides a reference point in the current activation record for users to locate parameters, local variables, saved link registers and preserved registers.



# Stack frame prologue

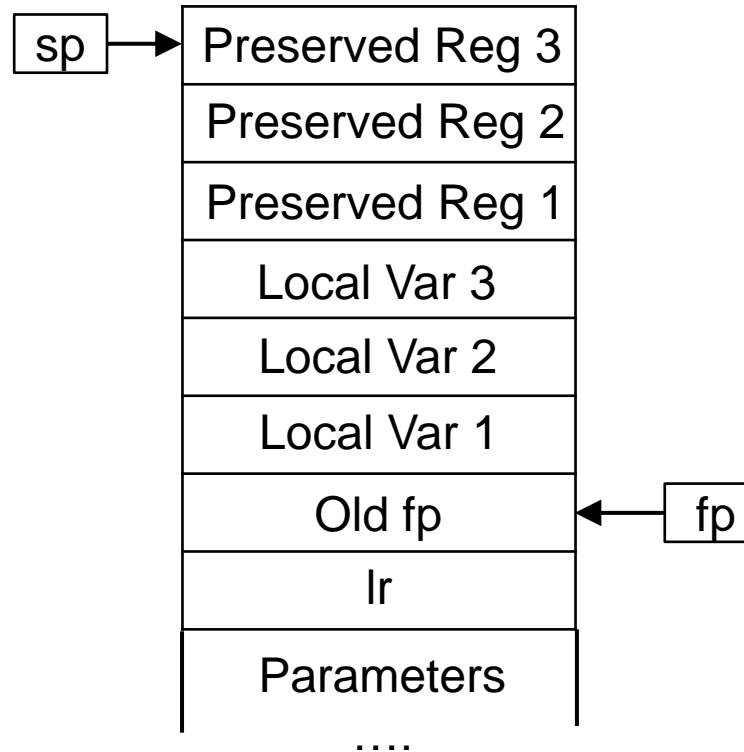
The prologue of a subroutine consists of the following steps:

1. Push the fp and lr onto the stack
  - fp is being preserved
  - The subroutine is called by the Branch Link (bl) instruction, which stores the instruction immediately following the subroutine call into lr.
2. Save the current sp to the fp.
3. Allocate local variable storage space on the stack.
4. Push register to preserve onto the stack





# After prologue



# ARM code implementing prologue

Sub:

```
stmfd sp!, {fp, lr} //Step 1
```

```
mov fp, sp //Step 2
```

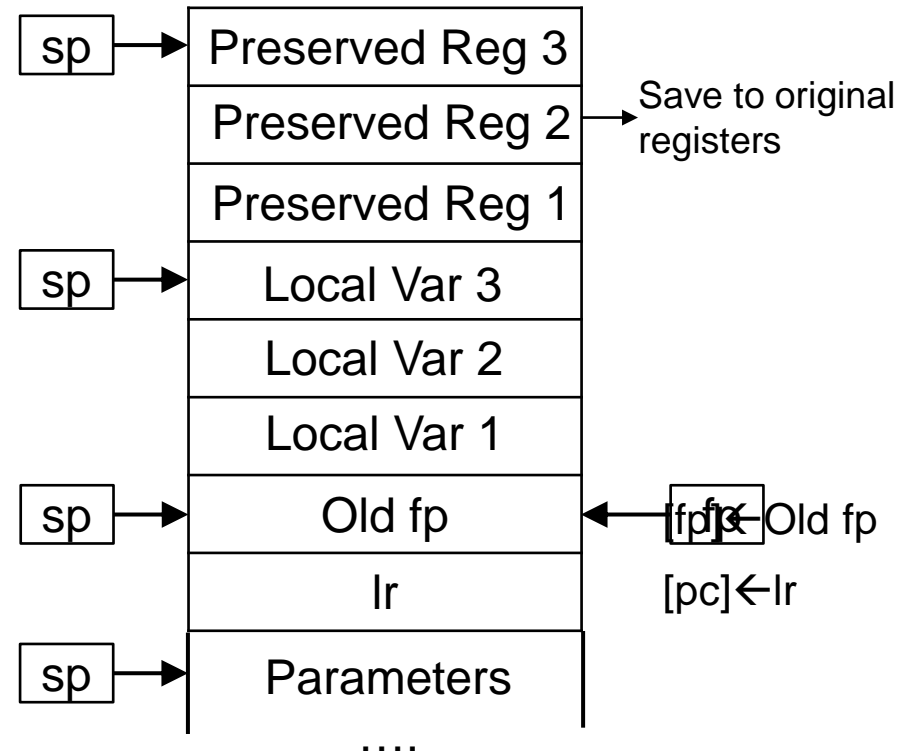
```
sub sp, sp, #4 //Step 3: assuming  
only one local variable
```

```
stmfd sp!, {r1-r3} // Step 4:  
assuming r1 to r3 are used in the  
subroutine
```

