## AI Capstone HW3

## Minesweeper

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In this homework, we're asked to write a minesweeper game and use logical inference to build an AI that automatically play minesweeper game.

I wrote this homework using Python, in this report, I will first introduce the modules I create for this homework including module for literal, clause, knowledge base, game and player. And then talk about how to use logical inference technique, especially in this homework, resolution, to develop a AI for this game.

#### 1 Game Module

The code of Game Module can be referred to the appendix, Code 1. In this module, I implement some useful functions that will be later used in the development. I think the comments in code are clear enough to explain the code, therefore, I will not make further explanation regarding to this module. Noted that the <code>open\_cell</code> function means that marked that cell with mines or safe.

## 2 Logical Related Module

In this homework, we will need to use logical inference to solve the minesweeper game, thus we need to create modules that deal with logic. On the top of everything, we have a knowledge base (KB), which contains a set of logical statements or facts expressed in a formal language. These statements are represented using clauses, which are composed of a disjunction of literals.

For example, we could represent the fact that a cell is adjacent to a mine using a clause such as  $\neg A \lor B$  where A represents the safe cell and B represents the mine. We could also represent the fact that a cell does not contain a mine

using a clause such as  $(\neg A)$ , where  $\neg$  represents negation.

Literals are the building blocks of clauses and represent a proposition that is either true or false. In the context of the minesweeper game, we can represent each cell on the game board using a propositional symbol, where the symbol represents the proposition that the cell contains a mine or not. For example, "A" could represent the proposition that cell A contains a mine, while "¬A" represents the proposition that cell A does not contain a mine.

By using logical inference on the knowledge base and the rules of the game, we can deduce the state of the cells on the game board and determine which cells contain mines. This involves using techniques such as resolution to draw logical conclusions based on the knowledge base.

#### 2.1 Literal Module

The code can be referred to Code 2. Each literal contains two parts, the first part is the position of a certain cell, stores as a tuple, and a boolean posi indicates that whether this literal has negation or not. And because we will later store the literal in a set, we will need to define the hash function for any literal, in this homework, the hash function for literal is hash value of its string representation, the negation is indicated by a prime ('). For example, the literal of cell at position (x, y) with negation is (x, y)'

#### 2.2 Clause Module

The code for this module can be referred to Code 3. This module defines a Clause class that used a set to store literals in the clause. A clause is a disjunction of literals, where a literal is a basic proposition that is either true or false.

In this module, I defined some useful function, like str, which defined how to print a clause to console, and eq function, defined the equity of two clauses.

#### 2.3 Knowledge Base Module

The code of this module can be referred to Code 4. This module defines a KB class that represents a knowledge base, which is a collection of logical clauses. The knowledge base is used to store knowledge about a domain of interest and to perform logical inference to draw conclusions from that knowledge.

The init method initializes the KB object with a set of clauses. The insert method is used to insert a new clause into the knowledge base, while ensuring that the knowledge base remains consistent and does not contain redundant or contradictory information.

The insert method takes two parameters, a Clause object to be inserted and the KBØ object that contains the inferred clauses. The method first apply resolution to all clauses in KBØ, noted that KBØ stores all the clauses that has been already inferred and every clause is single-literal clause. This step decrease the number of literal in inserted clause. Then, it checks if the clause is already in the knowledge base, or if it is a superset of another clause in the knowledge base. If either of these conditions is true, the method returns without modifying the knowledge base. Otherwise, the clause is added to the knowledge base. And if any of clause in KB is a superset of inserted clause, then remove that clause.

The KB class is useful for representing and manipulating knowledge bases in logical inference systems. The insert method ensures that the knowledge base remains consistent and that new clauses are added in a way that preserves the logical structure of the knowledge base.

## 3 Player Module

The code of this module is Code 5. This module implements the AI that automatically play the minesweeper game, and inserted the clauses to KB by the given hint.

