

## Data representation analysis

**Step 1** Create a directory on your computer where the home work will be implemented. That means all input files should be placed there and R will create the output files in this directory.

**Step 2** Open R- studio. In the command prompt select “Session” then “Set working directory” and “Choose directory”. Using the command prompt with file manager select the directory you created in Step 1.

```
> setwd("D:/ABI Assignments")
```

**Step 3**(1 mark) Read Auto.csv file. Use command `dim` to check how many observations and variables are in this file. Report the output below:

**COMMAND:**

```
> Auto <- read.csv("D:/ABI Assignments/Auto.csv")
> dim(Auto)
[1] 397  9
```

**OUTPUT:** 397 Observations and 9 Variables.

**Step 4**(1 mark) Use command `fix` to open the file editor. The program will open you this file, check what variables you have there and close the file. Change the name of variable “cylinders” to “cyl”. Use command `names` to print the name of the variables. Report the output below:

```
> fix(Auto)

> names(Auto)
[1] "mpg"           "cyl"           "displacement"  "horsepower"
[5] "weight"        "acceleration"  "year"          "origin"
[9] "name"
```

The screenshot shows a 'Data Editor' window with a menu bar (File, Edit, Help) and a data grid. The grid has 19 rows and 8 columns. The first row is highlighted. The columns are labeled: mpg, cylinders, displacement, horsepower, weight, acceleration, and year. The data values are as follows:

|    | mpg | cylinders | displacement | horsepower | weight | acceleration | year |
|----|-----|-----------|--------------|------------|--------|--------------|------|
| 1  | 18  | 8         | 307          | 130        | 3504   | 12           | 70   |
| 2  | 15  | 8         | 350          | 165        | 3693   | 11.5         | 70   |
| 3  | 18  | 8         | 318          | 150        | 3436   | 11           | 70   |
| 4  | 16  | 8         | 304          | 150        | 3433   | 12           | 70   |
| 5  | 17  | 8         | 302          | 140        | 3449   | 10.5         | 70   |
| 6  | 15  | 8         | 429          | 198        | 4341   | 10           | 70   |
| 7  | 14  | 8         | 454          | 220        | 4354   | 9            | 70   |
| 8  | 14  | 8         | 440          | 215        | 4312   | 8.5          | 70   |
| 9  | 14  | 8         | 455          | 225        | 4425   | 10           | 70   |
| 10 | 15  | 8         | 390          | 190        | 3850   | 8.5          | 70   |
| 11 | 15  | 8         | 383          | 170        | 3563   | 10           | 70   |
| 12 | 14  | 8         | 340          | 160        | 3609   | 8            | 70   |
| 13 | 15  | 8         | 400          | 150        | 3761   | 9.5          | 70   |
| 14 | 14  | 8         | 455          | 225        | 3086   | 10           | 70   |
| 15 | 24  | 4         | 113          | 95         | 2372   | 15           | 70   |
| 16 | 22  | 6         | 198          | 95         | 2833   | 15.5         | 70   |
| 17 | 18  | 6         | 199          | 97         | 2774   | 15.5         | 70   |
| 18 | 21  | 6         | 200          | 85         | 2587   | 16           | 70   |
| 19 | 27  | 4         | 97           | 88         | 2130   | 14.5         | 70   |

Name changed from cylinders to cyl.

The screenshot shows an RStudio interface. The 'Data Editor' window is open, displaying a table of car data. The table has 8 columns: mpg, cyl, displacement, horsepower, weight, acceleration, year, and origin. The data is sorted by mpg in descending order. The 'Data' pane on the left shows the 'Auto' dataset with 397 rows and 9 columns.