# Stack frame epilogue

The epilogue of a subroutine consists of the following steps:

1. Pop preserved registers from the stack.
2. Deallocate local variable storage from the stack
3. Pop fp and pc from the stack
  - the pc now contains the saved lr → Execution resumes at the line after the subroutine call



# ARM code implementing prologue

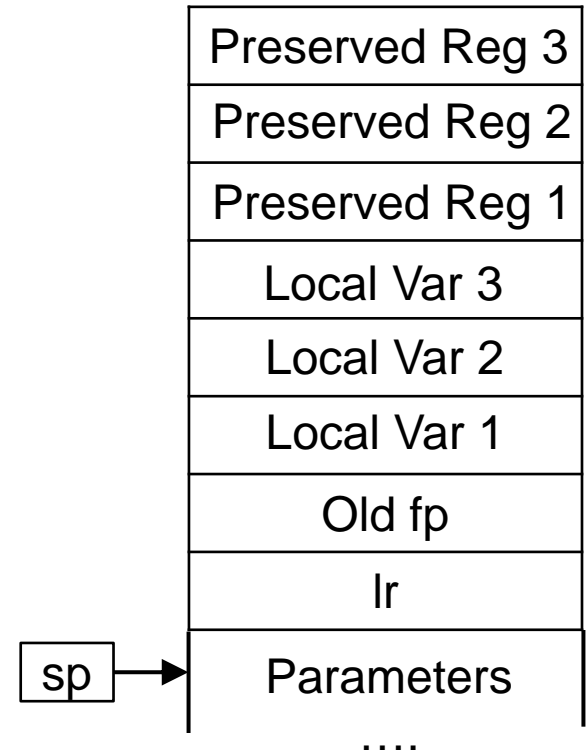
```
ldmfd sp!, {r1-r3} // Step 1
```

```
add sp, sp, #4 // Step 2
```

```
ldmfd sp!, {fp, pc} // Step 3
```

# State after epilogue

- The state of memory, except for the returned values in `r0` and updated parameter values, should be the same as before the subroutine was called.
- *Local variables* are called “local” because after the subroutine is done, references to all these local variables are removed (i.e., they cannot be accessed).
- Note that popped and deallocated values are still there, as the stack frame does not “clean up” memory used in the stack, but they are no longer kept track of by `sp` and will be overwritten by other uses of the stack.



# Before and after calling a subroutine

Before calling the subroutine:

- Push parameter(s) to the stack

After returning from the subroutine

- Deallocate parameter(s) from the stack

# Example 1: Putting it together

- Write a program that calculates the value of  $f(x)$  where
  - $f(x) = g(x) + h(x)$ ,  
where  $g(x) = x^2$  and  $h(x) = x + 0x18$
- Use r1 to store g
- Use r2 to store h
- The output is stored in r0
- Need to preserve r1 and r2
- No local variable

```

.global _start
_start:

mov sp, #0
mov fp, #0
ldr r1, =0x08
stmfd sp!, {r1} // push parameter to stack (Point 1)
bl Sub
add sp, sp, #4 // Deallocate the parameter (Point 7)

_stop:
b _stop

Sub:
//Prologue
stmfd sp!, {fp, lr} // Step 1 (Point 2)
mov fp, sp //Step 2 (Point 3)
//Step 3: No local variable
stmfd sp!, {r1-r3} // Step 4: Preserve r1 and r2 (Point 4)

ldr r3, [fp, #8] // Retrieve parameter and store in r3
mul r1, r3, r3 // Use r1 to store g
add r2, r3, #0x18 // Use r2 to store h

add r0, r1, r2 // Compute sum of g and h and save in
                // r0 as the return value.

//Epilogue
ldmfd sp!, {r1-r3} // Step 1 (Point 5)
// Step 2: No local variable
ldmfd sp!, {fp, pc} // Step 3 (Point 6)

.end

