

# Computer Vision

Kuan-Wen Chen  
2022/3/3

# What's Computer Vision

Computer Vision vs. Computer Graphics

電腦視覺

計算機圖學

# Every picture tells a story



Goal of computer vision is to write computer programs that can interpret images

# Can computers match (or beat) human vision?



Yes and no (but mostly no!)

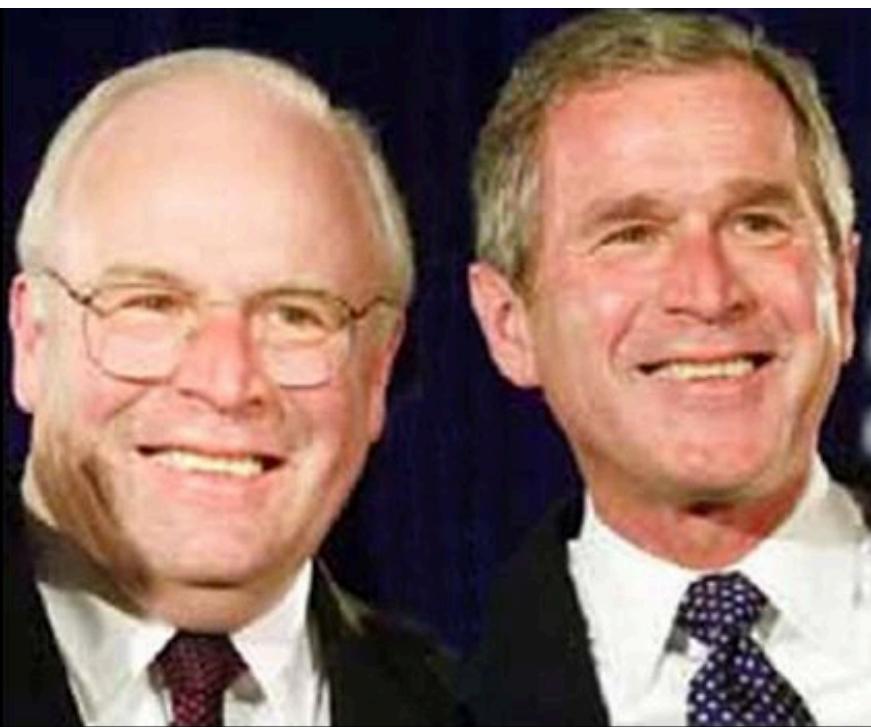
humans are much better at “hard” things  
computers can be better at “easy” things