|    | mpg | cyl | displacement | horsepower | weight | acceleration | year | origin |
|----|-----|-----|--------------|------------|--------|--------------|------|--------|
| 1  | 18  | 8   | 307          | 130        | 3504   | 12           | 70   | 1      |
| 2  | 15  | 8   | 350          | 165        | 3693   | 11.5         | 70   | 1      |
| 3  | 18  | 8   | 318          | 150        | 3436   | 11           | 70   | 1      |
| 4  | 16  | 8   | 304          | 150        | 3433   | 12           | 70   | 1      |
| 5  | 17  | 8   | 302          | 140        | 3449   | 10.5         | 70   | 1      |
| 6  | 15  | 8   | 429          | 198        | 4341   | 10           | 70   | 1      |
| 7  | 14  | 8   | 454          | 220        | 4354   | 9            | 70   | 1      |
| 8  | 14  | 8   | 440          | 215        | 4312   | 8.5          | 70   | 1      |
| 9  | 14  | 8   | 455          | 225        | 4425   | 10           | 70   | 1      |
| 10 | 15  | 8   | 390          | 190        | 3850   | 8.5          | 70   | 1      |
| 11 | 15  | 8   | 383          | 170        | 3563   | 10           | 70   | 1      |
| 12 | 14  | 8   | 340          | 160        | 3609   | 8            | 70   | 1      |
| 13 | 15  | 8   | 400          | 150        | 3761   | 9.5          | 70   | 1      |
| 14 | 14  | 8   | 455          | 225        | 3086   | 10           | 70   | 1      |
| 15 | 24  | 4   | 113          | 95         | 2372   | 15           | 70   | 3      |
| 16 | 22  | 6   | 198          | 95         | 2833   | 15.5         | 70   | 1      |
| 17 | 18  | 6   | 199          | 97         | 2774   | 15.5         | 70   | 1      |
| 18 | 21  | 6   | 200          | 85         | 2587   | 16           | 70   | 1      |
| 19 | 27  | 4   | 97           | 88         | 2130   | 14.5         | 70   | 3      |

**Step 5** (1 mark) There are various ways to deal with the missing data. In this case, only five of the rows contain missing observations, and so we choose to use the `na.omit()` function to simply remove these rows. Check the file with `dim()` command again. How many missing row do you have in this file?

### OUTPUT:

```
> na.omit(Auto)
> dim(Auto)
[1] 397  9
```

**CONCLUSION:** There are no missing values in the file.

**Step 6** (1 mark) We can use the `plot()` function to produce *scatterplots* of the quantitative variables. To indicate the file from which variables should be plotted use command `attach()` before. Report the results including the scatterplot of cylinders vs mpg. Save the output to the \*.pdf file then download it to this report.

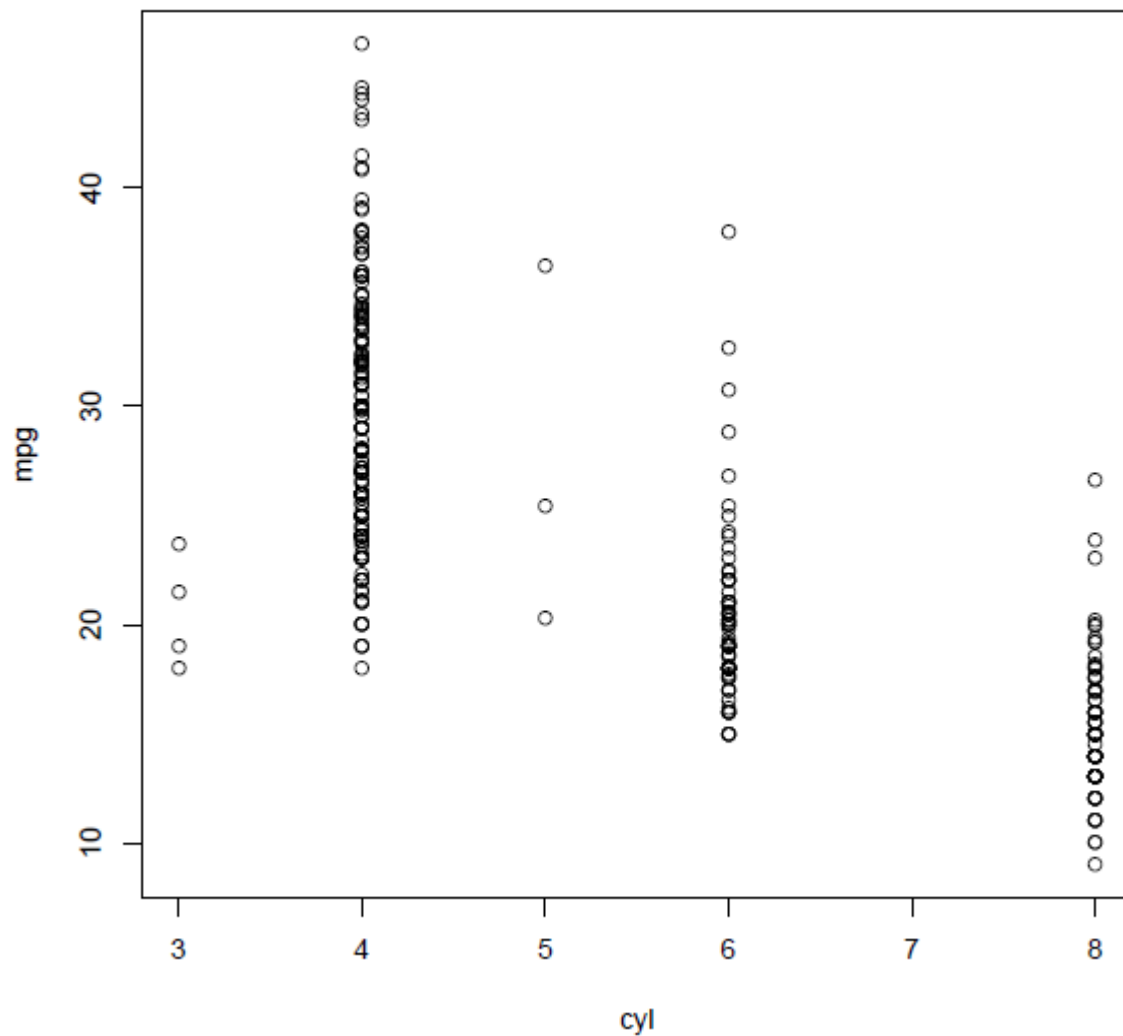
## **COMMAND**

```
attach(Auto)
plot(cyl, mpg, main="Scatterplot",
     xlab="cyl ", ylab="mpg ")
```

```
pdf (" scatterplot.pdf ")
plot(cyl,mpg)
dev.off ()
```