```



Pt	Stack					sp	fp
1	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa aaaaaaaa	aaaaaaaa aaaaaaaa	aaaaaaaa 00000008	FFFFFFFFC	0
2	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa 00000000	aaaaaaaa 00000014	aaaaaaaa 00000008	FFFFFFFF4	0
3	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa 00000000	aaaaaaaa 00000014	aaaaaaaa 00000008	FFFFFFFF4	FFFFFFFF4
4	ffffffe0 fffffff0	aaaaaaaa 00000000	aaaaaaaa 00000000	00000008 00000014	00000000 00000008	FFFFFFE8	FFFFFFFF4
5	ffffffe0 fffffff0	aaaaaaaa 00000000	aaaaaaaa 00000000	00000008 00000014	00000000 00000008	FFFFFFFF4	FFFFFFFF4
6	ffffffe0 fffffff0	aaaaaaaa 00000000	aaaaaaaa 00000000	00000008 00000014	00000000 00000008	FFFFFFFFC	0
7	ffffffe0 fffffff0 00000000	aaaaaaaa 00000000 e3a0d000	aaaaaaaa 00000000	00000008 00000014	00000000 00000008	0	0

## Example 2: Nested Subroutine Revisited

- The following program calculates the value of  $f(0x08)$  where
  - $f(x) = g(x+0x18) + 0x05$
  - $g(x) = x+0x12$
- No local variables in both subroutines
- `r0` is used to store the output

```

ldr sp, =0
ldr fp, =0
ldr r1, =0x08
stmfd sp!, {r1} //push parameter of f to
stack (Point 1)
bl f
add sp, sp, #4 //deallocate parameter for f
(Point 14)
Here:
b Here

f:
// Prologue
stmfd sp!, {fp, lr} // Step 1 (Point 2)
mov fp, sp // Step 2 (Point 3)
// Step 3: No local variable
stmfd sp!, {r1} // Step 4 (Point 4)

ldr r1, [fp, #8] // Retrieve parameter of f
add r1, r1, #0x18 // generate parameter for g
stmfd sp!, {r1} // push parameter of g to
stack (Point 5)

bl g

add sp, sp, #4 // deallocate parameter for g
(Point 11)
add r0, r0, #0x05 // Calculate output
parameter and store in r0

//Epilogue
ldmfd sp!, {r1} // Step 1 (Point 12)
//Step 2: No local variable
ldmfd sp!, {fp, pc} // Step 3 (Point 13)

```

```

g:
// Prologue
stmfd sp!, {fp, lr} // Step 1 (Point 6)
mov fp, sp // Step 2 (Point 7)
stmfd sp!, {r1} (Point 8)

ldr r1, [fp, #8]
add r0, r1, #0x12 // Calculate output
parameter and store in r0

//Epilogue
ldmfd sp!, {r1} // Step 1 (Point 9)
//Step 2: No local variable
ldmfd sp!, {fp, pc} // Step 3 (Point 10)

.end

```

Pt	Stack					sp	fp
1	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa aaaaaaaa	aaaaaaaa aaaaaaaa	aaaaaaaa 00000008	FFFFFFFFC	0
2	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa 00000000	aaaaaaaa 00000014	aaaaaaaa 00000008	FFFFFFF4	0
3	ffffffe0 fffffff0	aaaaaaaa aaaaaaaa	aaaaaaaa 00000000	aaaaaaaa 00000014	aaaaaaaa 00000008	FFFFFFF4	FFFFFFF4
4	ffffffe0 fffffff0	aaaaaaaa 00000008	aaaaaaaa 00000000	aaaaaaaa 00000014	aaaaaaaa 00000008	FFFFFFF0	FFFFFFF4
5	ffffffe0 fffffff0	aaaaaaaa 00000008	aaaaaaaa 00000000	aaaaaaaa 00000014	00000020 00000008	FFFFFFEC	FFFFFFF4
6	ffffffe0 fffffff0	aaaaaaaa 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	FFFFFFE4	FFFFFFF4
7	ffffffe0 fffffff0	aaaaaaaa 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	FFFFFFE4	FFFFFFE4