# Human perception has its shortcomings...

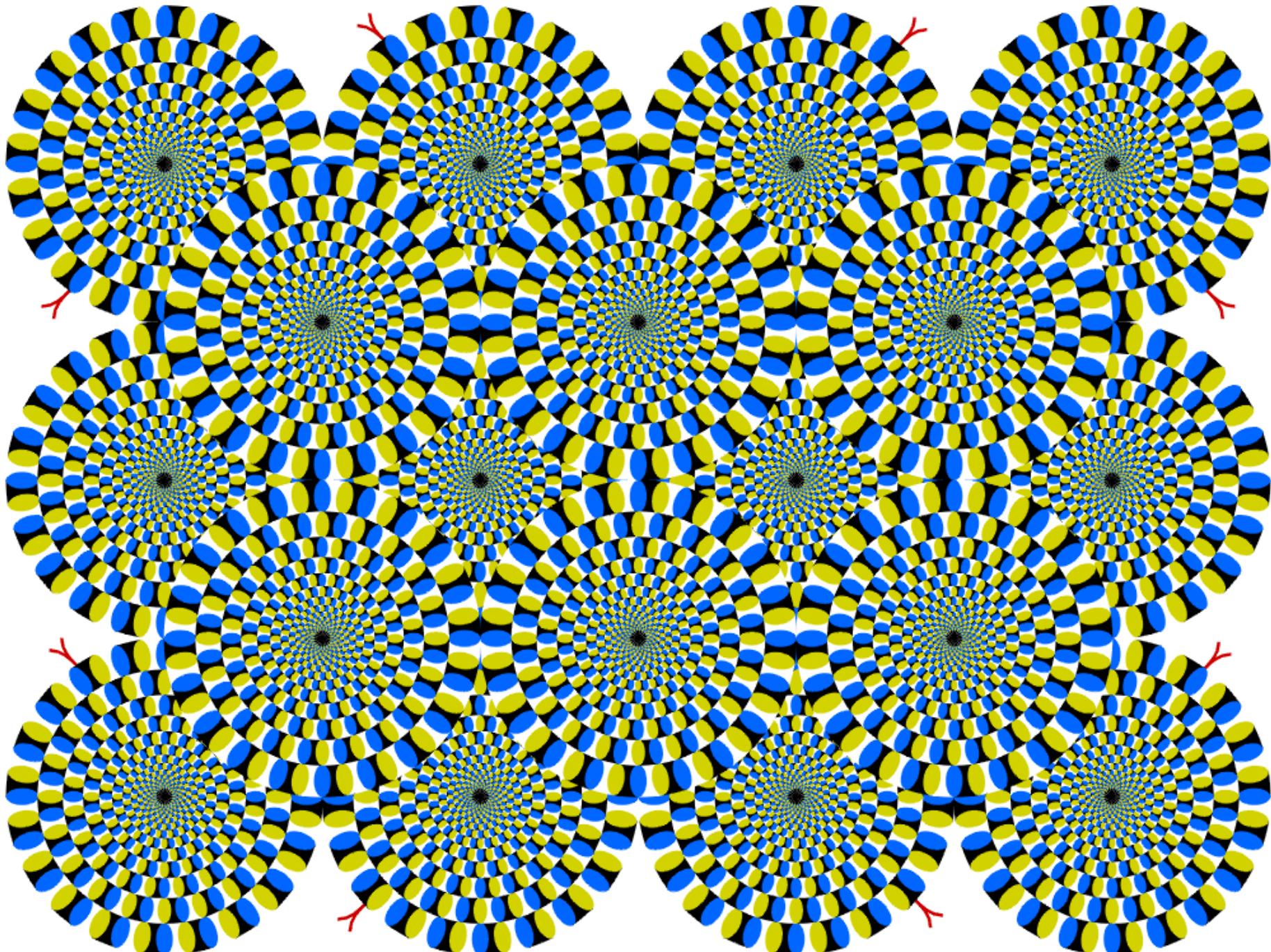


头条号 / 闻来达

# Human perception has its shortcomings...



Source: Sinha, Pawan, and Tomaso Poggio. "[I Think I Know That Face...](#)" *Nature* 384 (1996): 404. © 1996.



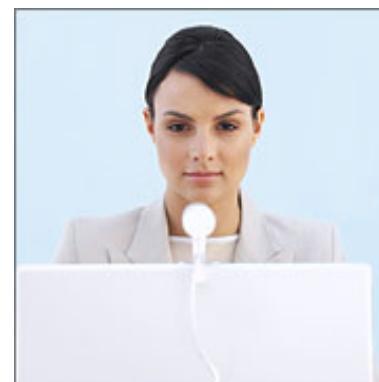
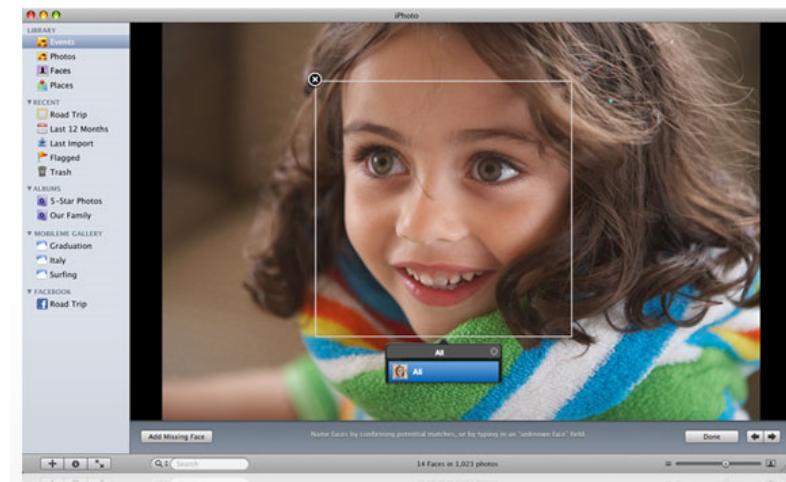
Copyright [A.Kitaoka](#) 2003

# What's Computer Vision

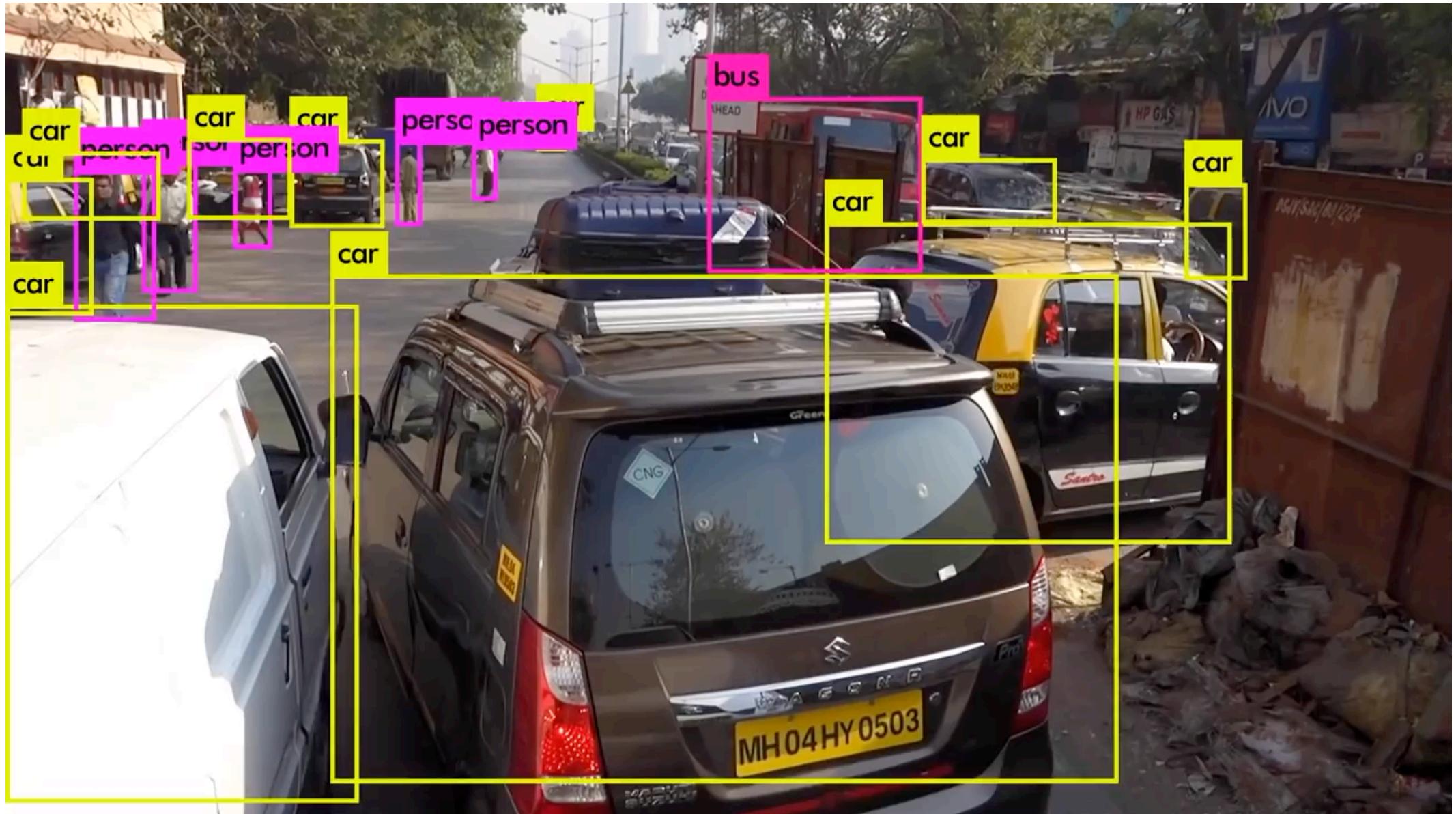
[following Slides from CSE/EE 576, @cs.washington.edu]