## **OUTPUT:**

```
> attach(Auto)
> plot(cyl, mpg, main="Scatterplot", xlab="cyl ", ylab="mpg ")
>
> pdf (" scatterplot.pdf ")
> plot(cyl,mpg)
> dev.off ()
RStudioGD
2
```



**Step 7** (1 mark) Produce the histogram for horsepower variable using `hist()` command. Use blue color (`col`) and 6 bars (`breaks`).

### COMMAND

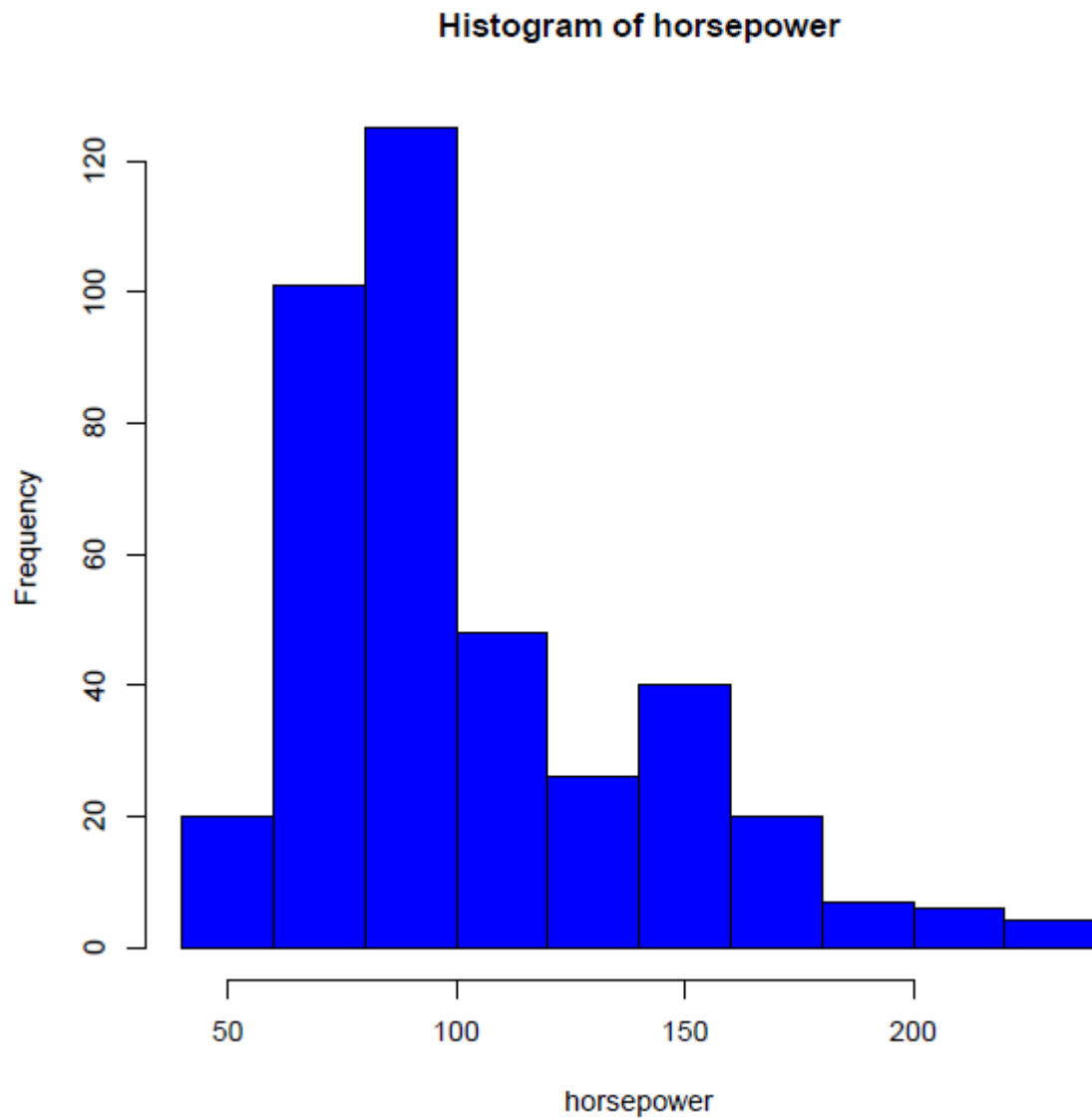
```
plot(cyl, mpg, main="Scatterplot",
     xlab="cyl ", ylab="mpg ")

hist(horsepower, breaks=6, col="blue")

pdf (" histogram .pdf ")
hist(horsepower ,col =" blue ")
dev.off ()
```