Pt	Stack					sp	fp
8		↓				FFFFFFE0	FFFFFFE4
	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008		
9			↓			FFFFFFE4	FFFFFFE4
	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008		
10					↓	FFFFFFEC	FFFFFFF4
	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008		
11	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	FFFFFFF0	FFFFFFF4
		↑					
12	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	FFFFFFF4	FFFFFFF4
			↑				
13	ffffffe0 fffffff0	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	FFFFFFFC	0
					↑		
14	ffffffe0 fffffff0 00000000	00000020 00000008	ffffffff4 00000000	00000038 00000014	00000020 00000008	0	0
	↑						

# Example 3: Pass by reference (Lab 6)

- Suppose you have the following data:

```
.data  
.align  
x:  
.word 15  
y:  
.word 9
```

- You want to swap the two values.
- You could pass the values 15 and 9 to the stack and swap their positions in the stack, but that is not what you want to achieve. This “pass-by-value” approach does not work.
- You want to pass the *addresses* of 15 and 9 as parameters to the stack so *that the values in the two memory locations get swapped*. This is referred to as “**pass by reference**”.

# Swap: Pass by reference

## Main Program

```
16 .global _start
17 _start:
18
19 ldr    r1, =y           // get address of second parameter
20 stmfd  sp!, {r1}        // push second parameter onto stack
21 ldr    r1, =x           // get address of first parameter
22 stmfd  sp!, {r1}        // push first parameter onto stack
23 bl     swap             // call subroutine
24 add    sp, sp, #8       // release parameter memory
25
26 _stop:
27 b      _stop
```

## Data Storage

```
70 .data
71 .align
72 x:
73 .word    15
74 y:
75 .word    9
76
77 .end
```

# Swap: Pass by reference

---

swaps location of two values in memory.

---

Parameters:

[fp, #8] – address of x

[fp, #12] – address of y

Local variable

temp (4 bytes on stack)

Uses:

r0 - stores address of x

r1 - stores address of y

r2 - registers for swapping operations

---

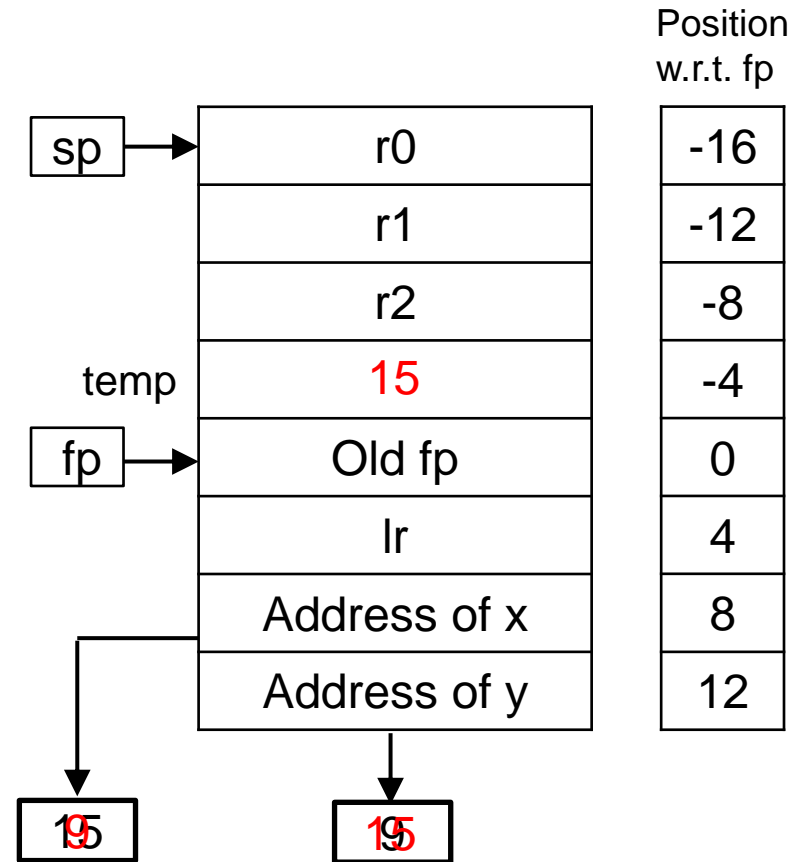
```
36 swap:
37 // Prologue
38 stmfd sp!, {fp, lr} // push frame pointer
39 mov fp, sp // save current stack top to frame pointer
40 sub sp, sp, #4 // set aside space for local variable temp
41 stmfd sp!, {r0-r2} // preserve other registers
42
43 ldr r0, [fp, #8] // put address of x in r0
44 ldr r1, [fp, #12] // put address of y in r1
45
46 ldr r2, [r0] // put value of x in r2
47 str r2, [fp, #-4] // copy value of x to temp
48
49 ldr r2, [r1] // put value of y in r2
50 str r2, [r0] // store value of y in address of x
51
52 ldr r2, [fp, #-4] // get temp
53 str r2, [r1] // store temp in address of y
54
55 //Epilogue
56 ldmfd sp!, {r0-r2} // pop preserved registers
57 add sp, sp, #4 // remove local storage
58 ldmfd sp!, {fp, pc} // pop frame pointer
59
60 .data
61 .align
62 x:
63 .word 15
64 y:
65 .word 9
66
67 .end
```



