STAT 6021: Project Two

Medical Insurnace Costs

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1 Executive Summary:

The growing issue of higher medical costs per family has become a big concern to Americans. Increasing healthcare costs stop people from getting the needed care or fill prescriptions. Many families have difficulty in affording healthcare costs and this difficulty in paying bills has significant consequences for US families.

We selected a personal medical costs dataset. We want to explore what demographic characteristics affect the medical charges each family potentially pays in a year. So, we have considered Medical Cost Personal Dataset.

Dataset: datasets_13720_18513_insurance.csv

- The variables are as follows
 - Predictors
 - * x1: age: age of primary beneficiary.
 - * x2: sex: insurance contractor gender, female, male.
 - * x3: bmi: Body mass index, providing an understanding of body, weights that are relatively high or low relative to height, objective index of body weight (kg / m ^ 2) using the ratio of height to weight, ideally 18.5 to 24.9.
 - * x4: children: Number of children covered by health insurance / Number of dependents.
 - * x5: smoker: Smoking
 - * x6: region: the beneficiary's residential area in the US, northeast, southeast, southeast, northwest.
 - Response Variable
 - * Y: charges: Individual medical costs billed by health insurance.
- The main objectives for this project are -
 - 1. Explore relationship between response variable **charges** & the six other predictor variables (x1-x6).
 - 2. Analyze the correlation and directionality of the dataset.
 - 3. Create a model a best fit model to predict the insurance **charges** based the demographic predictor variables and evaluate the validity and usefulness of this model.

Additionally, we plan to utilize model selection tools to give us a deeper understanding of how different potential models compare. We want to recommend a best fit model and end our section by exploring the pros and cons of our models under consideration.

2 Exploratory Data Analysis:

We start our exploratory data analysis by taking a look at the dataset.

```
bmi children smoker
                                                 charges
  age
         sex
                                       region
  19 female 27.900
                                ves southwest 16884.924
                                 no southeast 1725.552
  18
2
       male 33.770
                           1
3
  28
       male 33.000
                           3
                                 no southeast 4449.462
4
  33
       male 22.705
                           Λ
                                 no northwest 21984.471
  32
       male 28.880
                                 no northwest 3866.855
5
  31 female 25.740
                                 no southeast 3756.622
                           0
```

Our dataset looks clean and has no missing values.

At a glance, we have six predictors and a response variable **charges**. The dataset has 1338 rows, and non of the columns are missing values.

```
'data.frame': 1338 obs. of 7 variables:

$ age : int 19 18 28 33 32 31 46 37 37 60 ...

$ sex : Factor w/ 2 levels "female", "male": 1 2 2 2 2 1 1 1 2 1 ...

$ bmi : num 27.9 33.8 33 22.7 28.9 ...

$ children: int 0 1 3 0 0 0 1 3 2 0 ...

$ smoker : Factor w/ 2 levels "no", "yes": 2 1 1 1 1 1 1 1 1 1 1 ...

$ region : Factor w/ 4 levels "northeast", "northwest", ..: 4 3 3 2 2 3 3 2 1 2 ...

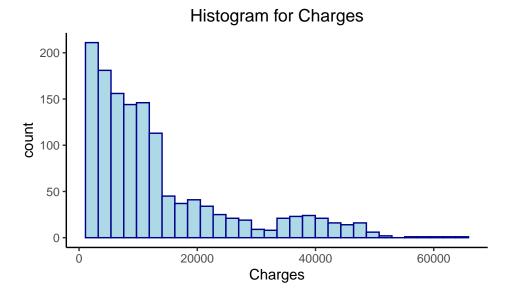
$ charges : num 16885 1726 4449 21984 3867 ...
```