## OUTPUT

```
> plot(cyl, mpg, main="Scatterplot",  
+       xlab="cyl ", ylab="mpg ")  
> hist(horsepower, breaks=6, col="blue")  
>  
> pdf (" histogram .pdf ")  
> hist(horsepower ,col =" blue ")  
> dev.off ()  
RStudioGD  
2
```



**Step8** (1 mark) Produce the statistical summary form mpg and acceleration variables using `summary()` command. Are these data samples symmetric or skewed.

**COMMAND:**

```
summary(mpg)
```

```
summary(acceleration)
```

**OUTPUT**

```
>
> summary(mpg)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  9.00  17.50   23.00   23.52   29.00   46.60
> summary(acceleration)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
  8.00  13.80   15.50   15.56   17.10   24.80
>
> library(e1071)
>
> skewness(Auto$mpg)
[1] 0.4525649
>
> skewness(Auto$acceleration)
[1] 0.278699
> |
```

**Observation:**

- The data samples are skewed.
- If mean and median does not coincide, it is skewed and not symmetric.
- For mpg, Media =23.00 < Mean =23.52- It is Right Skewed
- For acceleration, Media=15.00 < Mean=15.56- It is Right Skewed
- The data samples are Positive skewed which indicates that the mean of the data values is larger than the median, and the data distribution is right-skewed.

## Simple (one variable) linear regression

You need to connect MASS library using the command `library(MASS)`. The `Boston` data is part of the `MASS` library. The `MASS` library contains the `Boston` data set, which records `medv` (median house value) for 506 neighborhoods around Boston. We will seek to predict `medv` using 13 predictors such as `rm` (average number of rooms per house), `age` (average age of houses), and `lstat` (percent of households with low socioeconomic status).