What Works Today?

# Face detection and recognition, Biometrics



# Object detection and recognition



# Self-driving Car



# Binary Machine Vision

# Introduction

- binary value 1: considered part of object
- binary value 0: background pixel
- binary machine vision: generation and analysis of binary image



# Thresholding

- $B(r,c) = 1$  if  $I(r,c) \geq T$
  - $B(r,c) = 0$  if  $I(r,c) < T$
- 
- $r$ : row,  $c$ : column
  - $I$ : grayscale intensity,  $B$ : binary intensity
  - $T$ : intensity threshold

# Thresholding

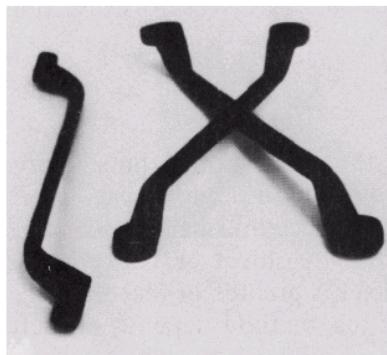


$T=128 \rightarrow$



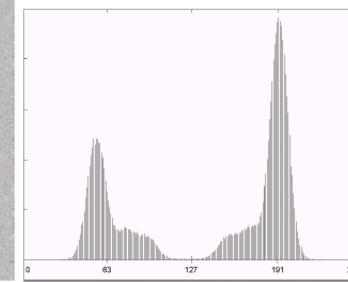
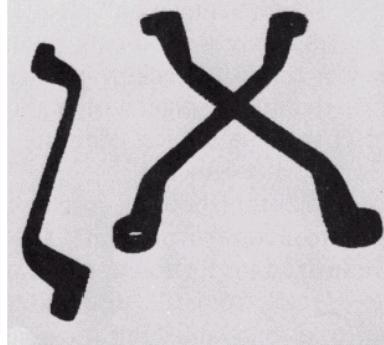
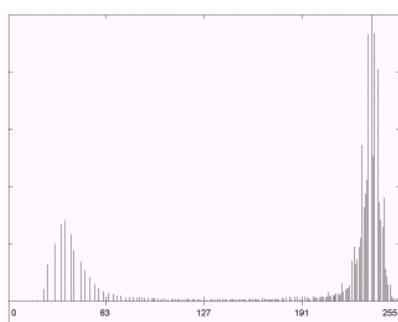
how to choose  $T$ ?

# Histogram Analysis for Image Thresholding



a  
b  
c

**FIGURE 10.28**  
(a) Original image.  
(b) Image histogram.  
(c) Result of global thresholding with  $T$  midway between the maximum and minimum gray levels.



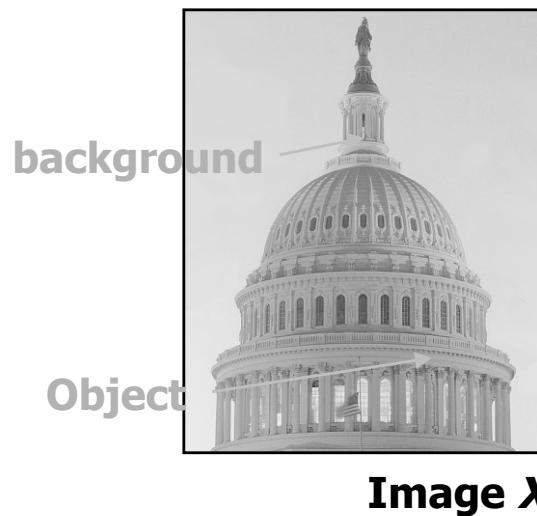
a  
b  
c

**FIGURE 10.29**  
(a) Original image.  
(b) Image histogram.  
(c) Result of segmentation with the threshold estimated by iteration.  
(Original courtesy of the National Institute of Standards and Technology.)

