

Covariance matrix of a two-dimensional dataset

TOTAL POINTS 5

1.Question 1

Compute the covariance matrix for the following dataset

$$D = \begin{bmatrix} 12 \\ 54 \end{bmatrix}$$

Here, every column vector represents a data point.

Do the exercise using pen and paper.

1 / 1 point

- ☒ $\begin{bmatrix} 4 & 2 \\ 2 & 1 \end{bmatrix}$
- ☐ $\begin{bmatrix} 2 & 4 \\ 2 & 1 \end{bmatrix}$
- ☐ $\begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix}$

2.Question 2

Consider a data set D with covariance matrix

$$\begin{bmatrix} 3 & 2 \\ 2 & 4 \end{bmatrix}$$

What is the covariance matrix if we multiply every vector in D by 2?

1 / 1 point

- ☐ $\begin{bmatrix} 16 & 8 \\ 8 & 12 \end{bmatrix}$
- ☐ $\begin{bmatrix} 3 & 2 \\ 2 & 4 \end{bmatrix}$
- ☒ $\begin{bmatrix} 12 & 8 \\ 8 & 16 \end{bmatrix}$
- ☐ $\begin{bmatrix} 4 & 2 \\ 2 & 3 \end{bmatrix}$

3.Question 3

Consider the data set

$$D = \begin{bmatrix} 12 \\ 74 \end{bmatrix} \text{ with covariance matrix } \begin{bmatrix} 9 & 3 \\ 3 & 1 \end{bmatrix}$$

Compute the new covariance matrix when we add

$\begin{bmatrix} 2 \\ 2 \end{bmatrix}$ to each element in D .

1 / 1 point

- ☐ $\begin{bmatrix} 11 & 5 \\ 5 & 3 \end{bmatrix}$
- ☐ $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
- ☐ $\begin{bmatrix} 9 & 3 \\ 3 & 1 \end{bmatrix}$

4.Question 4

Provide a valid 2x2 covariance matrix by replacing the -1 entries in the code below.

1 / 1 point

```
def covariance_matrix():  
    """Return a valid 2x2 covariance matrix"""  
    covariance_matrix = np.array([[1, 0.8],  
                                   [0.8, 1]])  
    return covariance_matrix  
  
print(covariance_matrix())
```

RunReset

```
[[ 1.  0.8]  
 [ 0.8  1. ]]
```

5.Question 5

We are looking at a data set D where every element in D consists of an x and y coordinate. The data covariance matrix is given by $\begin{bmatrix} 1 & 0.8 \\ 0.8 & 1 \end{bmatrix}$

Which of the following statements is correct?

1 / 1 point

- ☒ x and y are positively correlated, i.e., when x increases then y increases on average, and vice versa.
- ☐ x and y are negatively correlated, i.e., when x increases then y decreases on average, and vice versa.
- ☐ x and y are uncorrelated, i.e., when x increases then y does not change on average (and vice versa).