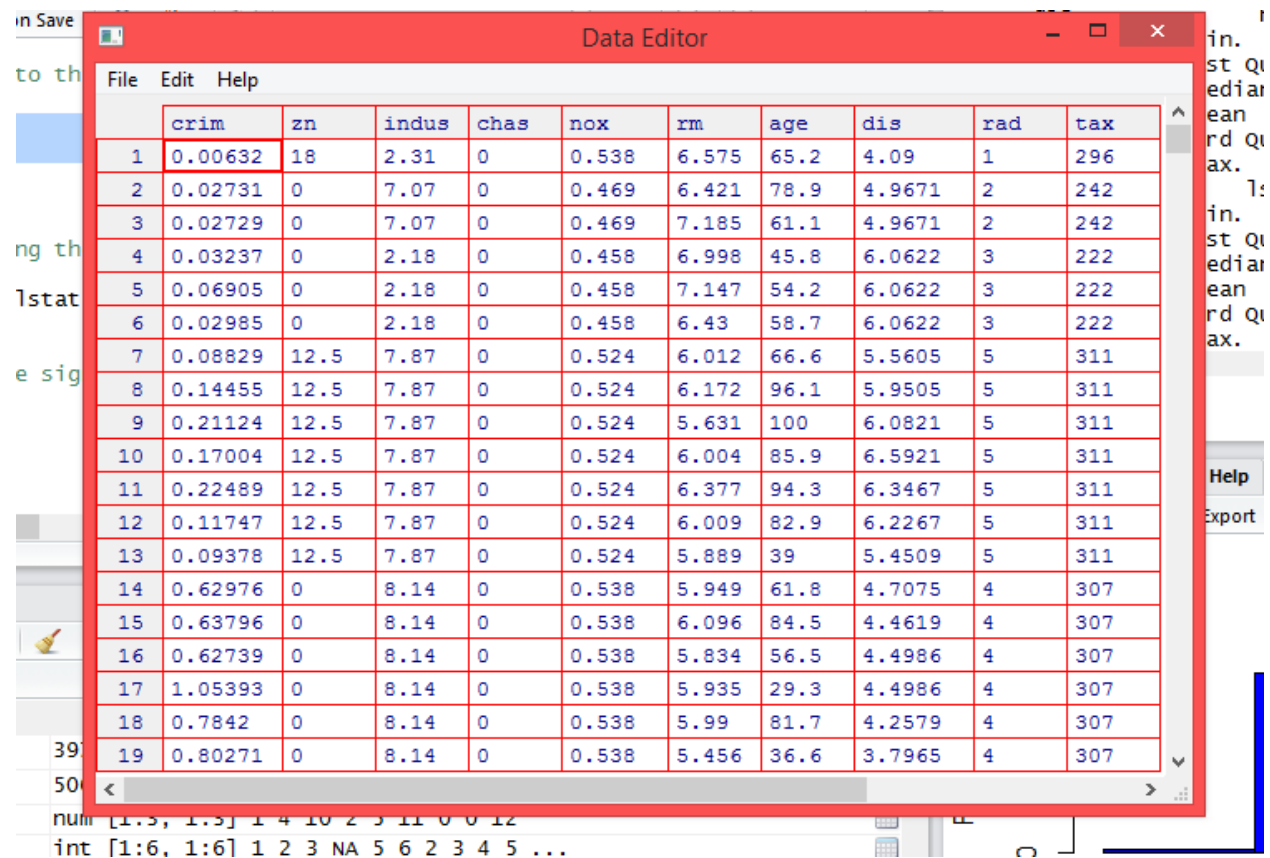
**Step 1** (1 mark) Have a look to this data using `fix` command and print summary statistics for all variables.