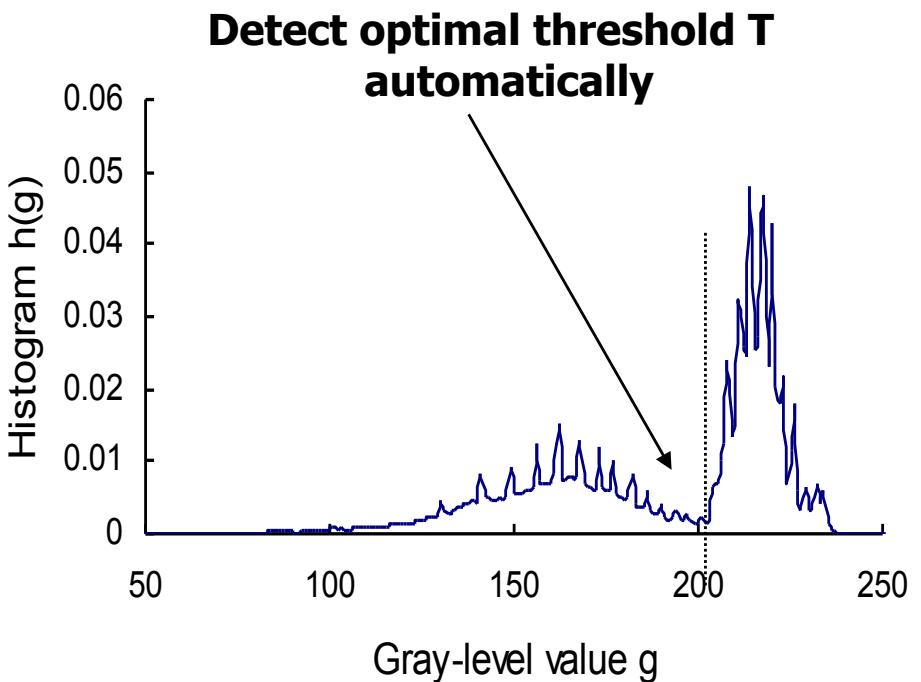
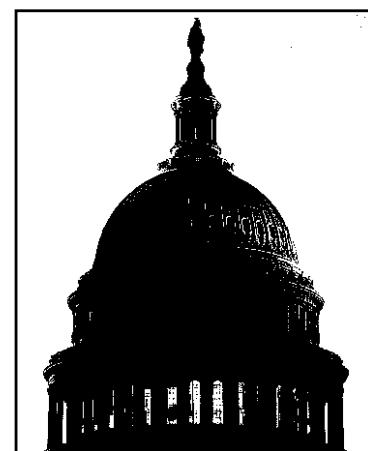


# Histogram Analysis for Image Thresholding

Example:

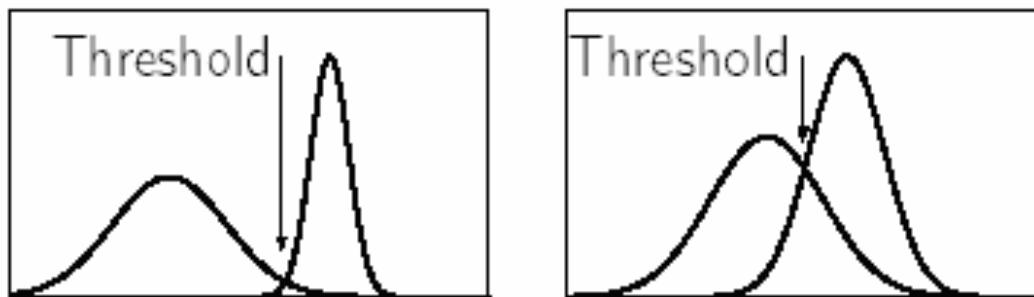


**Histogram**



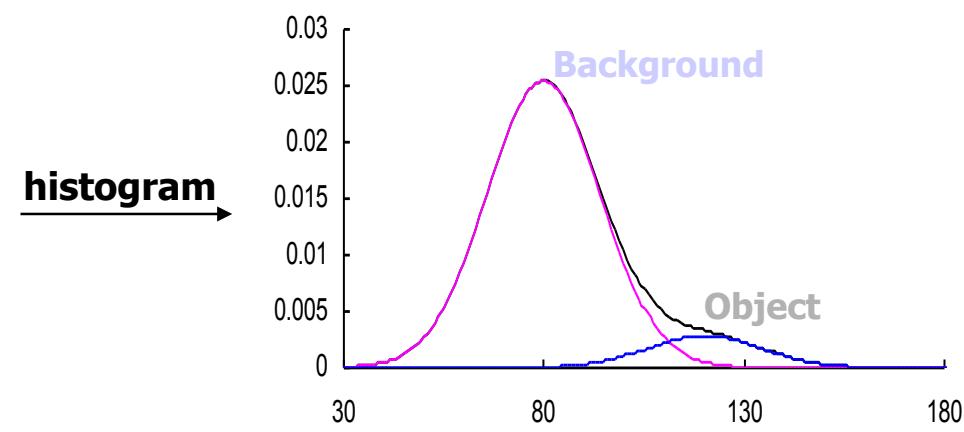
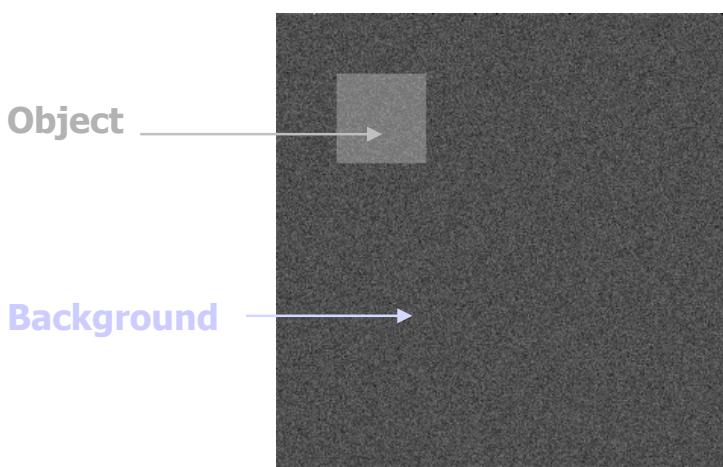
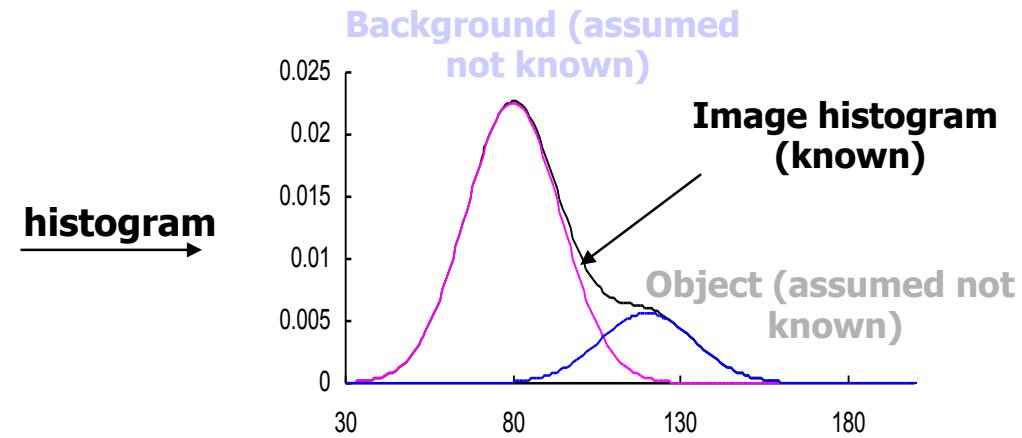
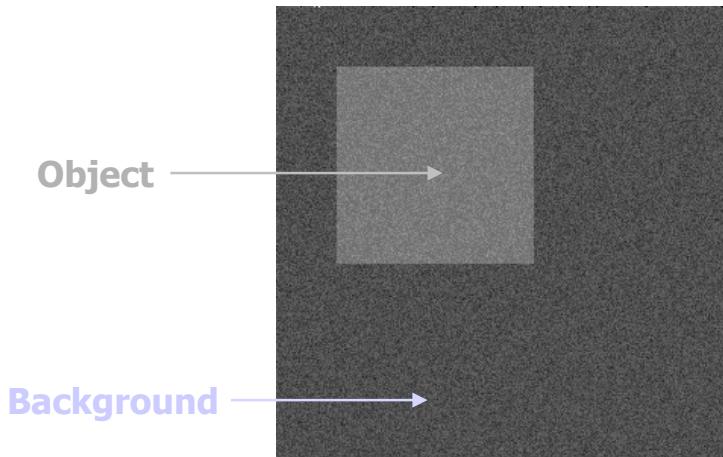
# Thresholding

- Histogram shape can be useful in locating the threshold.
  - However it is not reliable for threshold selection when peaks are not clearly resolved.
- Choosing a threshold in the valley between two overlapping peaks, and inevitably some pixels will be incorrectly classified by the thresholding.



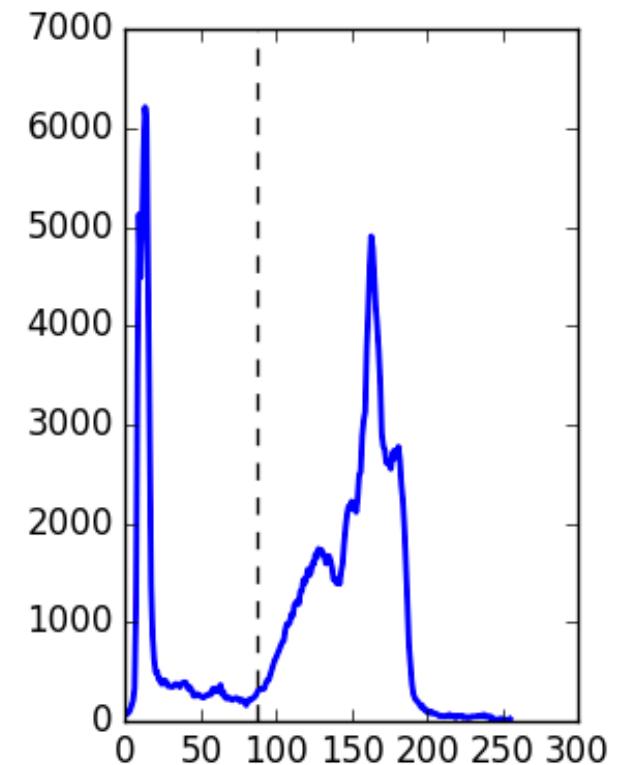
The determination of peaks and valleys is a non-trivial problem

# Sensitivity to object size



# Otsu Thresholding

Select a threshold that minimize the **within-class variance**



# Otsu Thresholding

- define the *within-class variance* as the weighted sum of the variances of each cluster:

$$\sigma_{\text{Within}}^2(T) = n_B(T)\sigma_B^2(T) + n_O(T)\sigma_O^2(T)$$



$$n_B(T) = \sum_{i=0}^{T-1} p(i)$$

$$n_O(T) = \sum_{i=T}^{N-1} p(i)$$

$\sigma_B^2(T)$  = the variance of the pixels in the background (below threshold)

$\sigma_O^2(T)$  = the variance of the pixels in the foreground (above threshold)

Minimize

# Otsu Thresholding

Minimize

$$\begin{aligned}\sigma_{\text{Between}}^2(T) &= \sigma^2 - \sigma_{\text{Within}}^2(T) \\ &= n_B(T) [\mu_B(T) - \mu]^2 + n_O(T) [\mu_O(T) - \mu]^2\end{aligned}$$

