

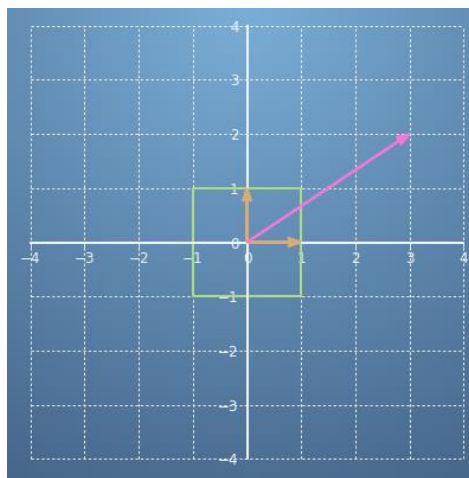
Using matrices to make transformations

TOTAL POINTS 6

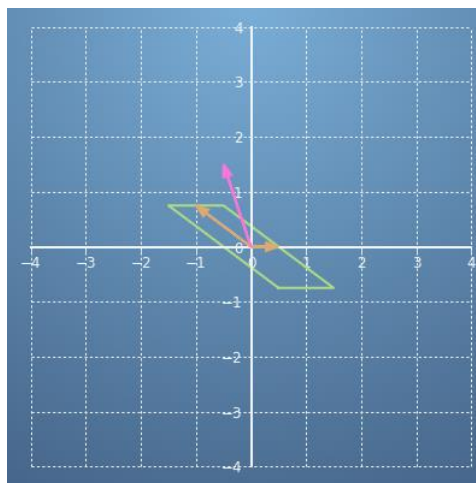
1.Question 1

Matrices make transformations on vectors, potentially changing their magnitude and direction.

If we have two unit vectors (in orange) and another vector, $r=[3 \ 2]$ (in pink), before any transformations - these look like this:



Take the matrix, $A=[1/20 \ -13/4]$, see how it transforms the unit vectors and the vector, r ,



What new vector, r' , does A transform r to? Specifically, what does the following equal?

- ☐ $[3/2 \ -1/2]$
- ☒ $[-1/2 \ 3/2]$

- ☐ $[-3/2 \ 3/2]$
- ☐ $[3/2 \ -3/4]$

1 / 1 point

2.Question 2

Let's use the same matrix, $A=[1/20 \ -13/4]$, from the previous question.

Type an expression for the vector,

$$s=A[-24].$$

Replace a and b with the correct values below:

$$s = [-5, 3]$$

RunReset

$[-5, 3]$

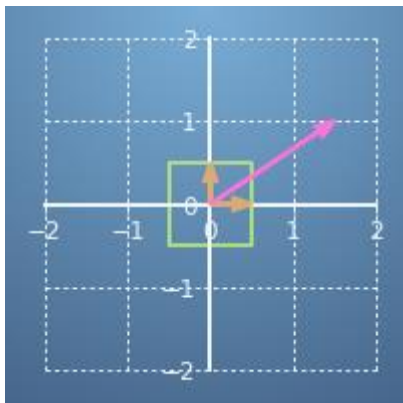
1 / 1 point

3.Question 3

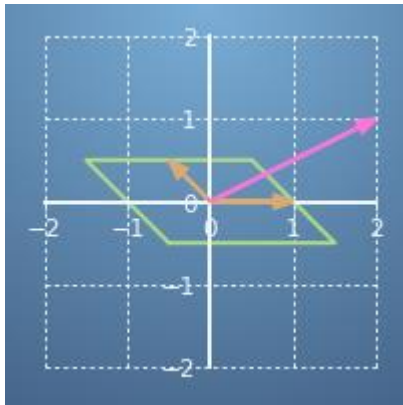
Select the transformation which best corresponds to the matrix,

$$M=[-1/2 \ 1/2 \ 1/2 \ 1/2].$$

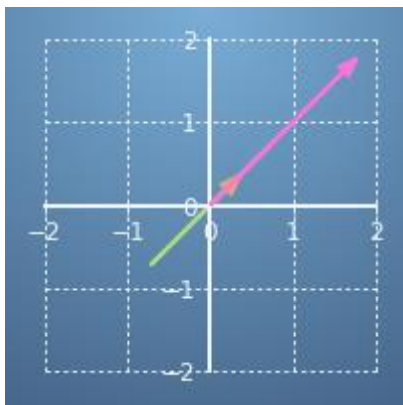
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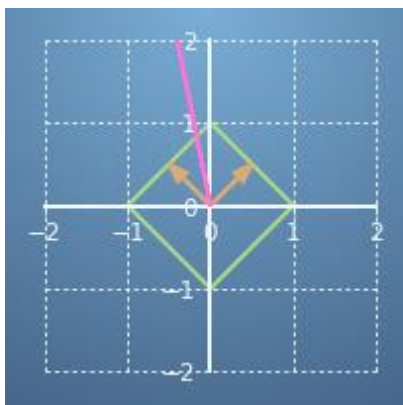
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○



●



1 / 1 point

4.Question 4

A digital image can be stored by putting lots of coloured pixels at their particular coordinates on a grid.

If we apply a matrix transformation to the coordinates of each of the pixels in an image, we transform the image as a whole.

Given a starting image (such as this one of “The Ambassadors” [1533] by Hans Holbein the Younger),



which is made up of 400×400 pixels, if we apply the same transformation to each of those 160,000 pixels, the transformed image becomes:



Pick a matrix that could correspond to the transformation.

☒
$$\begin{bmatrix} \frac{\sqrt{3}}{2} & -1/2 \\ 1/2 & \frac{\sqrt{3}}{2} \end{bmatrix}$$

1 / 1 point

5.Question 5

At the bottom of the “The Ambassadors”, in the middle of the floor, there is a skull that Holbein has already applied a matrix transformation to!

To undo the transformation, build a matrix which is firstly a shear in the y direction followed by a scaling in y direction. I.e., multiply the matrices,

$$M = \begin{bmatrix} 1 & 0 \\ 0 & 8 \end{bmatrix} \begin{bmatrix} 1 & -1/20 \\ 0 & 1 \end{bmatrix}$$

Replace a, b, c and d with the correct values below:

$$M = \begin{bmatrix} 1, 0, \\ -4, 8 \end{bmatrix}$$

RunReset

[[1, 0], [-4, 8]]

1 / 1 point

6.Question 6

Use your answer from the previous question to transform the skull back to normal. Change the values of the matrix and press *Go!* to score on this question.

You can also use this example to experiment with other matrix transformations. Try some of the ones in this quiz. Have a play!

Ans. [[1, 0], [-4, 8]]