## COMMAND

```
library(MASS)
fix(Boston)
summary(Boston)
```

## OUTPUT

```
> library(MASS)
> fix(Boston)
```



|    | crim    | zn   | indus | chas | nox   | rm    | age  | dis    | rad | tax |
|----|---------|------|-------|------|-------|-------|------|--------|-----|-----|
| 1  | 0.00632 | 18   | 2.31  | 0    | 0.538 | 6.575 | 65.2 | 4.09   | 1   | 296 |
| 2  | 0.02731 | 0    | 7.07  | 0    | 0.469 | 6.421 | 78.9 | 4.9671 | 2   | 242 |
| 3  | 0.02729 | 0    | 7.07  | 0    | 0.469 | 7.185 | 61.1 | 4.9671 | 2   | 242 |
| 4  | 0.03237 | 0    | 2.18  | 0    | 0.458 | 6.998 | 45.8 | 6.0622 | 3   | 222 |
| 5  | 0.06905 | 0    | 2.18  | 0    | 0.458 | 7.147 | 54.2 | 6.0622 | 3   | 222 |
| 6  | 0.02985 | 0    | 2.18  | 0    | 0.458 | 6.43  | 58.7 | 6.0622 | 3   | 222 |
| 7  | 0.08829 | 12.5 | 7.87  | 0    | 0.524 | 6.012 | 66.6 | 5.5605 | 5   | 311 |
| 8  | 0.14455 | 12.5 | 7.87  | 0    | 0.524 | 6.172 | 96.1 | 5.9505 | 5   | 311 |
| 9  | 0.21124 | 12.5 | 7.87  | 0    | 0.524 | 5.631 | 100  | 6.0821 | 5   | 311 |
| 10 | 0.17004 | 12.5 | 7.87  | 0    | 0.524 | 6.004 | 85.9 | 6.5921 | 5   | 311 |
| 11 | 0.22489 | 12.5 | 7.87  | 0    | 0.524 | 6.377 | 94.3 | 6.3467 | 5   | 311 |
| 12 | 0.11747 | 12.5 | 7.87  | 0    | 0.524 | 6.009 | 82.9 | 6.2267 | 5   | 311 |
| 13 | 0.09378 | 12.5 | 7.87  | 0    | 0.524 | 5.889 | 39   | 5.4509 | 5   | 311 |
| 14 | 0.62976 | 0    | 8.14  | 0    | 0.538 | 5.949 | 61.8 | 4.7075 | 4   | 307 |
| 15 | 0.63796 | 0    | 8.14  | 0    | 0.538 | 6.096 | 84.5 | 4.4619 | 4   | 307 |
| 16 | 0.62739 | 0    | 8.14  | 0    | 0.538 | 5.834 | 56.5 | 4.4986 | 4   | 307 |
| 17 | 1.05393 | 0    | 8.14  | 0    | 0.538 | 5.935 | 29.3 | 4.4986 | 4   | 307 |
| 18 | 0.7842  | 0    | 8.14  | 0    | 0.538 | 5.99  | 81.7 | 4.2579 | 4   | 307 |
| 19 | 0.80271 | 0    | 8.14  | 0    | 0.538 | 5.456 | 36.6 | 3.7965 | 4   | 307 |



```

> summary(Boston)
      crim          zn          indus          chas          nox
Min.   : 0.00632   Min.   : 0.00   Min.   : 0.46   Min.   :0.00000   Min.   :0.3850
1st Qu.: 0.08204   1st Qu.: 0.00   1st Qu.: 5.19   1st Qu.:0.00000   1st Qu.:0.4490
Median : 0.25651   Median : 0.00   Median : 9.69   Median :0.00000   Median :0.5380
Mean   : 3.61352   Mean   :11.36   Mean   :11.14   Mean   :0.06917   Mean   :0.5547
3rd Qu.: 3.67708   3rd Qu.:12.50   3rd Qu.:18.10   3rd Qu.:0.00000   3rd Qu.:0.6240
Max.   :88.97620   Max.   :100.00   Max.   :27.74   Max.   :1.00000   Max.   :0.8710

      rm          age          dis          rad          tax
Min.   :3.561   Min.   : 2.90   Min.   : 1.130   Min.   : 1.000   Min.   :187.0
1st Qu.:5.886   1st Qu.:45.02   1st Qu.: 2.100   1st Qu.: 4.000   1st Qu.:279.0
Median :6.208   Median :77.50   Median : 3.207   Median : 5.000   Median :330.0
Mean   :6.285   Mean   :68.57   Mean   : 3.795   Mean   : 9.549   Mean   :408.2
3rd Qu.:6.623   3rd Qu.:94.08   3rd Qu.: 5.188   3rd Qu.:24.000   3rd Qu.:666.0
Max.   :8.780   Max.   :100.00   Max.   :12.127   Max.   :24.000   Max.   :711.0

      ptratio      black      lstat      medv
Min.   :12.60   Min.   : 0.32   Min.   : 1.73   Min.   : 5.00
1st Qu.:17.40   1st Qu.:375.38   1st Qu.: 6.95   1st Qu.:17.02
Median :19.05   Median :391.44   Median :11.36   Median :21.20
Mean   :18.46   Mean   :356.67   Mean   :12.65   Mean   :22.53
3rd Qu.:20.20   3rd Qu.:396.23   3rd Qu.:16.95   3rd Qu.:25.00
Max.   :22.00   Max.   :396.90   Max.   :37.97   Max.   :50.00

```

**Step 2**(1 mark) Start by using the `lm()` function to fit a simple linear regression model, with `medv` as the response and `lstat` as the predictor. The basic syntax is `lm(y~x,data)`, where `y` is the response, `x` is the predictor, and `data` is the data set in which these two variables are kept. Do not forget to attach Boston data either by separate command or by option “`data`” in `lm` command.