$\mu = n_B(T)\mu_B(T) + n_O(T)\mu_O(T)$

$\mu = n_B(T)\mu_B(T) + n_O(T)\mu_O(T)$

Maximize

$$\sigma_{\text{Between}}^2(T) = n_B(T)n_O(T)[\mu_B(T) - \mu_O(T)]^2$$

# Algorithm of Otsu Thresholding

Goal: select a  $T$  that maximizes  $n_B(T)n_O(T)[\mu_B(T) - \mu_O(T)]^2$

- For each potential threshold  $T$ ,
  1. Separate the pixels into two clusters according to the threshold.
  2. Find the mean of each cluster.
  3. Square the difference between the means.
  4. Multiply by the number of pixels in one cluster times the number in the other.

# An Computational Issue

- The computations aren't independent as we change from one threshold to another.
- We can incrementally update with the following equations:

$$n_B(T + 1) = n_B(T) + n_T$$

$$n_O(T + 1) = n_O(T) - n_T$$

$$\mu_B(T + 1) = \frac{\mu_B(T)n_B(T) + n_T T}{n_B(T + 1)}$$

$$\mu_O(T + 1) = \frac{\mu_O(T)n_O(T) - n_T T}{n_O(T + 1)}$$

# Connected Components Labeling

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- **Connected components analysis:**
  - connected components labeling of the binary-1 pixels
  - property measurement of the component regions
  - decision making



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- All pixels that have value binary-1 and are connected to each other by a path of pixels all with value binary-1 are given the same identifying **label**.

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- **connected components labeling**: a grouping operation

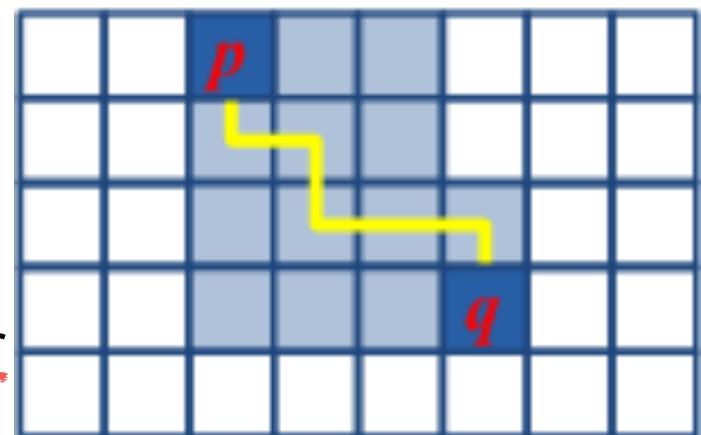
# Connected Components Labeling

- All pixels that have value binary-1 and are connected to each other by a path of pixels all with value binary-1 are given the same identifying **label**.
- **label**: unique name or index of the region
- **label**: identifier for a potential object region
- **connected components labeling**: a grouping operation
- **pixel property**: position, gray level or brightness level
- **region property**: shape, bounding box, position, intensity statistics

# Connected Components Operators

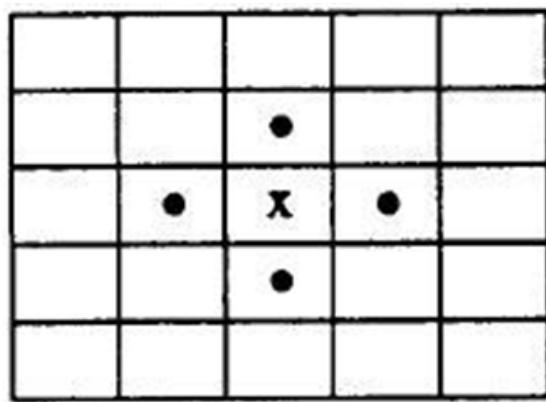
- Definition of Connected Component
  - Two pixels  $p$  and  $q$  belong to the same connected component  $C$  if there is a sequence of 1-pixels  $(p_0, p_1, \dots, p_n)$ , where
    - $p_0 = p$
    - $p_n = q$
    - $p_{i-1}, p_i : i = 1, \dots, n$  are neighbor

?

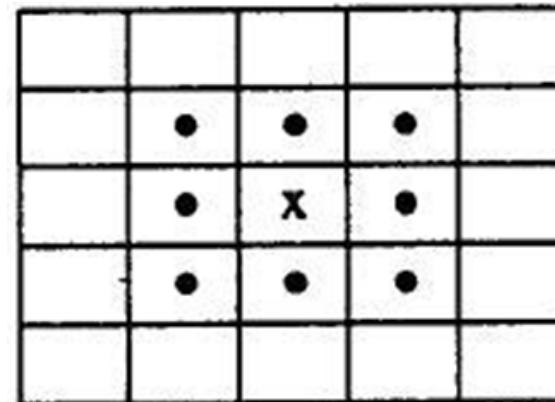


# Connected Components Operators

- 4-connected: north, south, east, west
- 8-connected: north, south, east, west, northeast, northwest, southeast, southwest



4-connected



8-connected

Border: subset of 1-pixels also adjacent to 0-pixels

# Connected Components Operators

0	1	1	0	1	0	0
0	1	1	0	1	0	1
1	1	1	0	1	0	1
0	0	0	0	1	1	1
0	1	0	0	0	0	0
0	1	1	1	1	1	0
0	1	1	1	0	0	0

Original Image

0	1	1	0	2	0	0
0	1	1	0	2	0	2
1	1	1	0	2	0	2
0	0	0	0	2	2	2
0	3	0	0	0	0	0
0	3	3	3	3	3	0
0	3	3	3	0	0	0

Connected Components

# Connected Components Algorithms

- Common Features
  - Process a row of image at a time
  - Assign a new labels to the first pixel of each component.
  - Propagate the label of a pixel to its neighbors to the right or below it.