#### 3.1 Generate Clauses by Given Hint

A hint is made up of the positions of unmarked cell around the opened cell and the number of mines in those unmarked cell. Suppose the positions are  $x_1, x_2, ..., x_m$  and there are n mines in those m unmarked cell.<sup>1</sup> The inserted clauses are generated as follow:

- If n=m, then all the unmarked cells are mines. Therefore inserted  $(x_i)$  where i=1,2,...,m to KB.
- If n = 0, then all the unmarked cells are safe. Therefore inserted  $\neg(x_i)$  where i = 1, 2, ..., m to KB.
- If m > n > 0, which is the general case, inserted two types of clauses to KB.
  - 1. Inserted  $\binom{m}{m-n+1}$  clauses, each clause contains m-n+1 positive literal.
  - 2. Inserted  $\binom{m}{n+1}$  clauses, each clause contains n+1 positive literal.

The above results are given by pigeonhole theorem, for the first type, because there are only m-n safe cells, for any clause that contains more than m-n literals, it must have at least one literal that corresponds to mine cell, thus the whole clause will be true. Similarly, for the second type, there are only n mine cells, for any clause with more than n literals, it must contain at least one literal that corresponds to safe cell, thus the whole clause will be true. These two type of clauses are the essential of this logical inference, without those clauses, we can't get the correct results.

Noted that when inserting clause into KB, we follow the process mentioned in subsection 2.3.

#### 3.2 The Inference Process

The inference process is the main part of AI.

It first check if there are any single literal clause in  $\mathsf{KB}$ . If there contains any, that called it C, it move C to  $\mathsf{KBO}$ , which is the knowledge base that stores inferred clauses, and because C is single literal, which means we already know that the corresponded cell is a safe cell or mine. Thus, we can open the cell and get the hint if the cell is safe, then

 $<sup>^{1}</sup>x_{i}$  is a tuple

inserting new clause by the above process. And then, we can apply matching to every other clause in  $\mathsf{KB}$  with C. The matching process will be later described in subsection 3.3. Simply put, the matching process is to apply resolution to clauses and decrease the number of literal in clauses. Make the clause stricter.

If there doesn't contain any single literal clause, then apply pairwise matching to clauses in KB. These process is meant to generate single literal clauses eventually. If we can't get single literal clause for multiple iterations. Then the game is likely to be stuck, we can terminate the game play.

#### 3.3 The Matching Process

The matching process involves two clauses, let's called them a and b. we want to simplify a and b using resolution and merged into one clauses c.

It first checked whether a=b or  $a\subset b$  or  $b\subset a$ . If any of conditions hold, we can only leave one stricter clauses. If none of the conditions hold, we can enter next step, which is applying resolution to two clauses to generate new clause. Noted that because we don't want to make KB grow to fast, thus if the number of literals of a and b are both greater than 2. Then we don't apply resolution in matching process.

## 4 Experiments and Results

In this section, I will mainly discuss about the performance of our game AI, and analysis it.

First of all, because this AI is based on logical inference., when opening a cell, the AI is sure about whether it's a safe cell or mine. It means that the AI will never be wrong, it will only have two outcome, win or stuck. Win means correctly marked every cell. Stuck means the we can't have further inference.

And also, in order to increase the running performance, the results in this section are executed in PyPy. PyPy is an alternative implementation of the Python programming language that aims to be faster, more memory efficient, and more compatible with existing Python code than the standard CPython interpreter.

## 4.1 Performance of Different Difficulty

The board configuration of each difficulty is defined as in Table 1.

Table 1: The board configuration of each difficulty.

Difficulty	Board Size	Number of Mines
Easy	$9 \times 9$	10
Medium	$16 \times 16$	25
Hard	$16\!\times\!30$	99

The results below is running on my personal computer with single thread program. For each difficulty, I tested 5 games, and each game is running independently.

## 4.2 Performance of Different Number of Initial Safe Cell

At the beginning of the game, the game module would first give the player the positions of some initial safe cell. The default value for the number of these safe cells is  $\sqrt{\# \text{ of cell in board}}$ . In this section, I will test how this number effect the running time for the program. And because running this experiments with hard difficulty is time-consuming, I will run the experiment with medium difficulty.

The default value of initial safe cell is 16. I will change this number to 8, 16, 32, 64, 128 and 231. And measure the average running time of 5 games.

Table 2: The performance with different number of init safe cell. The parwise matching is the average number of running pairwise matching.