# Swap: Pass by reference

```
36 swap:
37 // Prologue
38 stmfd sp!, {fp, lr}           // push frame pointer
39 mov fp, sp                   // save current stack top to frame pointer
40 sub sp, sp, #4               // set aside space for local variable temp
41 stmfd sp!, {r0-r2}           // preserve other registers
42
43 ldr r0, [fp, #8]              // put address of x in r0
44 ldr r1, [fp, #12]             // put address of y in r1
45
46 ldr r2, [r0]                 // put value of x in r2
47 str r2, [fp, #-4]            // copy value of x to temp
48
49 ldr r2, [r1]                 // put value of y in r2
50 str r2, [r0]                 // store value of y in address of x
51
52 ldr r2, [fp, #-4]            // get temp
53 str r2, [r1]                 // store temp in address of y
54
55 //Epilogue
56 ldmfd sp!, {r0-r2}           // pop preserved registers
57 add sp, sp, #4               // remove local storage
58 ldmfd sp!, {fp, pc}           // pop frame pointer
59
60 .data
61 .align
62 x:
63 .word 15
64 y:
65 .word 9
66
67 .end
```

## Stack after prologue of swap



# MinMax subroutine in Lab 6

-----  
Finds the minimum and maximum values in a list.

Equivalent of: void MinMax (\*start, \*end, \*min, \*max)

Passes addresses of list, end of list, max, and min as parameters.

-----  
Parameters:

start - start address of list (fp + 4)

end - end address of list (fp + 8)

min - address of minimum result (fp + 12)

max - address of maximum result (fp + 16)

Uses:

r0 - address of start of list

r1 - address of end of list

r2 - minimum value so far

r3 - maximum value so far

r4 - address of value to process

```
61 MinMax:
62 stmfd sp!, {fp}           // preserve frame pointer
63 mov    fp, sp             // Save current stack top to frame pointer
64 // allocate local storage (none)
65 stmfd sp!, {r0-r4}        // preserve other registers
66
67 ldr    r0, [fp, #4]        // Get address of start of list
68 ldr    r2, [r0]            // store first value as minimum
69 ldr    r3, [r0], #4        // store first value as maximum
70 ldr    r1, [fp, #8]        // get address of end of list
71
72 MinMaxLoop:
73 cmp    r0, r1              // Compare addresses
74 beq    _MinMax
75 ldr    r4, [r0], #4
76 cmp    r4, r2
77 movlt  r2, r4
78 cmp    r4, r3
79 movgt  r3, r4
80 b      MinMaxLoop
81
82 _MinMax:
83 // Store results to address parameters
84 ldr    r0, [fp, #12]
85 str    r2, [r0]
86 ldr    r0, [fp, #16]
87 str    r3, [r0]
88
89 ldmfd  sp!, {r0-r4}        // pop preserved registers
90 // deallocate local storage (none was allocated)
91 ldmfd  sp!, {fp}          // pop frame pointer
92 bx     lr                  // return from subroutine
```

```
98 .data // Data section
99 .align
100 Data:
101 .word 4,5,-9,0,3,0,8,-7,12 // The list of data
102 _Data: // End of list address
103 Min:
104 .space 4
105 Max:
106 .space 4
107
108 .end
```

