

Highly-tunable hot-electron distributions from scattering-mediated absorption

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Abstract

Light-initiated energetic electron transfer (EET) has attracted considerable attention as an emerging paradigm for photocatalysis and solar energy conversion, and the use of noble metal nanoparticles that support Localized Surface Plasmon Resonances (LSPR) has been widely explored as a medium for realizing this paradigm. It was recently shown that composite nanostructures that enable the interplay between dielectric scattering resonances and broad-band absorption in small metal nanostructures, a phenomenon termed scattering-mediated absorption, can be used to mediate EET and selective photochemistry with low-intensity light while completely circumventing plasmon excitation. This observation raises the question as to whether the energetic electrons derived from scattering mediated absorption have unique distributions and dynamics compared to their plasmon-derived counterparts, and if so, what implications these differences have for the efficiency and selectivity of EET. In this work, we develop a multi-scale modelling approach for elucidating the dynamics of energetic electrons derived from scattering mediated absorption and from plasmon excitation. We show that populations and dynamics of energetic electrons derived from scattering mediated absorption can be tuned via simple geometric parameters of the composite structures, and also suggest that in a variety of circumstances, energetic electron generation may be more efficient via scattering mediated absorption than by plasmon excitation under the same illumination conditions.

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Introduction

Various strategies that exploit the optical properties of metal nanoparticles, namely their ability to support localized surface plasmons resonances (LSPR, which are collective oscillations of their conduction electrons driven by visible light), have been explored recently with the aim of using low-intensity light to efficiently drive chemical reactions.¹⁻⁴ The interest in this area has been motivated partly by the fact that metal nanoparticles (most prominently silver and gold) are exceptionally good absorbers of visible light, so they are ideal candidates for harvesting solar photons.⁵ Importantly, the resonant properties of plasmonic particles are highly tunable by parameters under synthetic control such as geometry, composition, surface chemistry, and the surrounding environment.⁶⁻⁸ An emerging paradigm that exploits LSPR for photocatalysis is known as Plasmon-mediated Hot-Electron Transfer (PHET), and a growing number of reports are demonstrating the ability of PHET to catalyze energetically demanding chemical reactions.⁹⁻¹⁶ In PHET, the collective plasmon excitation decays rapidly (on a 10 femtosecond timescale) to a non-equilibrium distribution of energetic electron-hole pairs, or a so-called hot-electron distribution^{2,17-21} Hot-electrons can deposit energy into reactive degrees of freedom of molecules adsorbed to the nanoparticle surface, thereby initiating chemical transformations. Despite the considerable progress made in demonstrating the potential of the paradigm of PHET, its widespread application faces several challenges. The intrinsic optical properties of noble metals that give rise to the extraordinarily large absorption cross sections associated with LSPR are also fundamentally related to the broad energy spectra and short lifetimes associated with LSPR and the subsequent hot-electron distributions.²² Furthermore, the timescale of hot-electron relaxation competes with transfer to adsorbate states (both occur on 100 fs timescales), which fundamentally limits the efficiency of energy transfer.¹⁹ Finally, the most promising plasmonic materials typically have poor catalytic activity, and similarly, good catalytic metals typically are poor light harvesters.¹⁵

Considering this, an incredible opportunity exists to identify new classes of structures for mediating light-matter interactions and energy transfer events that offer the same advan-