Init. Safe Cell	Win	Stuck	Avg. Time	Std. Time	Pairwise Matching
8	5	0	1.47	0.37	0.6
16	5	0	2.65	1.86	0.8
32	5	0	3.59	1.17	0
64	5	0	3.88	0.92	0
128	5	0	3.61	0.13	0
231	5	0	2.73	0.36	0

## 5 Conclusion and Future Work

In this section, I will mainly talk about the conclusion toward this homework, and some future work to improve the performance of this game AI.

First of all, this homework let me understand the concept of logical inference, and how it can apply to solve a real world problem. However, this method is quite time-consuming, because we need to apply resolution repeatedly to many clauses in knowledge base.

Therefore, for future work, I want to first improve the performance of my program. This program has much space to improve, including the data structure to store clauses and the matching process.

# Appendix A Code of Modules and Functions

Code 1: Game Module

```
1 class Game:
      def __init__(self, difficulty=0):
3
         Initialize the game board
4
5
         Parameters
         difficulty : int
9
            0: Easy, 1: Medium, 2: Hard
10
11
         Returns
12
13
         None
14
15
         board_configurations = [
             (9, 9, 10), # Easy
16
17
             (16, 16, 25), # Medium
             (16, 30, 99) # Hard
18
19
         self.h, self.w, self.num_of_mines
20
         → # height, width, number of mines
         self.board = [[0 for _
21

    in range(self.w)] for _ in range(self.h)]

         → # -1: mine, 0~8: number of mines around
         self.shown_cell = [[False for _
22
         → in range(self.w)] for _ in range(self.h)]

→ # Indicate the cell is opened or not
         self.mine_pos = set() # The position of mines
24
         # Randomly generate mines
25
26
         → len(self.mine_pos) < self.num_of_mines:</pre>
27
            i = random.randrange(self.h)
            j = random.randrange(self.w)
28
29
            if (i, j) not in self.mine_pos:
                self.mine_pos.add((i, j))
30
31
                self.board[i][j] = -1
32
33
      def open_cell(self, cell, safe):
34
         Open the cell
35
   \rightarrow and return the number of mines around the cell
36
37
         Parameters
38
         _____
39
         cell: tuple
```

```
The position of the cell
         safe : bool
41
42
             True
   \hookrightarrow if the cell is safe, False if the cell is a mine
         Returns
45
         int
46
47
             The number of mines
   → around the cell, return -1 if wrongly opened
         if ((cell in self.mine_pos) ^ (not safe))
49
         → or self.shown_cell[cell[0]][cell[1]]:
             return -1
50
         if cell not in self.mine pos:
52
             self.board[cell[0]][cell[1]]
             else:
53
             self.board[cell[0]][cell[1]] = "X"
55
         self.shown_cell[cell[0]][cell[1]] = True
56
57
         return self.board[cell[0]][cell[1]]
59
      def get_hint(self, cell):
60
61
         Get the hint of the cell
62
63
64
         Parameters
65
         cell: tuple
             The position of the cell
67
68
         Returns
69
70
71
72
             The list of the cells around the cell
73
             The number of mines around the cell
74
75
         cnt = 0
76
77
78
         for i in range(cell[0]-1, cell[0]+2):
             for j in range(cell[1]-1, cell[1]+2):
                if i < 0 or i
80
                \rightarrow >= self.h or j < 0 or j >= self.w:
                    continue
81
                if self.shown_cell[i][j]:
                   continue
83
                if (i, j) != cell:
85
                   if (i, j) in self.mine_pos:
                       cnt += 1
86
                   res.append((i, j))
```

```
return res, cnt
88
89
90
       def get_surround_mines(self, cell):
91
92
          Get the number of mines around the cell
93
94
          _____
95
96
          cell: tuple
97
              The position of the cell
98
          Returns
99
00
          _____
01
          int
02
              The number of mines around the cell
03
04
          cnt = 0
          for i in range(cell[0]-1, cell[0]+2):
05
              for j in range(cell[1]-1, cell[1]+2):
06
                 if (i, j) in self.mine_pos:
107
                     cnt += 1
.08
109
          return cnt
10
111
112
       def get_init_safe_cells(self):
113
          Get the initial safe cells
114
115
116
          Parameters
17
18
          None
19
          Returns
120
21
          _____
          set
122
123
              The set of the initial safe cells
124
25
          num = round(math.sqrt(self.h * self.w))
          \# num = 10
126
27
          init_cells = set()
          while len(init_cells) < num:</pre>
128
29
              i = random.randrange(self.h)
30
              j = random.randrange(self.w)
              if (i, j) not in self.mine_pos
131
              → and (i, j) not in init_cells:
                 init_cells.add((i, j))
32
33
34
          return init_cells
135
136
       def print_board(self):
```

```
Print the game board. ? means the cell

→ is not opened yet. X means the cell is a mine.

   → 0~8 means the number of mines around the cell.
139
          Parameters
140
          _____
41
142
          None
143
144
          Returns
45
          None
146
47
          os.system('cls')
148
          for i in range(self.h):
149
150
             for j in range(self.w):
                 if self.shown_cell[i][j]:
151
152
                     print(self.board[i][j], end=' ')
                 else:
53
                    print('?', end=' ')
             print()
155
```