### COMMAND:

```
fit <- lm(medv~lstat , data = Boston)
summary(fit)
```

### OUTPUT

```
> lm.fit=lm(medv~lstat,data=Boston)
> attach (Boston )
> |
```

**Step 3**(1 mark) Interpret the significance of regression model.

```
> fit <- lm(medv~lstat , data = Boston)
> summary(fit)
```

Call:

```
lm(formula = medv ~ lstat, data = Boston)
```

Residuals:

| Min     | 1Q     | Median | 3Q    | Max    |
|---------|--------|--------|-------|--------|
| -15.168 | -3.990 | -1.318 | 2.034 | 24.500 |

Coefficients:

|             | Estimate | Std. Error | t value | Pr(> t )   |
|-------------|----------|------------|---------|------------|
| (Intercept) | 34.55384 | 0.56263    | 61.41   | <2e-16 *** |
| lstat       | -0.95005 | 0.03873    | -24.53  | <2e-16 *** |

---

Signif. codes: 0 ‘\*\*\*’ 0.001 ‘\*\*’ 0.01 ‘\*’ 0.05 ‘.’ 0.1 ‘ ’ 1

Residual standard error: 6.216 on 504 degrees of freedom

Multiple R-squared: 0.5441, Adjusted R-squared: 0.5432

F-statistic: 601.6 on 1 and 504 DF, p-value: < 2.2e-16

### OBSERVATION

- **p-value** is **2.2e-16** which is very less than 0.05, so it is highly significant, P-value is less than 0.05, this will reject the null hypothesis.
- The T-statistic value must be greater than 2(or less than -2) which indicates the coefficient is significant with >95% coincidence.
- **t** value is significant for medv = 61.41
- **t** value is significant = -24.41

**Step 4**(1 mark) The model output list can be checked by using command `names`.

#### **OUTPUT**

```
> names(Boston)
 [1] "crim"    "zn"      "indus"   "chas"    "nox"     "rm"
 [7] "age"     "dis"     "rad"     "tax"     "ptratio" "black"
[13] "lstat"   "medv"
```

**Step 5**(2 mark) Plot `medv` and `lstat` scatter plot using the `plot()` command. Plot the least squares regression in red line using `abline()` functions, use width parameter `lwd` of regression line as 3. Report these two graphs.

#### **Command:**

```
attach(Boston)

plot(lstat, medv , main="Scatterplot",
     xlab="lstat", ylab="medv ")
```

```
pdf (" scatterplot1.pdf ")
```

```
plot(lstat, medv)
```

```
dev.off ()
```

#### **OUTPUT**

```
> plot(lstat, medv , main="Scatterplot",
+      xlab="lstat", ylab="medv ")
>
> pdf (" scatterplot1.pdf ")
> plot(lstat, medv)
> dev.off ()
RStudioGD
2
```

### **COMMAND**

```
attach(Boston)

plot(lstat, medv , main="Scatterplot",
      xlab="lstat ", ylab="medv ")

abline(lm(medv~lstat),lwd =3, col="red")

pdf (" scatterplot2.pdf ")

plot(lstat, medv ,col =" red ")

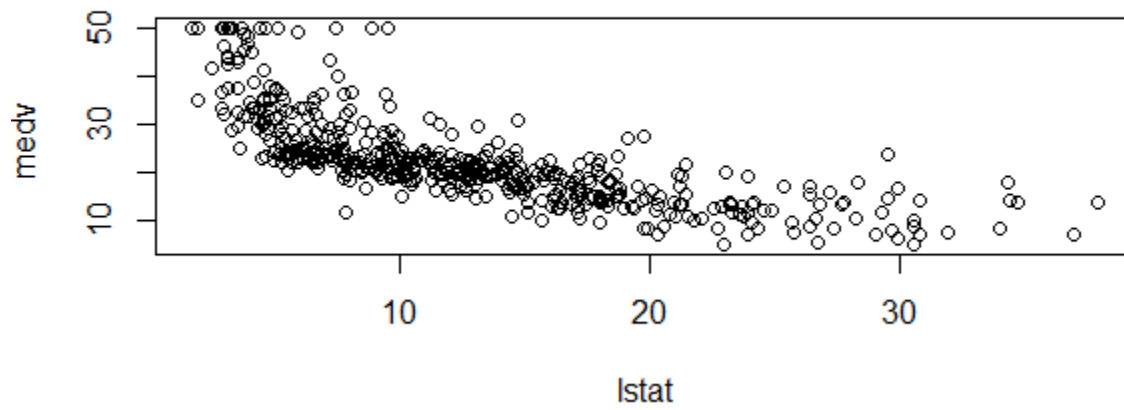
dev.off ()
```