The predictor variables **sex**, **smoker**, and **region** are categorical variables. They are automatically converted as a factor by R when loading the dataset, if you use the option **stringsAsFactors** = **TRUE** while reading the CSV file.

```
age
                     sex
                                    bmi
                                                   children
                                                                 smoker
Min.
       :18.00
                 female:662
                               Min.
                                      :15.96
                                                Min.
                                                        :0.000
                                                                 no:1064
1st Qu.:27.00
                 male :676
                               1st Qu.:26.30
                                                1st Qu.:0.000
                                                                 yes: 274
Median :39.00
                               Median :30.40
                                                Median :1.000
Mean
       :39.21
                               Mean
                                       :30.66
                                                Mean
                                                        :1.095
3rd Qu.:51.00
                               3rd Qu.:34.69
                                                3rd Qu.:2.000
Max.
       :64.00
                               Max.
                                      :53.13
                                                Max.
                                                        :5.000
      region
                    charges
northeast:324
                        : 1122
                 Min.
northwest:325
                 1st Qu.: 4740
southeast:364
                 Median: 9382
southwest:325
                 Mean
                         :13270
                 3rd Qu.:16640
                         :63770
                 Max.
  Min. 1st Qu.
                 Median
                            Mean 3rd Qu.
                                             Max.
  1122
           4740
                   9382
                           13270
                                   16640
                                            63770
```

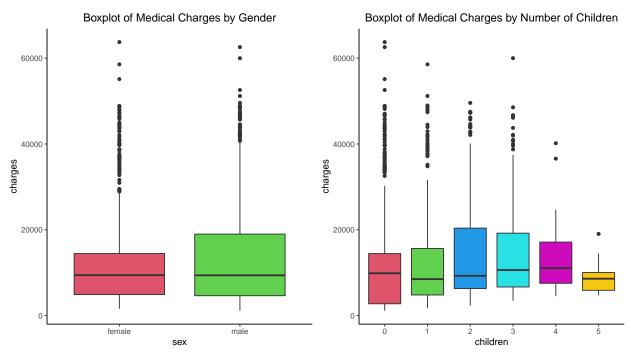
- From the summary, we can make the following observations :
 - The observations are evenly distributed across all four regions and sex.
 - The age varies between a low of 18 and a max of 64.
 - The dataset has almost 4:1 non-smoker to smoker ratio or only 20.5% of people smoke.
 - The bmi varies between a min of 15.96 and a max of 53.13.

The mean of the response variable is greater than the median of the response variable* that data is right-skewed, also seen in the histogram of charges shown below.



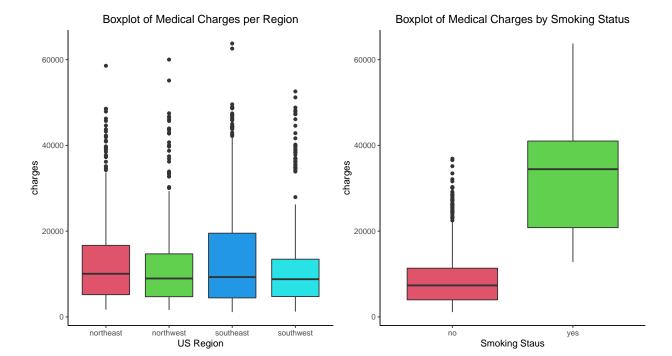
From the boxplot of medical **charges** by **sex**, we see that the median value of the **charges** for both males and females is almost the same. However, males tend to have higher medical expenses than females.

From the boxplot of medical **charges** by **children**, we can make an interesting observation that the medical **charges** for people with five children are less than compared to people with one to four children.



Similarly, the median value of charges across all four regions appears to have the same value. The people in the southeast seem to have higher medical expenses then the people in the other areas.