Code 2: Literal Module

```
class Literal:
      A literal is a cell with a positive or
   \rightarrow negative sign. For example, (0, 0) is a positive
   \rightarrow literal, and (0, 0)' is a negative literal.
      def __init__(self, cell, is_posi):
 5
          Initialize the literal
          Parameters
9
          _____
11
          cell: tuple
12
             The position of the cell
13
          is posi : bool
             True if the literal
14

→ is positive, False if the literal is negative

15
16
          Returns
17
18
          None
19
          self.cell = cell
20
          self.posi = is_posi
21
22
      def __eq__(self, other):
23
24
25
          Check if two literals are the same
```

```
. . .
26
        return self.cell
27
        28
29
     def __str__(self):
30
31
        Return the string of the literal
32
33
        return str(self.cell)
        → + ('' if self.posi else "'")
34
35
     def __hash__(self):
36
        Return the hash value of the literal
37
38
39
        return hash(str(self))
```

Code 3: Clause Module

```
1 class Clause:
2
      A clause is a set of literals
3
4
      def __init__(self, literals=[]):
5
6
7
         Initialize the clause
8
         Parameters
9
10
          _____
         literals: list
11
12
            The list of literals
13
14
         Returns
15
16
         None
17
18
         self.literals = set(literals)
19
20
21
      def __str__(self):
22
23
         Return the string of the clause
24
         return "[" + ' '.join([str(1)
25

    for l in self.literals]) + "]"

26
      def __eq__(self, other):
27
28
         Check if two clauses are the same
29
30
31
         return self.literals == other.literals
```

```
32
      def __len__(self):
33
34
          Return the number of literals in the clause
35
36
          return len(self.literals)
37
38
      def __hash__(self):
39
40
41
          Return the hash value of the clause
42
          return hash(str(self))
43
44
      def __copy__(self):
45
46
47
          Return the copy of the clause
48
          return Clause(self.literals.copy())
49
```

Code 4: KB Module

```
1 class KB:
2
      A knowledge base is a set of clauses
3
4
      def __init__(self, clauses=set()):
5
 6
         Initialize the knowledge base
 8
         Parameters
9
10
         _____
11
         clauses : set
            The set of clauses
12
13
14
         Returns
15
16
         None
17
         self.clauses = clauses
18
19
      def insert(self, clause: Clause, KB0):
20
21
         Insert a clause into the knowledge base
22
23
         Parameters
24
25
         clause : Clause
26
             The clause to be inserted
27
         KB0 : KB
28
29
             The knowledge base that
       contains of claueses that are already inferred
```

```
30
31
        Returns
32
33
        None
34
        for clause1 in KBO.clauses:
35
           cell_pos = list(clause1.literals)[0].cell
36
            pos = list(clause1.literals)[0].posi
37
38
           for lit in clause.literals.copy():
               if lit.cell == cell pos and lit.posi !
39
               clause.literals.remove(lit)
40
41
        if len(clause.literals) == 0:
            return None
42
        if clause in self.clauses:
43
44
           return None
45
        for clause1 in self.clauses.copy():
           if clause1
46
            → .literals.issubset(clause.literals):
               return None
47
            elif clause
48

    .literals.issubset(clause1.literals):
49
               if clause1 in self.clauses:
                  self.clauses.remove(clause1)
50
        if clause in KBO.clauses or clause in self |
51
         return None
52
53
54
        if len(clause.literals) >= 1:
55
            self.clauses.add(clause)
        # print(f"insert {clause}")
56
        # print(f"[\n{','.join([str(c)
57

→ for c in self.clauses])}\n]")
```