### **Output:-**

```
> plot(lstat, medv , main="Scatterplot",
+      xlab="lstat ", ylab="medv ")
> abline(lm(medv~lstat),lwd =3, col="red")
>
> pdf (" scatterplot2.pdf ")
> plot(lstat, medv ,col =" red ")
> dev.off ()
RStudioGD
2
```

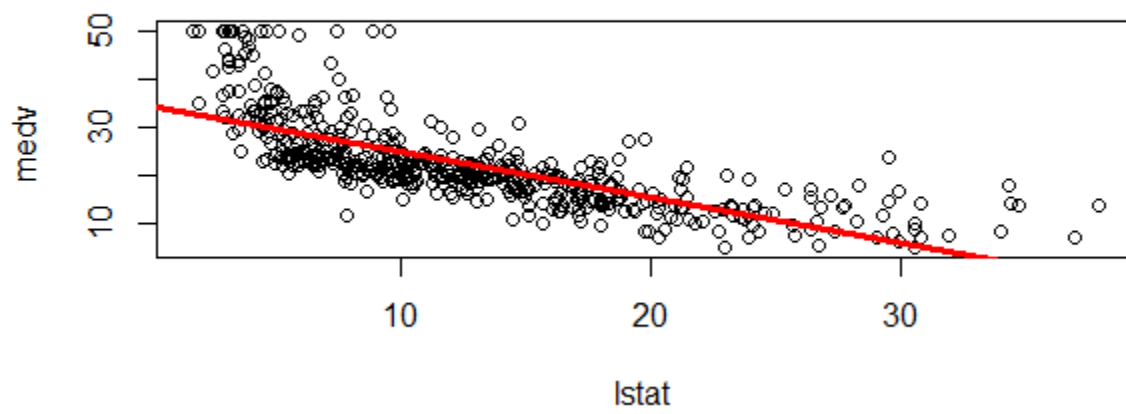
OUTPUT

**Scatterplot**



OUTPUT

**Scatterplot**



## Multiple linear regression

In order to fit a multiple linear regression model using least squares, we again use the `lm()` function. The syntax `lm(y~x1+x2+x3)` is used to fit a model with three predictors, `x1`, `x2`, and `x3`. The `summary()` function now outputs the regression coefficients for all the predictors.

**Step 1**(1 mark) Built the regression line of `medv` variable against `lstat` and `age`. Print the summary output of this regression model.

### COMMAND:

```
fit <- lm(medv~lstat+age, data = Boston)
summary(fit)
```

### OUTPUT

```
> fit <- lm(medv~lstat+age, data = Boston)
> summary(fit)

Call:
lm(formula = medv ~ lstat + age, data = Boston)

Residuals:
    Min       1Q   Median       3Q      Max
-15.981  -3.978  -1.283   1.968   23.158

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  33.22276    0.73085   45.458 < 2e-16 ***
lstat       -1.03207    0.04819  -21.416 < 2e-16 ***
age          0.03454    0.01223   2.826  0.00491 **
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.173 on 503 degrees of freedom
Multiple R-squared:  0.5513, Adjusted R-squared:  0.5495
F-statistic: 309 on 2 and 503 DF, p-value: < 2.2e-16
```

**Step 2**(1 mark) Analyze the overall significance of the model.

### OBSERVATION:

#### **R square Value:**

- R squares measures the variability of the data is captured by the Model.
- R-squares value = 0.5513(55.13%).

**F-value**

- F- statistic value is 309, which is larger than 1 and we can reject null hypothesis. Also it indicates that there would be relation between the response and predictors.

**Step 3**(1 mark) Analyze the significance of each individual coefficient.

**OBSERVATION:**

$$Y(\text{medv}) = 33.22276 - 1.03207 * \text{lstat} + 0.03454 * \text{age}$$

$\beta_0 = 33.22276$  =intercept. It is independent of any predictors.

$\beta_1 = -1.03207$ ; We can inferred that the response and the predictors are negatively correlated. If any of these will increases the other decreases.

$\beta_2 = 0.03454$ ; We can inferred that response and the predictors are positively correlated. If any of these will increases the other increases as well.