

Project 3D data onto a 2D subspace

TOTAL POINTS 6

1.Question 1

For a vector $\mathbf{x} = [6 \ 0 \ 0]$ and the subspace U spanned by the basis vectors $\mathbf{b}_1 = [1 \ 1 \ 1]$ and $\mathbf{b}_2 = [0 \ 1 \ 2]$, which of the following statements are true?

You can use the formula slide that comes with the corresponding lecture.

4 / 4 points

- ☐ The coordinates of the projected point with respect to $\mathbf{b}_1, \mathbf{b}_2$ are $[0 \ 0]$.
- ☒ The projection of \mathbf{x} onto U is $[5 \ 2 \ -1]$
- ☐ The projection matrix is $[0 \ 0 \ 0], [0 \ 1 \ 2], [0 \ 2 \ 4]$
- ☒ The projection matrix is $1/6 [[5 \ 2 \ -1], [2 \ 2 \ 2], [-1 \ 2 \ 5]]$
- ☐ The projection matrix is not symmetric.
- ☒ The projection matrix is symmetric.
- ☐ The projection of \mathbf{x} onto U is $[0 \ 0 \ 0]$
- ☒ The coordinates of the projected point with respect to $\mathbf{b}_1, \mathbf{b}_2$ are $[5 \ -3]$.
- ☐ The rank of the projection matrix is 1.

2.Question 2

Project $[3 \ 2 \ 2]$ onto the subspace spanned by $[1 \ 0 \ 0]$ and $[0 \ 1 \ 1]$

You can use the formula slide that comes with the corresponding lecture.

1 / 1 point

- ☐ $[2 \ 1 \ 1]$
- ☒ $[3 \ 2 \ 2]$
- ☐ $[2 \ 1 \ 2]$
- ☐ $[6 \ 4 \ 4]$

3.Question 3

1. Project $[12 \ 0 \ 0]$ onto the subspace U_1 spanned by $[1 \ 1 \ 1], [0 \ 1 \ 2]$

2. Project the result from 1. onto the subspace spanned by

$[-10\sqrt{6} \ -4\sqrt{6} \ 2\sqrt{6}]$. What is the final projection?

Hint: For step 2. you do not necessarily need to compute anything.

You can use the formula slide that comes with the corresponding lecture.

1 / 1 point

- ☒ $[10 \ 4 \ -2]$
- ☐ $[5 \ 2\sqrt{6} \ -1\sqrt{6}]$
- ☐ $[5 \ 2\sqrt{6} + 1 \ -\sqrt{6} + 2]$