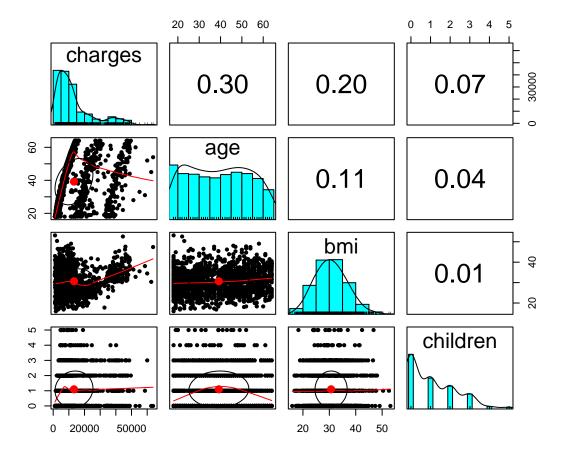
However, exploring the boxplot of medical **charges** by **smoking** status, we see that the medical **charges** for those who smoke are much higher than those who do not smoke.



The Correlation matrix:

	charges	age	bmi	children
charges	1.00000000	0.2990082	0.1983410	0.06799823
age	0.29900819	1.0000000	0.1092719	0.04246900
bmi	0.19834097	0.1092719	1.0000000	0.01275890
children	0.06799823	0.0424690	0.0127589	1.00000000

We see **age** and **charges** are moderately correlated, meaning as age increases, the medical charges also increase moderately. There is also a moderate correlation between **age** and **bmi**, and **children** and **charges**



Computational Exploration One of our project goals is finding the best fit model, but we did not find a strong correlation between the response and predictor variables. So we will search for candidate models applying model automatic predictor search procedures.

We will use the R^2_{adj} and the BIC metrics to identify likely models since these both penalize for adding more terms.

- Following are the two Automatic search procedure recommended models -
 - The model with lowest BIC is: $chareges = B_0 + B_1(age) + B_2(bmi) + B_3(children) + B_4(somkeyes)$
 - From the above, we see that our model with the lowest BIC (-1817.233) is the simple regression of age, bmi, children, smokeyes against charges.
 - The model with highest adjusted R^2 is **chareges** = $B_0 + B_1(age) + B_2(bmi) + B_3(children) + B_4(somkeyes) + B_5(regions outheast) + B_6(regions outhwest)$
 - The model with the highest adjusted R² is age, bmi,children,smokeyes,regionsoutheast, and regionsouthwest against medical charges.

We also considered the models with the highest R^2 , lowest Cp, and lowest MSE values. The best Cp and best MSE are both on the same model as the best adjusted R^2 .

The model with the best \mathbb{R}^2 value has all predictors as adjusted \mathbb{R}^2 in addition to regionnorthwest

Summary of Exploratory Data Analysis: We can make following observations from the exploratory data analysis:

- 1. The smokers have more medical expenses than non-smokers
- 2. None of the correlations from the correlation matrix appear to be strong
- 3. The quantitative predictors age, bmi, and children are moderately correlated with response variable
- 4. From computational analysis, we observed that categorical variable sex and region may be considred as significant predictors.
- 5. And we think that we are dealing with skewed dataset, particularly charges

3. Initial Model Considered:

Based on results from the model search procedures, we will will consider our **initial model to be one with the highest adjusted R².

```
initalmodel <- lm(charges ~ age + bmi + children + smoker + region +sex, data=data)
summary(initalmodel)</pre>
```

Call:

```
lm(formula = charges ~ age + bmi + children + smoker + region +
    sex, data = data)
```

Residuals:

```
Min 1Q Median 3Q Max
-11304.9 -2848.1 -982.1 1393.9 29992.8
```

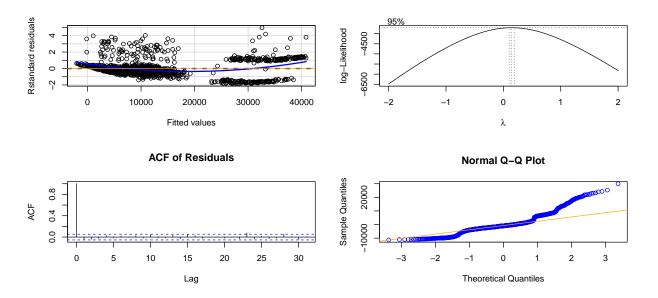
Coefficients:

	Estimate Std.	Error	t value	Pr(> t)	
(Intercept)	-11938.5	987.8	-12.086	< 2e-16	***
age	256.9	11.9	21.587	< 2e-16	***
bmi	339.2	28.6	11.860	< 2e-16	***
children	475.5	137.8	3.451	0.000577	***
smokeryes	23848.5	413.1	57.723	< 2e-16	***
regionnorthwest	-353.0	476.3	-0.741	0.458769	
regionsoutheast	-1035.0	478.7	-2.162	0.030782	*
regionsouthwest	-960.0	477.9	-2.009	0.044765	*
sexmale	-131.3	332.9	-0.394	0.693348	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6062 on 1329 degrees of freedom Multiple R-squared: 0.7509, Adjusted R-squared: 0.7494 F-statistic: 500.8 on 8 and 1329 DF, p-value: < 2.2e-16

Validating linear regression assumptions:



Looking at the above plots, we observe :

- 1. ** variance is not constant, as seen in the box-cox plot** and
- 2. ** non-linearity, as seen in the residual plot.

To fix non-constant variance and non-linearity issues, we will transform y first and the then predictors.

In our hypothesis, we said that old age people, people who smoke, and people with high bmi (bmi>30) might be at high risk. So their medical costs may be higher, based on that hypothesis, and considering that our initial model suffers from non-linearity and non-constant variance issues. We will transform both the response variable and the predictors.

Aligned to our Hypothesis and based on EDA, we will - 1. Transform **charges** (y) to fix non-constant variance 2. Transform age (x1) - by adding a non-linear term for age 3. Create a indicator variable for bmi (obesity indicator) (new categorical predictor) 4. Add and interaction term between smokers and bmi indicator predictor

[1] TRUE

Call:

```
lm(formula = charges^0.15 ~ age + age2 + children + bmi + sex +
bmi30 * smoker + region, data = data)
```

Residuals:

```
Min 1Q Median 3Q Max -0.4167 -0.1094 -0.0469 0.0192 1.3158
```

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	2.816e+00	7.348e-02	38.323	< 2e-16 ***	
age	2.428e-02	3.226e-03	7.527	9.53e-14 ***	
age2	-6.299e-05	4.024e-05	-1.565	0.117753	
children	5.109e-02	5.710e-03	8.948	< 2e-16 ***	
bmi	4.007e-03	1.848e-03	2.169	0.030288 *	
sexmale	-4.518e-02	1.318e-02	-3.429	0.000625 ***	
bmi301	-2.074e-02	2.280e-02	-0.910	0.363243	

```
smokerves
                  7.202e-01
                             2.372e-02
                                        30.360 < 2e-16 ***
regionnorthwest
                 -3.253e-02
                             1.883e-02
                                        -1.727 0.084396
regionsoutheast
                 -8.001e-02
                             1.896e-02
regionsouthwest
                 -7.718e-02
                             1.890e-02
                                        -4.083 4.71e-05 ***
bmi301:smokeryes
                  4.531e-01
                             3.261e-02
                                        13.896
```

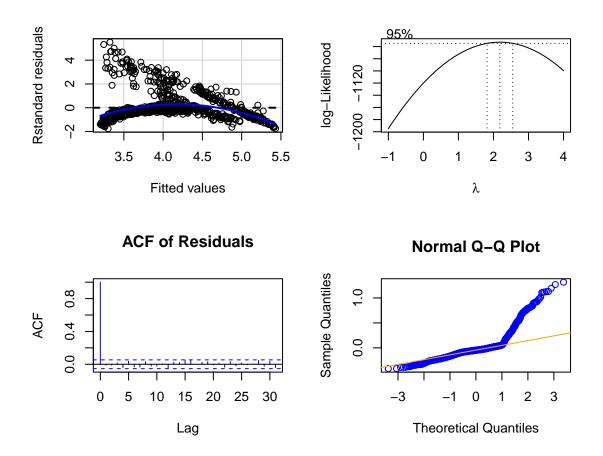
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2397 on 1326 degrees of freedom Multiple R-squared: 0.8063, Adjusted R-squared: 0.8047 F-statistic: 501.9 on 11 and 1326 DF, p-value: < 2.2e-16

