TRIGONOMETRY

DEFINITION

RIGHT TRIANGLE DEFINITION

$$\sin \theta = \frac{opposite}{hypotenuse}$$

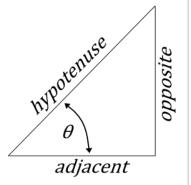
$$\csc \theta = \frac{hypotenuse}{opposite}$$

$$\cos \theta = \frac{adjacent}{hypotenuse}$$
 $\sec \theta = \frac{hypotenuse}{adjacent}$

$$\sec \theta = \frac{hypotenuse}{adjacent}$$

$$\tan \theta = \frac{opposite}{adjacent}$$

$$\cot \theta = \frac{adjacent}{opposite}$$



TRIG FUNCTIONS RANGE

$$-1 \le \sin \theta \le 1$$

$$-1 \le \cos \theta \le 1$$

$$-\infty \le \tan \theta \le \infty$$

$$\csc \theta \ge 1$$
 and $\csc \theta \le -1$

$$\sec \theta \ge 1$$
 and $\sec \theta \le -1$

$$-\infty \le \cot \theta \le \infty$$

UNIT CIRCLE DEFINITION

$$\sin \theta = y$$

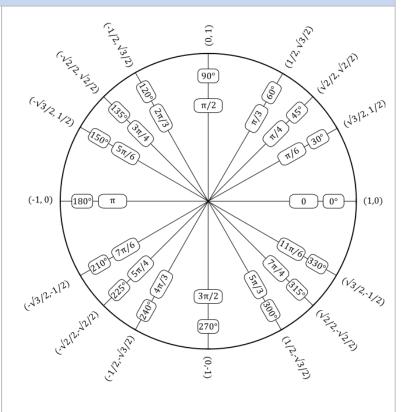
$$\cos \theta = x$$

$$\tan \theta = \frac{y}{x}$$

$$\csc \theta = \frac{1}{v}$$

$$\sec \theta = \frac{1}{x}$$

$$\cot \theta = \frac{x}{y}$$



TRIG FUNCTIONS DOMAIN

 $\sin \theta$, θ can be any angle

 $\cos \theta$, θ can be any angle

$$\tan \theta$$
, $\theta \neq \left(n + \frac{1}{2}\right) \pi$, $n = 0, \pm 1, \pm 2, ...$

$$\csc \theta$$
, $\theta \neq n \pi$, $n = 0, \pm 1, \pm 2, ...$

$$\sec \theta$$
, $\theta \neq \left(n + \frac{1}{2}\right) \pi$, $n = 0, \pm 1, \pm 2, ...$

$$\cot \theta$$
, $\theta \neq n \pi$, $n = 0, \pm 1, \pm 2, ...$

INVERSE TRIG FUNCTION NOTATION

$$\sin^{-1} x \equiv \arcsin x \equiv A \sin x$$

$$\cos^{-1} x \equiv \arccos x \equiv A\cos x$$

 $\tan^{-1} x \equiv \arctan x \equiv \operatorname{Atan} x$

INVERSE TRIG DOMAIN

$$\sin^{-1} x : -1 \le x \le 1$$

$$\cos^{-1} x : -1 \le x \le 1$$

$$\tan^{-1} x : -\infty \le x \le \infty$$

TRIG FUNCTIONS PERIOD

$$\sin(\omega\theta) \rightarrow T = \frac{2\pi}{\omega}$$

$$\cos(\omega\theta) \to T = \frac{2\pi}{\omega}$$

$$tan(\omega\theta) \rightarrow T = \frac{\pi}{\omega}$$

$$\csc(\omega\theta) \rightarrow T = \frac{2\pi}{\omega}$$

$$\sec(\omega\theta) \to T = \frac{2\pi}{\omega}$$

$$\cot(\omega\theta) \rightarrow T = \frac{\pi}{\omega}$$

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INVERSE TRIG FUNCTION RANGE

$$-\frac{\pi}{2} \le \sin^{-1} x \le \frac{\pi}{2}$$

$$0 \le \cos^{-1} x \le \pi$$

$$-\frac{\pi}{2} \le \tan^{-1} x \le \frac{\pi}{2}$$