tages as metal nanoparticles, namely exceptional light-harvesting potential, while also offering greater selectivity and efficiency in energy transfer, as well as tunable surface chemistry for enhanced catalytic activity. Ideally, such structures could be made mostly, if not entirely, from cost-effective materials. Recent progress towards this aim has been made by designing hybrid nanostructures that effectively delegate the light-harvesting and catalytic functions to separate components of the structure. Recently, Halas and co-workers demonstrated an antenna-reactor concept that leverages the nearfield enhancement from aluminum plasmons to generate energetic carriers on palladium islands and showed the efficacy of this strategy for the photocatalytic transformation of acetylene to ethylene.¹⁵ Two of the current authors, along with Sun and co-workers, demonstrated a phenomena known as scattering-mediated absorption where dielectric scattering resonances in SiO₂ nanospheres were utilized to induce resonant absorption in non-plasmonic platinum nanoparticles in SiO₂/Pt nanohybrids.¹³ The scattering-mediated absorption (SMA) phenomena was also observed to induce highly selective photocatalytic oxidation of benzyl alcohol to benzaldehyde.¹³ Zhang *et al.* independently described a SMA phenomenon in Au-TiO₂ nanohybrids that leveraged so-called whispering gallery modes to enhance plasmonic and non-plasmonic absorption in gold nanoparticles, and demonstrated these structures efficacy for photocatalytic water splitting.¹⁴ Interestingly, hot-carrier transfer was implicated in the photocatalytic mechanisms that resulted from these SMA phenomena.^{13,14} The prospect of using SMA in hybrid dielectric/metal nanostructures to initiate hot-carrier generation and transfer is particularly compelling as it could completely circumvent plasmon excitation. Not only does this open up possibilities to utilize a broader palette of materials, it also presents the possibility of realizing unique photocatalytic pathways owing to differences in the distributions and dynamics of energetic carriers produced by SMA compared to those produced by plasmon excitation.

The push to identify novel structures for mediating hot-carrier generation and transfer has been paralleled by efforts to develop theoretical methodologies to elucidate these processes. The underlying electronic structure has been treated both within free-electron models con-

fined by potential wells^{17,23–26} (here called "particle-in-a-well (PIW) models), as well as by *ab initio* approaches.^{18,20,21,27} Using PIW models, Govorov and co-workers developed a theory of hot-electron generation within the framework of time-dependent perturbation theory that has elucidated a variety of shape- and size-dependent factors for optimizing the hot-carrier generation.^{17,23} A similar approach was also pursued by Kumarasinghe *et al.* suggesting that nanorods are exceptionally good structures for hot-carrier generation.²⁵ García de Abajo and co-workers recently described a quantum master equation approach with an underlying PIW model that elucidated a number of key factors that influence hot-carrier excitation and decay dynamics.²⁶ The utilization of *ab initio* approaches by Sundararaman *et al* has also provided valuable insights into the role that a metals bandstructure plays in determining the efficiency of hot-carrier generation, and particularly in the asymmetry between hot-electron and hot-hole generation.¹⁸ Nordlander and co-workers have directly compared free-electron and *ab initio* approaches and found negligible impact on hot-carrier generation and dynamics in Ag nanospheres resulting from electron correlation,²⁴ though Bernardi *et al* have demonstrated that many-body effects are important in the hot-carrier dynamics resulting from surface plasmon polaritons in gold and silver.²⁷

We develop an novel approach for studying hot-carrier dynamics that may arise from arbitrary electromagnetic fields, including the unique nearfields that arise from SMA on hybrid dielectric-metal nanoparticles and plasmon resonance on noble metal nanoparticles. We consider the electronic degrees of freedom on the metal nanoparticle subject to the time-dependent Hamiltonian

$$\hat{H}(t) = \hat{H}_{el} - \mathbf{E}(t) \cdot \hat{\boldsymbol{\mu}}, \quad (1)$$

where the specific form of $\mathbf{E}(t)$ derives from a rigorous time-domain electrodynamics calculation with a realistic model of the nanostructure in question and \hat{H}_{el} describes non-interacting electrons confined by an infinite potential well. Through appropriate choice of the shape of the potential well, nanocubes and nanospheres are modelled. We compute the time-domain field using a commercial simulator based on the finite-difference time-domain method;²⁸ more

details are given in the supplemental information.