0	0	1	0	0	0	1
0	0	1	1	0	0	1
0	0	1	1	1	0	1
0	0	1	1	1	1	1

0	0	1	0	0	0	2
0	0	1	1	0	0	2
0	0	1	1	1	0	2
0	0	1	1	1	1	A

# Connected Components Algorithms

- Common Features

0	0	1	0	0	0	1
0	0	1	1	0	0	1
0	0	1	1	1	0	1
0	0	1	1	1	1	1

0	0	1	0	0	0	2
0	0	1	1	0	0	2
0	0	1	1	1	0	2
0	0	1	1	1	1	A

- What label should be assigned to A
- How does the algorithm keep track of the equivalence of two labels
- How does the algorithm use the equivalence information to complete the processing

# Algorithm 1: Iterative Algorithm

- Algorithm Steps
  - Use no auxiliary storage
  - Computational Expensive
- Step1 (Initialization): Assign an unique label to each pixel.
- Step2 (Iteration) : Perform a sequence of top-down and bottom-up label propagation.

	1	1		1	1	
	1	1		1	1	
	1	1	1	1	1	

1	2		3	4	
5	6		7	8	
9	10	11	12	13	

	1	1		3	3	
	1	1		3	3	
	1	1	1	1	1	

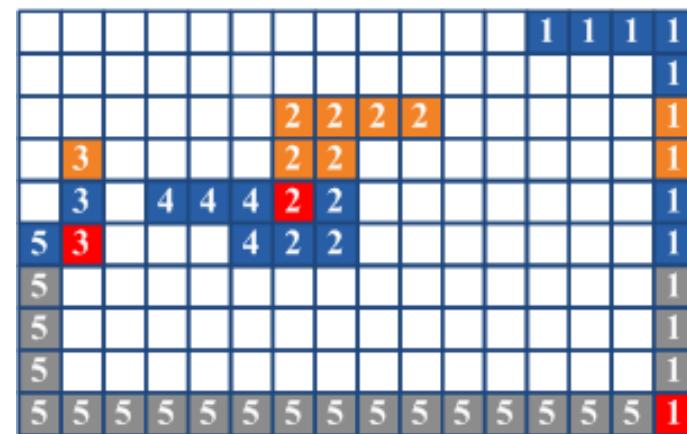
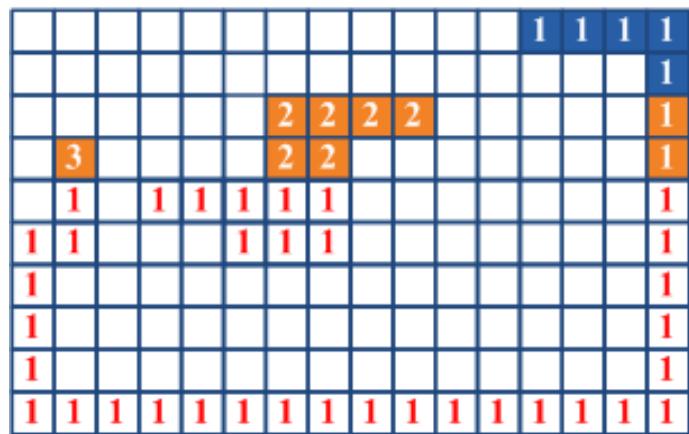
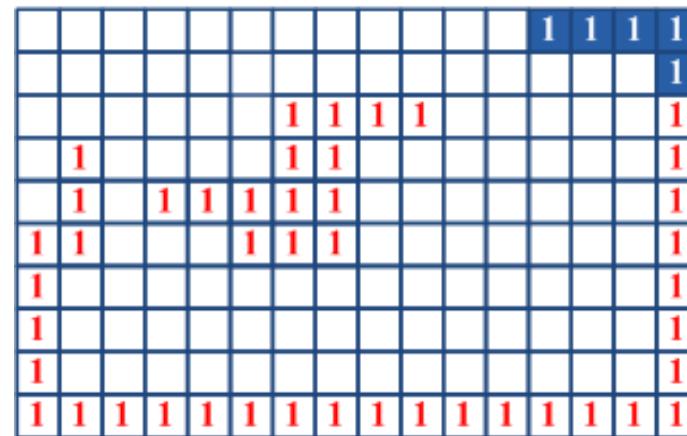
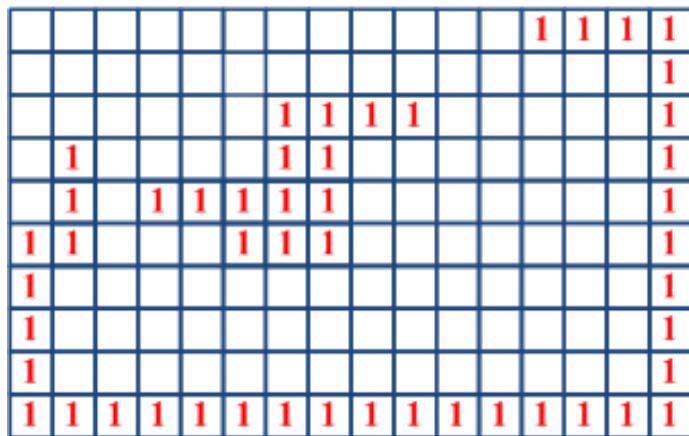
1	1		1	1	
1	1		1	1	
1	1	1	1	1	

# Algorithm 2: Classic Algorithm

- Two-Pass Algorithm
  - Pass 1:
    - Perform label assignment and label propagation
    - Construct the **equivalence relations** between labels when two different labels propagate to the same pixel.
    - Apply **resolve function** to find the transitive closure of all equivalence relations.
  - Pass 2:
    - Perform label translation.