# Example 3: Recursion (Lab 7)

- The following C code implements the Euclidean algorithm in computing the Greatest Common Denominator (gcd) of two integers.

```
1  int gcd(a, b) {  
2      if(a == b) {  
3          return a;  
4      } else if(a > b) {  
5          return gcd(b, a - b);  
6      } else {  
7          return gcd(b, a);  
8      }
```

# Example 3: Recursion (Lab 7)

```
1  int gcd(a, b) {  
2      if(a == b) {  
3          return a;  
4      } else if(a > b) {  
5          return gcd(b, a - b);  
6      } else {  
7          return gcd(b, a);  
8      }
```

Principle:

- Condition 1:
  - If  $a > b$ , the problem can be reduced using the following property:
    - $\text{gcd}(a, b) = \text{gcd}(b, a - b)$
- Condition 2:
  - If  $b > a$ , reverse the order by calling  $\text{gcd}(b, a)$
  - Inside this  $\text{gcd}$  call, condition 1 would be satisfied, thereby reducing the problem.
- Eventually, the two input arguments are equal and  $\text{gcd}(a, a) = a$

# Numerical Examples

Large-Small	20	15
20-15	5	15
15-5	5	10
10-5	5	5

- $\text{gcd}(20, 15)$
- $\text{gcd}(15, 5)$
- $\text{gcd}(5, 10)$
- $\text{gcd}(10, 5)$
- $\text{gcd}(5, 5)$

Two arguments are the same.  
 $\text{gcd} = 5$

Large-Small	60	36
60-36	24	36
36-24	24	12
24-12	12	12

- $\text{gcd}(60, 36)$
- $\text{gcd}(36, 24)$
- $\text{gcd}(24, 12)$
- $\text{gcd}(12, 12)$

Two arguments are the same.  
 $\text{gcd} = 12$

# Example 3: Recursion (Lab 7)

## Main Program

```
21 ldr    r1, =numbers    // get address of numbers
22 ldr    r2, [r1, #4]    // put second number into register (4 bytes past first number)
23 stmfd  sp!, {r2}       // push second number onto stack
24 ldr    r2, [r1]        // put first number into register
25 stmfd  sp!, {r2}       // push first number onto stack
26 bl     gcd             // call the subroutine
27 add    sp, sp, #8      // release the parameter memory from the stack
28 // Result in r0
29
30 ldr    r1, =result
31 str    r0, [r1]        // write result back to memory
```

## Data Section

```
82 .data
83 .align
84 numbers:
85 .word 30, 12
86 result:
87 .space 4
88 .end
```

Before calling the subroutine:

- Push second and then first parameter(s) to the stack

After returning from the subroutine

- Deallocate parameter(s) from the stack

# gcd subroutine

Finds the Greatest Common  
Denominator of two integers (recursive)

Uses simple recursive algorithm:

```
int gcd(a, b) {  
    if(a == b) {  
        return a;  
    } else if(a > b) {  
        return gcd(b, a - b);  
    } else {  
        return gcd(b, a);  
    }  
}
```

Parameters:

a - value of first number

b - value of second number

Returns:

r0 - GCD of a and b

Uses:

r0 - value of a - return value

r1 - value of b

```
58 gcd:  
59 stmfd    sp!, {fp, lr}           // preserve frame pointer  
60 mov      fp, sp                 // save current stack top to frame pointer  
61 // No local variables  
62 stmfd    sp!, {r1}  
63  
64 // Copy parameters into registers  
65 ldr      r0, [fp, #8]           // get a  
66 ldr      r1, [fp, #12]          // get b  
67  
68 cmp      r0, r1  
69 beq      _gcd                   // a is the gcd: return in r0  
70 subgt    r0, r0, r1             // a > b: gcd(b, a - b)  
71 // else: gcd(b, a)  
72 stmfd    sp!, {r0}             // 2nd parameter - push a onto the stack  
73 stmfd    sp!, {r1}             // 1st parameter - push b onto the stack  
74 bl      gcd                     // recursive call to subroutine  
75 add      sp, sp, #8             // release parameter memory from stack  
76  
77 _gcd:  
78 ldmdfd   sp!, {r1}             // pop preserved registers  
79 // No local variables  
80 ldmdfd   sp!, {fp, pc}          // pop frame pointer
```