The many-electron wavefunction of the metal nanoparticles is expanded in terms of a configuration-interaction expansion that includes all singly-excited configurations,

$$|\Psi_{CIS}\rangle = c_0|\Phi_0\rangle + \sum_{i,a} c_i^a |\Phi_i^a\rangle, \quad (2)$$

where the configuration $|\Phi_i^a\rangle$ has an electron excited from orbital i to orbital a , and c_0 and c_i^a are complex expansion coefficients. Unless otherwise specified, indices i, j will indicate orbitals which are occupied in the ground state reference configuration and indices a, b will indicate orbitals which are unoccupied in the ground state reference.

The time-evolution of the wavefunction can be subsumed in the expansion coefficients, which allows the TDSE to be written

$$i\hbar \frac{d}{dt} \mathbf{c}(t) = \mathbf{H}(t) \mathbf{c}(t) \quad (3)$$

where $\mathbf{c}(t)$ is the vector of complex expansion coefficients and $\mathbf{H}(t)$ is the time-dependent Hamiltonian matrix. The Hamiltonian matrix is comprised of three unique blocks in the CIS model,

$$\mathbf{H}(t) = \begin{pmatrix} \langle \Phi_0 | \hat{H}(t) | \Phi_0 \rangle & \langle \Phi_0 | \hat{H}(t) | \Phi_i^a \rangle \\ \langle \Phi_j^b | \hat{H}(t) | \Phi_0 \rangle & \langle \Phi_j^b | \hat{H}(t) | \Phi_i^a \rangle \end{pmatrix}. \quad (4)$$

Explicit expressions for Hamiltonian matrix elements are given for both the nanocube and nanosphere models in the supplemental information. Given the simplicity of the underlying electronic Hamiltonian, the field-free Hamiltonian matrix is diagonal, and only the dipolar interaction of the nanoparticle with the external field can induce transitions among the electronic configurations, hence the treatment in this work neglects excited-state decay contributions from electron-electron scattering. These contributions will be explored in future work. The multiplication of the Hamiltonian matrix on the coefficient vector generates the gradient of the coefficient vector in time, and a variety of algorithms are known that use

this information to propagate the wavefunction in time. Here we use a symplectic integrator described in Ref. 29.

We analyze the hot-carrier distribution and dynamics that results from SMA and plasmon excitation by computing the instantaneous populations of orbitals both above and below the Fermi level of the metal nanostructure. In our model, the orbitals are energy eigenstates of a 1-electron Hamiltonian and have well-defined kinetic energy, and the orbital populations are given by the diagonal elements of the 1-electron reduced density matrix,

$${}^1D_q^q(t) = \langle \Psi(t) | \hat{a}_q^\dagger \hat{a}_q | \Psi(t) \rangle, \quad (5)$$

where the second-quantized operator \hat{a}_q^\dagger (\hat{a}_q) creates (kills) an electron in orbital q . The orbital indices can be uniquely mapped to the relevant orbital quantum numbers (n_x, n_y, n_z for the nanocube model, n, l, m for the nanosphere model) so that the orbital energies can be readily computed.

Methods

Electronic structure of metal nanospheres

For spherical metal nanoparticles, we approximate the one-electron orbitals as energy eigenstates of the particle-in-a-spherical-well. For a particle confined by a spherical well with radius R , the potential is 0 when $r < R$ and infinity with $r \geq R$, so that only kinetic energy contributes to the energetics. The energy eigenstates have the form^{22,30}

$$\psi_{n,l,m}(r, \theta, \phi) = j_l(\alpha r) Y_{l,m}(\theta, \phi), \quad (6)$$

where $j_l(\alpha r)$ are the spherical Bessel functions and $Y_{l,m}(\theta, \phi)$ are the spherical Harmonics. In our numerical implementation, we use the asymptotic approximation of the spherical Bessel functions $j_l(\alpha r) \approx \cos(\alpha r - \frac{\pi}{2}(l+1))/r$. To evaluate the spherical harmonics, we use a

recursive algorithm described in Ref. 31 to evaluate the associated Legendre polynomials. The energy eigenfunctions must vanish at $r = R$, which leads to the following form for the one-electron orbitals:

$$\psi_{n,l,m}(r, \theta, \phi) = \frac{2}{\sqrt{R}} \frac{\cos\left(\frac{\pi}{2}(2n+2+l)\frac{r}{R} - \frac{\pi}{2}(l+1)\right)}{r} Y_{l,m}(\theta, \phi). \quad (7)$$