#### Code 5: Player Module

```
class Player:
2
3
      The player class
4
      def __init__(self, game: Game):
5
6
         Initialize the player
7
9
         Parameters
10
11
          aame : Game
             The game to be played
12
13
14
          Returns
15
          _____
```

```
None
16
17
18
         self.game = game
19
         self.KB = KB(set())
         self.KB0 = KB(set())
20
         self.mine = set()
21
         self.safe = set()
22
         for i in self.game.get_init_safe_cells():
23
24
            self.safe.add(i)
25
            self.KB.insert(Clause([Literal(i,
            → False)]), self.KB0)
26
27
      def play(self):
28
29
         Play the game
30
31
         Parameters
32
33
         None
34
35
         Returns
36
37
         None
38
         unmarked_cnt = 0
39
         while unmarked_cnt <= 10:</pre>
40
            self.game.print_board()
41
            print(f"# in KB: {len(self.KB.clauses)},
42

    # in KB0: {len(self.KB0.clauses)}")

43
            # for clause in self.KB.clauses:
               print(clause, len(clause))
44
45
            # print("----")
            # for clause in self.KBO.clauses:
46
                print(clause)
            print(f"# single clause in

→ KB: {len([clause for clause in self | 
            updated = False
49
            if Clause([]) in self.KB.clauses:
50
               self.KB.clauses.remove(Clause([]))
51
            for clause in self.KB.clauses:
52
53
               if len(clause) == 1:
54
                  unmarked_cnt = 0
                  updated = True
55
                  lit = list(clause.literals)[0]
56
                  self.KB.clauses.remove(clause)
57
                  self.KB0
58

    .literals.copy()))
                  print(f"Open cell
59
                  if lit.posi:
60
```

```
for cell in comb:
                      if self.game.open_cell(lit |
                      62
                         print('Game Over!')
                                                                                              \hookrightarrow lits |
63
                         exit(0)
                                                                                              → .append(Literal(cell,
64
                      self.mine.add(lit.cell)
                                                                                              → True))
                  else:
                                                                                           self.KB
65
                      if self.game.open_cell(lit |
                                                                                           66

    self.KB0)

67
                         print('Game Over!')
                                                                                        for comb in
                         exit(0)
                                                                                        \hookrightarrow combinations(pos, n+1):
68
                      self.safe.add(lit.cell)
                                                                                           lits = []
                  # for clause1
                                                                                           for cell in comb:
70
                   → in self.KB.clauses.copy():
                       print(clause1)
                                                                                              \hookrightarrow \quad \textbf{lits} \mid
71
                  for clause1
                                                                                              → .append(Literal(cell,

    in self.KB.clauses.copy():
                                                                                              → False))
                      if clause1 in self.KB.clauses:
                                                                                           self.KB
                         self.KB
                                                                                           74

    self.KB0)

                                                                                 break
75
                                                                           if updated:
                                                              103
                                                                              continue
                                                              104
                                                                           KB_clause = list(self.KB.clauses.copy())

→ matching clauses(Clause(clause))

                                                              105
                                                                           print("entering pairwise matching")
                      unmarked_cnt += 1
                                                              06
                                                                           for idx, i in tqdm(enumerate(KB_clause)):
                                                              107
                                                                              for j in KB_clause[idx+1:]:
                         self.KB.insert(a, self.KB0)
                      if b:
                                                                                 if i in self.KB.clauses:
78
                                                              109
79
                         self.KB.insert(b, self.KB0)
                                                              110
                                                                                     self.KB.clauses.remove(i)
80
                                                              111
                                                                                 if j in self.KB.clauses:
                  if not lit.posi:
                                                                                     self.KB.clauses.remove(j)
81
                                                              112
                      pos, n = self |
                                                                                 if(len(i) == 0 or len(j) == 0):
82
                                                              113
                                                                                    continue
                      \hookrightarrow .game.get_hint(lit.cell)
                                                              114
                      # print(pos, n)
                                                                                 a, b = matching_clauses(Clause(i |
                                                              115
                      if len(pos) == n:
                                                                                 for i in pos:
                                                                                 86
                            \hookrightarrow self
                                                                                 if a:
                            \hookrightarrow . KB |
                                                                                    self.KB.insert(a, self.KB0)
                                                              118
                            → .insert(Clause([Literal(i,
                                                              119
                                                                                    if a != i and a != j:

    True)]), self.KB0)

                                                                                        # print(len(i),
                                                              120
                      elif n == 0:
                                                                                        \rightarrow len(j), i, j, a, b)
                         for i in pos:
                                                                                       updated = True
                                                                                 else:
                                                                                    # print(len(i),

    self |

                                                              123
                                                                                     \hookrightarrow Len(j), i, j, a, b)
                            \hookrightarrow . KB _{\parallel}
                            updated = True
                                                              124
                                                                                 if b:
                            → False)]), self.KB0)
                                                              125
                      else:
                                                                                    self.KB.insert(b, self.KB0)
                                                              126
90
                         for comb
                                                                                    if b != j and b != i:
                                                              127
                         # print(len(i),

    len(pos)-n+1):

                                                                                        \hookrightarrow len(j), i, j, a, b)
                                                                                        updated = True
                            lits = []
```

```
else:
30
                      # print(len(i),
131
                      \hookrightarrow Len(j), i, j, a, b)
                      updated = True
32
33
            if not updated:
34
               if len(self.KB0.clauses)
135
                36
                   print("Stuck")
37
               else:
                   print("Win!")
38
               exit(0)
39
         print("Stuck")
40
         exit(0)
```