Multiple R^2 and Adjusted R^2 measure how well our model explains the response variable. The transformed model has higher Multiple $R^2=0.8063$ and Adjusted $R^2=0.8047$ compared to initial model Multiple $R^2=0.7509$ and Adjusted $R^2=0.7494$

We also observe from the model summary, age2 the second order variable is insignificant based on t value and high p-value greater than 0.05. The interaction term bmi301:somkeryes is significant.

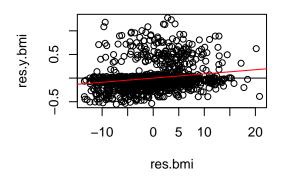
we now verify the linear regression model assumptions:

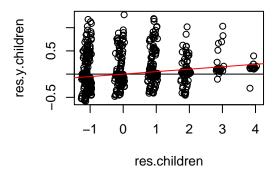


The bob-cox plot now shows that the non-constant variance issue is fixed. However, from the residual plot, it is not clear have solved the non-constant and non-linearity problem. So next, we explore which predictors can be removed by creating partial regression plots.

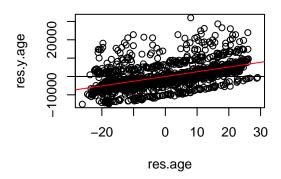
parital regression plot of bmi

parital regression plot of children





parital regression plot of age



Coefficients:

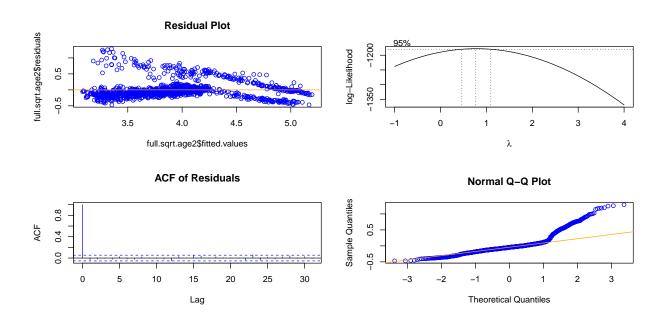
From the above partial regression plots, we still see a leaner pattern for all three quantitative variables, this means the linear terms for the predictors **bmi**, **age** and **children** is appropriate.

```
1338 obs. of 9 variables:
'data.frame':
           : int 19 18 28 33 32 31 46 37 37 60 ...
 $ age
 $ sex
           : Factor w/ 2 levels "female", "male": 1 2 2 2 2 1 1 1 2 1 \dots
           : num 27.9 33.8 33 22.7 28.9 ...
 $ children: int 0 1 3 0 0 0 1 3 2 0 ...
 $ smoker : Factor w/ 2 levels "no", "yes": 2 1 1 1 1 1 1 1 1 1 ...
 $ region : Factor w/ 4 levels "northeast", "northwest",..: 4 3 3 2 2 3 3 2 1 2 ...
 $ charges : num 16885 1726 4449 21984 3867 ...
 $ age2
           : num 361 324 784 1089 1024 ...
           : Factor w/ 2 levels "0", "1": 1 2 2 1 1 1 2 1 1 1 ...
Call:
lm(formula = charges^0.15 ~ log(age) + children + log(bmi) +
    smoker + region, data = data)
Residuals:
               1Q
                    Median
                                 3Q
                                         Max
-0.47069 -0.13211 -0.04842 0.04722 1.28840
```