The energy eigenvalues have the form

$$E_{n,l} = \frac{\hbar^2 \pi^2}{8mR^2} (2n+l+2)^2. \quad (8)$$

From the definition of the spherical polar coordinates, the x , y , and z components of the transition dipole integrals have the form

$$\langle \mu_x \rangle = \int_0^R \int_0^{2\pi} \int_0^\pi \psi_{n,l,m}^* \hat{\mu}_x \psi_{n',l',m'} r^2 \sin\theta \, dr \, d\theta \, d\phi \quad (9)$$

$$\langle \mu_y \rangle = \int_0^R \int_0^{2\pi} \int_0^\pi \psi_{n,l,m}^* \hat{\mu}_y \psi_{n',l',m'} r^2 \sin\theta \, dr \, d\theta \, d\phi \quad (10)$$

$$\langle \mu_z \rangle = \int_0^R \int_0^{2\pi} \int_0^\pi \psi_{n,l,m}^* \hat{\mu}_z \psi_{n',l',m'} r^2 \sin\theta \, dr \, d\theta \, d\phi, \quad (11)$$

where $\hat{\mu}_x = -e \cdot r \cdot \sin\theta \cos\phi$, $\hat{\mu}_y = -e \cdot r \cdot \sin\theta \sin\phi$, $\hat{\mu}_z = -e \cdot r \cdot \cos\theta$, and e is the charge of the electron.

In this work, we neglect the x and y components of the field and evaluate μ_z numerically, where the integral can be simplified to

$$\langle \mu_z \rangle = \delta_{m,m'} \cdot 2\pi \cdot \int_0^R \int_0^{2\pi} j_{n,l}(\alpha r) P_{n,l}(\cos\theta) \hat{\mu}_z j_{n',l'}(\alpha r) P_{n',l'}(\cos\theta) r^2 \sin\theta \, dr \, d\theta, \quad (12)$$

where $j_{n,l}(\alpha r)$ denotes the asymptotic approximation to the Spherical Bessel Function (written explicitly in Eq.) and $P_{n,l}(\cos\theta)$ denotes the associated Legendre polynomial.

Electronic structure of metal nanocubes

For cubic metal nanoparticles, we approximate the one-electron orbitals as energy eigenstates of the particle-in-a-cubic-well. For a particle confined by a cubic well with length L , the potential is 0 when $x < L, y < L, z < L$ and infinity otherwise. The energy eigenstates have the form

$$\psi_{nx,ny,nz} = \left(\frac{2}{L}\right)^{3/2} \sin\left(\frac{n_x \pi x}{L}\right) \sin\left(\frac{n_y \pi y}{L}\right) \sin\left(\frac{n_z \pi z}{L}\right). \quad (13)$$

The energy eigenvalues have the form

$$E_{nx,ny,nz} = \frac{\hbar^2 \pi^2}{2 m L^2} (n_x^2 + n_y^2 + n_z^2). \quad (14)$$

The transition dipole integrals can be evaluated analytically,

$$\begin{aligned} \langle \psi_{nx,ny,nz} | \hat{\mu}_x | \psi_{nx',ny',nz'} \rangle &= e \delta_{ny,ny'} \delta_{nz,nz'} \frac{L(\pi(n_x - n'_x)\sin(\pi(n_x - n'_x)) + \cos(\pi(n_x - n'_x)) - 1)}{\pi^2(n_x - n'_x)^2} \\ &\quad - e \delta_{ny,ny'} \delta_{nz,nz'} \frac{L(\pi(n_x + n'_x)\sin(\pi(n_x + n'_x)) + \cos(\pi(n_x + n'_x)) - 1)}{\pi^2(n_x + n'_x)^2} \end{aligned}$$

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