

Exercise 10

Dijkstra's Algorithm

10. Write a C++ program for implementation of Dijkstra's algorithm.

Objective:

The objectives of this exercise enable you to find the shortest path between two vertices in a graph with the help of Dijkstra's algorithm.

Procedure and description:

This algorithm is used to find the shortest path between the two vertices in a weighted directed graph and it is also very popular and efficient to find each and every path from starting (source) to terminal vertices.

Algorithm:

v_s : Source vertex

v_t : Terminal vertex (end vertex)

V_r : vertex with label r

$v_{s,z}$: vertex associated with s and z; z intermediate vertices to reach the Terminal vertex

$w(v_i, v_j)$: the weight associated with every edge (v_i, v_j)

Dijkstra's algorithm is given below in stepwise manner:

Step 1: Assign a temporary label 1 $(v_i) = \infty$ to all vertices except v_s

Step 2: Mark v_s as permanent by assigning 0 label to it

$$1(v_{s,z}) = 0$$

Step 3: Assign value of v_s to v_r where v_r is last vertex to be made permanent. $V_r = V_s$

Step 4: If $(v_i) > (v_k) + w(v_k, v_i)$.

$$(v_i) = (v_k) + w(v_k, v_i).$$

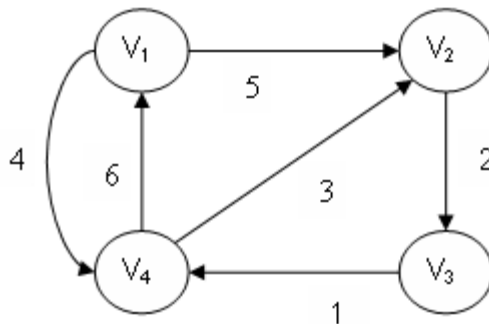
Step 5: $v_r = v_i$

Step 6: If v_t has temporary label, repeat step 4 to step 5 otherwise the value of v_t is permanent label and is equal to the shortest path v_s to v_t .

Step 7: Exit.

Expected Output:**Input:**

After executing program. Enter input graph, vertices and distance between vertices as a two dimensional matrix. For better understanding a graphical representation is shown below



Enter any two vertex's between which the shortest path is to be found. Consider vertices as V1 to V₃ respectively.

Output: the shortest path between V₁ to V₃ is: 7