Code 6: matching\_clauses Function

```
def matching_clauses(a: Clause, b: Clause):
      Check
3
   \rightarrow if two clauses can be matched using resolution
      Parameters
5
6
7
      a : Clause
         The first clause
      b : Clause
         The second clause
10
11
12
      Returns
      _____
13
14
      a : Clause
         The first clause after matching
15
      b : Clause
16
         The second clause after matching
17
18
      if a == b:
19
20
         return a, None
21
      if a.literals.issubset(b.literals):
22
          return a, None
23
24
      if b.literals.issubset(a.literals):
25
26
          return b, None
27
28
      if len(a) > 2 and len(b) > 2:
          return a, b
29
30
31
32
      comps = set()
33
      for i in a.literals:
```

```
for j in b.literals:
            if i.cell == j.cell and i.posi != j.posi:
35
36
               comps.add(i.cell)
37
      if len(comps) == 1:
38
         a = Clause(list(a.literals
         b = None
40
41
         for i in comps:
42
            if Literal(i, True) in a.literals:
43
               a.literals.remove(Literal(i, True))
            if Literal(i, False) in a.literals:
44
               a.literals.remove(Literal(i, False))
45
         return a, None
46
47
48
      return (a if len(a.literals) > 0 else
      → None), (b if len(b.literals) > 0 else None)
```

Code 7: Main function

```
1 if __name__ == "__main__":
      parser = argparse.ArgumentParser()
      parser.add_argument(
3
          "-d".
          "--difficulty",
          dest="difficulty",
          type=int,
          help="difficulty level

→ of the game 0: easy, 1: medium, 2: hard",

          default=0
9
10
      parser.add_argument(
11
          "-n",
12
          dest="n",
13
          type=int,
14
          help="number of games to play",
15
          default=1
16
17
      args = parser.parse_args()
18
19
      records = [] # win, time
      for i in range(args.n):
20
          game = Game(args.difficulty)
21
          start = time.time()
22
23
          player = Player(game)
24
          res = player.play()
          end = time.time()
25
          records.append((res, end-start))
26
      # Print status with windows
27
28
      print(f"Play {args.n}

    games with difficulty {args.difficulty}")
```

## Appendix B Complete Code

One can run this Python code by python main.py [-d difficulty]. Can also find the code from https://github.com/jayin92/NYCU-AI-Capstone/blob/main/hw3/src/main.py.