# Skeleton of the subroutine

```
58 gcd:
59 stmfd    sp!, {fp, lr}           // preserve frame pointer
60 mov      fp, sp                  // save current stack top to frame pointer
61 // No local variables
62 stmfd    sp!, {r1}
63
64 // Copy parameters into registers
65 ldr      r0, [fp, #8]             // get a
66 ldr      r1, [fp, #12]           // get b
67
68 cmp      r0, r1
69 beq      _gcd                    // a is the gcd: return in r0
70 subgt    r0, r0, r1              // a > b: gcd(b, a - b)
71                                     // else: gcd(b, a)
72 stmfd    sp!, {r0}               // 2nd parameter - push a onto the stack
73 stmfd    sp!, {r1}               // 1st parameter - push b onto the stack
74 bl      gcd                      // recursive call to subroutine
75 add      sp, sp, #8              // release parameter memory from stack
76
77 gcd:
78 ldmfd    sp!, {r1}               // pop preserved registers
79 // No local variables
80 ldmfd    sp!, {fp, pc}           // pop frame pointer
```

## Standard Prologue

Just like before and after calling a subroutine in the main program, we need to:

Push parameters to stack before calling subroutine

Deallocate parameters when the subroutine finishes

## Standard Epilogue



# Example: gcd (18,12)

Sequence of calls:

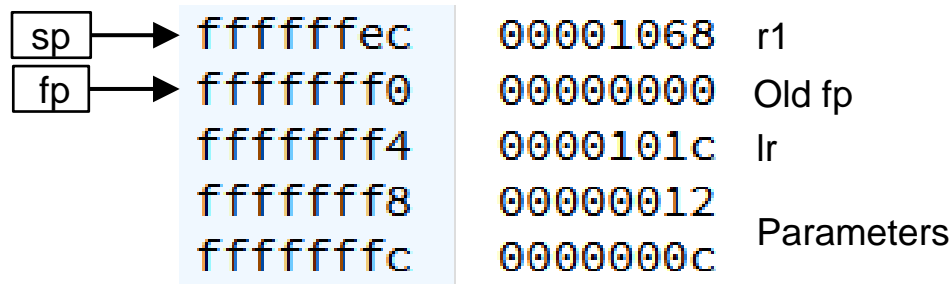
1. gcd (18, 12) from main program
2. gcd (12, 6)
3. gcd (6, 6) → return 6

```
1  int gcd(a, b) {  
2      if(a == b) {  
3          return a;  
4      } else if(a > b) {  
5          return gcd(b, a - b);  
6      } else {  
7          return gcd(b, a);  
8      }
```

# Example: gcd (18,12)

1. Call gcd (18, 12) from main program

State of the stack after the prologue of gcd:



# Example: gcd (18,12)

2. Call gcd (12, 6)

State of the stack after the prologue of gcd:

sp	→	ffffffd8	0000000c	r1
fp	→	ffffffdc	ffffffff	Old fp
		ffffffe0	00001054	lr
		ffffffe4	0000000c	
		ffffffe8	00000006	Parameters
		ffffffec	00001068	
		fffffff0	00000000	
		fffffff4	0000101c	
		fffffff8	00000012	
		fffffffc	0000000c	

# Example: gcd (18,12)

## 3. Call gcd (6, 6)

State of the stack after the prologue of gcd:

sp	→	ffffffc4	00000006	r1
fp	→	ffffffc8	ffffffdc	Old fp
		ffffffcc	00001054	lr
		ffffffd0	00000006	Parameters
		ffffffd4	00000006	
		ffffffd8	0000000c	
		ffffffdc	ffffffff0	
		ffffffe0	00001054	
		ffffffe4	0000000c	
		ffffffe8	00000006	
		ffffffec	00001068	
		fffffff0	00000000	
		fffffff4	0000101c	
		fffffff8	00000012	
		fffffffc	0000000c	