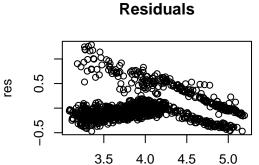
```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
                 0.318640
                            0.133283
                                       2.391 0.016955 *
log(age)
                 0.685523
                            0.018340 37.379 < 2e-16 ***
children
                 0.041804
                            0.005906
                                       7.078 2.36e-12 ***
log(bmi)
                 0.286829
                            0.036637
                                       7.829 9.98e-15 ***
smokeryes
                 0.955017
                            0.017604 54.249
                                              < 2e-16 ***
regionnorthwest -0.035919
                            0.020353
                                      -1.765 0.077820 .
regionsoutheast -0.085747
                            0.020425
                                      -4.198 2.87e-05 ***
regionsouthwest -0.073450
                            0.020434
                                      -3.595 0.000337 ***
```

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

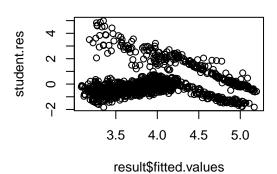
Residual standard error: 0.259 on 1330 degrees of freedom Multiple R-squared: 0.7731, Adjusted R-squared: 0.7719 F-statistic: 647.3 on 7 and 1330 DF, p-value: < 2.2e-16



[1] 3.529468



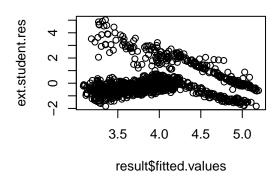
Studentized Residuals

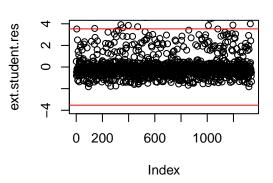


Externally Studentized Residuals

result\$fitted.values

Externally Studentized Residuals



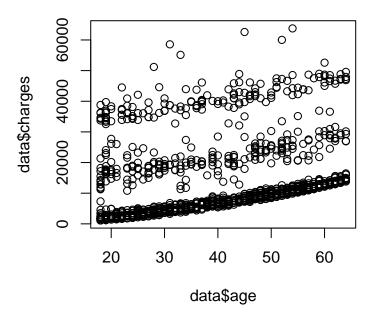


103	141	220	341	355	398	431	469
4.619736	3.570630	4.907768	3.915308	3.631488	3.850610	4.865511	3.728462
517	527	1009	1020	1028	1040	1196	1329
5.031708	4.585884	3.835164	4.450827	4.672036	4.535482	3.880408	3.997432

Even after applying transformations, the model fit is still not satisfying linear regression assumptions. We still see the presence of non-linearity and non-constant variance. It may be due to outliers in the data. This model is good enough to explore the relationship between the predictors and the response variable. However, the predicted values may be unrealistic.

And we notice that the simple scatter plot of charges against age has three distinct relationships, where the medical charges increase with age at a very slight increasing rate in three segments. Since this relationship is odd, we wish to explore if age is the reason for skew in the data.

plot(data\$age, data\$charges)



Suppose we remove age from the model and perform transformation on response variable. The bob-cox plot suggests non-constant variance, however when we carefully inspect the residual plot we still non-linearity and suspect non-constant variance is not addressed completely.

```
without.age <- lm(charges^.35 ~ + children + smoker + sex + region + bmi, data=data)
summary(without.age)</pre>
```

Call:

lm(formula = charges^0.35 ~ +children + smoker + sex + region +
bmi, data = data)

Residuals:

Min 1Q Median 3Q Max -13.8671 -4.2115 0.0291 3.5759 17.5451

Coefficients:

	${\tt Estimate}$	Std. Error	t value	Pr(> t)	
(Intercept)	15.5451	0.7931	19.600	< 2e-16	***
children	0.7732	0.1192	6.485	1.25e-10	***
smokeryes	14.8532	0.3577	41.526	< 2e-16	***
sexmale	-0.5982	0.2882	-2.076	0.038119	*
regionnorthwest	-0.4948	0.4124	-1.200	0.230442	
regionsoutheast	-1.4895	0.4142	-3.596	0.000335	***
regionsouthwest	-1.0330	0.4138	-2.496	0.012675	*
bmi	0.2304	0.0246	9.367	< 2e-16	***

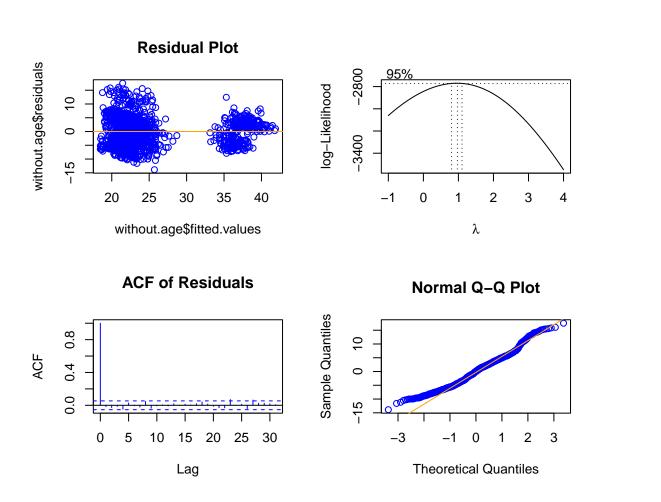
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.249 on 1330 degrees of freedom

```
Multiple R-squared: 0.5835, Adjusted R-squared: 0.5813
F-statistic: 266.2 on 7 and 1330 DF, p-value: < 2.2e-16
```

However, since age independently had the highest correlation with charges, the adjusted R-squared value falls to 0.5813 in the model without a period. Therefore, we do not believe it makes sense to use this model as a predictor, especially given the significant trade-off in predictability.

```
par(mfrow=c(2,2))
# without.age = without age and with y transformed to achieve lambda = 1 maximized
plot(without.age$fitted.values,without.age$residuals, main="Residual Plot", col='blue')
abline(h=0, col="orange")
boxcox.lambda <- boxcox(without.age, main = "Box-Cox", col='blue',lambda=seq(-1,4, by=0.1))
##ACF plot of residuals
acf(without.age$residuals, main="ACF of Residuals", col='blue')
##Normal probability or QQ plot of residuals
qqnorm(without.age$residuals, col='blue')
qqline(without.age$residuals, col="orange")</pre>
```



Initial Model Summary: We were able to increase the adjusted R^2 for our model by transforming the initial model we considered, however the non-constant variance and non-linearity issues in the data set were not fully addressed. So we acknowledged that our initial model could be used to explore the relationship between response and predictor variables. However, predictions may not be accurate.

4 Alternate Model Considered:

We would like to tweak our goal to find a model that predicts the charges to be above or below a certian threshold value. For the example above or below \$20,000. convert the problem domain to a logistic regress instead of linear regression.

we begin by converting the response variable to categorical variable and splitting the data into training & testing dataset

and then train the fitted model with the training dataset.

Call:

Deviance Residuals:

```
Min 1Q Median 3Q Max
-1.8184 -0.3834 -0.2428 -0.1373 3.1248
```

Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
                           1.07038 -7.399 1.37e-13 ***
(Intercept)
               -7.91973
                           0.01153
                                   3.428 0.000607 ***
age
                0.03953
                0.11077
                           0.02582
                                   4.289 1.79e-05 ***
bmi
smokeryes
                4.85604
                           0.37410 12.981 < 2e-16 ***
regionnorthwest 0.22102
                           0.44125
                                    0.501 0.616451
regionsoutheast -0.47459
                           0.41783 -1.136 0.256019
                           0.45047 -1.799 0.072008 .
regionsouthwest -0.81043
sexmale
                0.05906
                           0.30390
                                    0.194 0.845916
children
                0.03180
                           0.12272
                                   0.259 0.795552
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 664.52 on 668 degrees of freedom Residual deviance: 321.06 on 660 degrees of freedom
```

AIC: 339.06

Number of Fisher Scoring iterations: 6

The higher the difference between null deviance and residual deviance, the better the model's predictability. Our data supports' the claim that our logistic regression model is useful in estimating the log odds of whether medical **charges** are greater or less than \$20000

The model summary shows, based Z-value (Wald test) age, bmi, and smoker are significant predictors with a p-value of less than 0.05. Furthermore, the region sex and children predictors seem insignificant, hence removing the model.

```
hypothesis-testing H_0: coefficients for all predictors is = 0 and H_1: at least one coefficient is not zero
```

```
1-pchisq(lrmodel1$null.deviance - lrmodel1$deviance,8)
```

[1] 0

small p-value we reject the null hypothesis that at least one of these coefficients is not zero.

```
lrmodel2 <-glm(lrcharges ~ age + bmi + smoker, family="binomial" , data = lrdata_train)
summary(lrmodel2)</pre>
```

```
Call:
glm(formula = lrcharges ~ age + bmi + smoker, family = "binomial",
   data = lrdata train)
Deviance Residuals:
   Min
             1Q
                 Median
                               3Q
                                       Max
-1.7030 -0.3739 -0.2481 -0.1506
                                    3.1720
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
(Intercept) -7.86104 1.03377 -7.604 2.87e-14 ***
                       0.01150 3.554 0.000379 ***
            0.04087
age
                                4.111 3.94e-05 ***
            0.10134
                       0.02465
bmi
smokeryes
            4.75564
                       0.35844 13.268 < 2e-16 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 664.52 on 668 degrees of freedom
Residual deviance: 327.44 on 665 degrees of freedom
AIC: 335.44
```

We already know from the Wald test that the region sex and children predictors are insignificant, so we will conduct the delta G^2 test to see if these predictors can be removed from the model.

```
#test if additional predictors have coefficients equal to 0
1-pchisq(lrmodel2$deviance - lrmodel1$deviance,5)
```

[1] 0.2701389

Number of Fisher Scoring iterations: 6

p-value is 0.0941 greater than 0.05, so we cannot reject the null so that we will choose the simpler model with just the three predictors **age**, **bmi** and **smoker**.

Logistic Regression model validation Next, we will go over how well-chosen logistic regression model does in predicting an outcome that medical **charges** are greater than or less than \$20000 given the values of other predictors, using the probability of the observations in the test data of being in each class, we will choose a threshold of 0.5 for the confusion matrix.

False Positive Rate: When it's actually no, how often does it predict yes = 0.0625

False Negative Rate: When it's actually Yes, how often does it predict yes = 0.2198582

Sensitivity out of all the positive classes, how much we have predicted correctly = 0.7801418

Specificity determines the proportion of actual negatives that are correctly identified = 0.9375

The AUC value for our model is 0.8999704. The AUC value is higher than 0.5, which means the model does better than random guessing the classifying observations.

5. Conclusion:

- 1. Even after applying transformations, the model fit is still not satisfying linear regression assumptions.
- 2. We still see non-linearity, and non-constant variance issues are still not addressed in the model.
- 3. It could be due to skewed data or outliers in the dataset.
- 4. So we conclude that our initial transformed model is useful for exploring the relationship between predictor and response variables. However, the predicted values will be unreliable.

We recommend to go with the logistic regression model has better predictability.

$$\pi = \ln(P(\text{charges}>20000)==1)$$

$$\ln(\pi/(1-\pi)) = -7.86104 + 0.04087 \text{ (age)} + 0.10134 \text{ (bmi)} + 4.75564 \text{ (smokeryes)}$$

And the data is skewed when it comes to age & smokers, producing more balanced dataset may improve the predictability of our initial MLR model.