## Algorithm 2: Classic Algorithm

- Example:



$$\{2=4\}$$

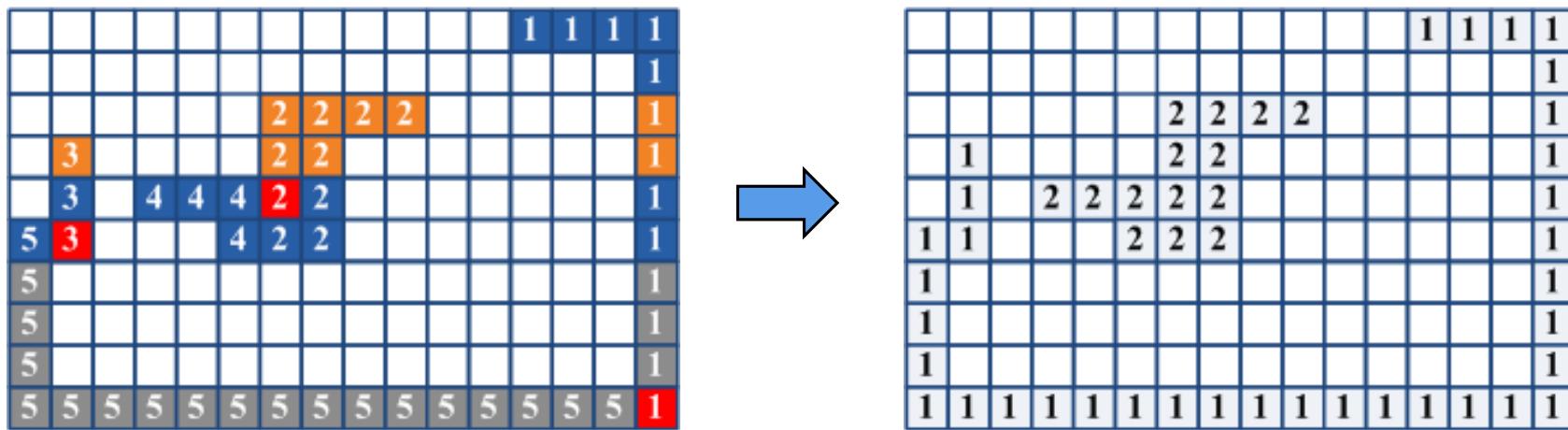
{3=5}

{1=5}

# Algorithm 2: Classic Algorithm

- Example:
  - Resolve Function

$$\{2=4\} \quad \{3=5\} \quad \{1=5\} \quad \rightarrow \quad \{2=4\} \quad \{1=3=5\}$$

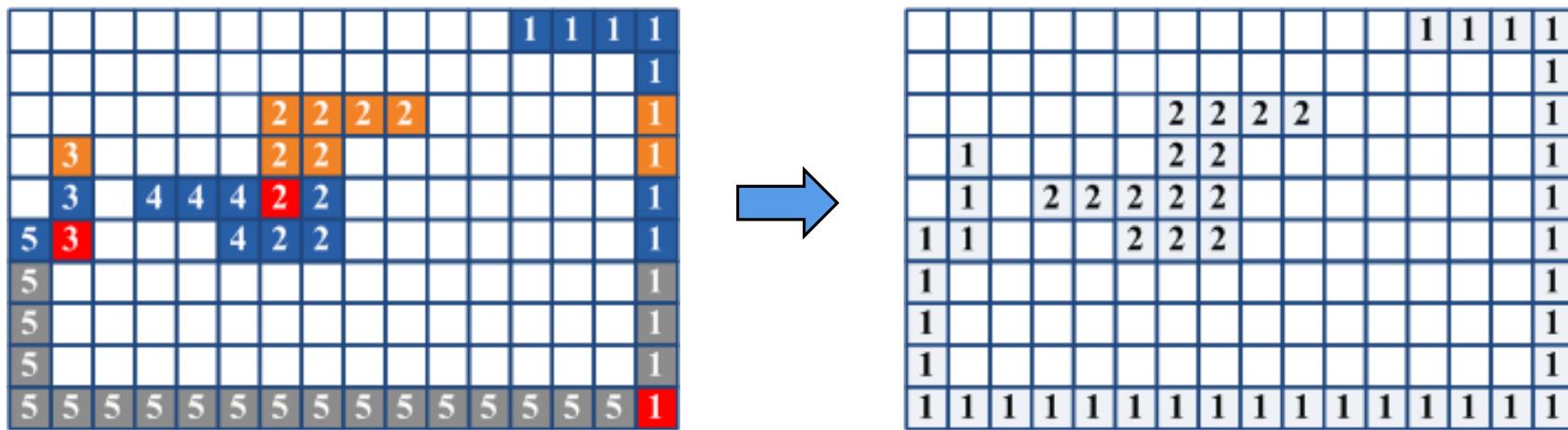


- Computational Efficiency
- Need a lot of space to store equivalence

# Algorithm 2: Classic Algorithm

- Example:
  - Resolve Function

$$\{2=4\} \quad \{3=5\} \quad \{1=5\} \quad \rightarrow \quad \{2=4\} \quad \{1=3=5\}$$



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